

INVESTIGATION OF TISSUES ENDOGENOUS PULSATIONS FOR ULTRASOUND ELASTOGRAPHY_po pataisymo padalinyje

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PULSATIONS FOR ULTRASOUND
ELASTOGRAPHY

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Technological Sciences, Electrical and Electronic Engineering (T 001)

2021, Kaunas

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ABBREVIATIONS

ASA – angular spectrum approach
AUC – area under curve
BM – block matching
CCA – common carotid artery
CSD – cross-sectional distensibility
CVD – cardiovascular diseases
FM – feature matching
FWHM – full width at half maximum (of point spread function)
IMT – *intima-media* thickness
KZK – Khokhlov-Zabolotskaya-Kuznetsov
LOKI – longitudinal kinetics
MAE – mean absolute error
MCS – mean scatterer spacing
MSE – mean squared error
NRMSE – normalized root mean squared error
OF – optical flow
PSF – point spread function
PW – pulse wave
PWV – pulse wave velocity
PWV – pulse wave velocity
RF – radiofrequency
ROC – receiver-operating characteristic
ROI – region of interest
SNR – signal-to-noise ratio
TMM – tissue-mimicking material
US – ultrasound
USE – ultrasound elastography
VVI – velocity vector imaging

INTRODUCTION

Relevance of the Research

Cardiovascular diseases (CVDs) are the main cause of human death worldwide. Every year, more people die from this disease than from other. In 2019, the latest year for which worldwide statistics are calculated, globally 18.6 million people died from CVDs what reflects a 17.1% increase over the past decade ^[1]. 42.1% of the leading cause of death attributable to CVDs was from coronary heart disease ^[1], and atherosclerosis is a major cause of this disease. Global cardiovascular deaths are predicted to reach 23.6 million by 2030 ^[2]. Stroke, one of the several possible outcomes of CVD, represents the second cause of mortality and the sixth cause of permanent disability ^[3,4]. Prediction of cardiovascular events towards efficient patients' treatment is, therefore, a major public health issue ^[5,6,7,8,9]. Atherosclerosis, the underlying pathological mechanism, is a chronic and systemic vascular disease often referred to as a "silent killer", because its progression and evolution are tremendously complex and rather unpredictable, leading to an exceedingly high number of fatal events occurring without any precautionary sign ^[10]. Generally, in the long term atherosclerotic arterial affection is not noticeable, however general signs of this illness develop only after the onset of complications: thickening of the *intima-media* complex, narrowing of the lumen or its thrombosis, and/or loss of elasticity ^[11]. Atherosclerosis causes heart attacks, strokes, peripheral arterial diseases, and is all called CVDs, and myocardial infarction and stroke are described as the final stage of atherosclerosis ^[12].

Arterial stiffness is an independent predictor of cardiovascular events, and it is analyzed to assess cardiovascular risk ^[13,14,15]. *Intima-media* thickness (IMT), pulse wave velocity (PWV), and cross-sectional distensibility (CSD) are the most commonly used risk markers for arterial stiffness evaluation in clinical practice ^[16,17,18,19]. Unfortunately, the clinical potential of these traditional risk markers as a screening test remains limited ^[20]. It is difficult to evaluate the risk of CVDs in patients under the age of 50 especially in the absence of specific individual CVDs risk factors or anamnesis. As a result, assessing the likelihood of developing a disease and, if necessary, starting drug treatment is challenging ^[13].

Nonetheless, it has been proven that mechanical changes (i.e., longitudinal and radial motion of the arterial wall) appear much earlier than significant anatomical changes (i.e., IMT) of the arterial wall ^[12]. In recent years, radial motion has been widely studied and become a parameter describing the mechanical properties of the arterial walls. Becoming an informative non-invasive parameter, radial motion helps to investigate cardiovascular diseases and to determine the elasticity of arterial walls. The longitudinal motion has not received such recognition unlike the radial motion of the arterial wall. Comparing with the radial motion, it was believed that the longitudinal motion during the heart cycle was negligible. However, using modern ultrasound scanners, it has been noticed that the *intima-media* complex during the heart cycle moves not only in the radial but also in a longitudinal direction ^[21,22]. It has also been observed that as the radial motion the longitudinal motion of the

arterial wall has the same amplitude and reaches about one millimeter ^[23]. Furthermore, clinical investigations have linked longitudinal motion of the common carotid artery (CCA) to risk factors and CVDs ^[24,25]. Previous studies have shown a relationship between arterial stiffness, CVDs, and the decrease in longitudinal motion ^[12]. Even though longitudinal motion amplitude is linked to CVDs, the determinants of phases of longitudinal motion remain unknown ^[16].

Within the context of CVD risk assessment, the motion of arterial tissues during the cardiac cycle is important as mechanical deformation represents vessel elasticity and is putatively inversely related to arterial stiffness, an independent indicator of all-cause mortality and morbidity ^[26]. Arterial tissue motion during the cardiac cycle consists of radial (artery wall motion perpendicular to blood flow), longitudinal (*intima-media* complex motion in parallel with blood flow) motions, and circumferential strain. Using several motion tracking techniques, the motion of the arterial tissue from sequences of ultrasound (US) radiofrequency (RF) signals or images has been analyzed and summarized by Rizi *et al* in ^[27].

Currently, available ultrasound elastography (USE) techniques can be classified into two major groups according to the measured physical quantity: 1) strain imaging, 2) shear wave imaging ^[28]. Both these groups of methods use an external source of stress. Nevertheless, an internal source of deformation or so-called endogenous motion in the tissue induced by heartbeat and vascular activity could be used in elasticity measurement ^[29,30,31].

Methods, based on endogenous motion detection, are not applied in clinical practice these days. Firstly, these methods should be carefully studied and investigated. Due to this, computational ultrasound imaging could be used to simulate US RF signals or B-scan images from measurements using algorithms that are dedicated to this purpose. The most popular simulation software packages ^[32,33,34] are CREANUIS ^[35] (based on Khokhlov-Zabolotskaya-Kuznetsov (KZK) equation) for nonlinear propagation and simulation of harmonic imaging and Field II ^[36] (based on Huygens principle and hybrid digital-analytic method) which gained a wide application since the publication of model in 1991 ^[37] and software package in 1996 ^[38]. The popularity of Field II lies in considerable flexibility to accommodate a wide range of transducers, beamforming options, and imaging possibilities. It is still a powerful and evolving tool for simulation of various scanning and focusing modalities as well as whole echoscopy mechanism including scattering in the tissues and organs ^[39]. Although there are a lot of Field II applications described in many articles, only a few publications deal with the quantitative comparison of simulation and experiment evaluating uncertainties ^[40,41].

The motion of the carotid artery wall has been modeled by many authors. Gemignani *et al.* ^[42] simulated radial motion as Sawtooth function, while Solomon *et al.* ^[43] as triangular function. As reported by Deng *et al.* ^[44], they proposed a geometric model of a common carotid artery (CCA) where the dynamic scatterers model is constructed by moving the positions of the scatterers according to the synthesized pulse wave (PW). The PW is estimated from the *in vivo* RF signals of the vessel wall using a 1-D normalized cross-correlation (NCC) algorithm based on echo

tracking. For the motion in the radial direction, Hu *et al.* [45] proposed an isotropic pulse model with elasticity to describe the relationship between radial displacement and blood pressure. However, neither of the previous studies considers the longitudinal motion of the artery together with radial and longitudinal motions slope deep into the tissue. It was done by Stoitsis *et al.* [46] simulating the radial motion as pulse function which parameter values were determined based on experiments with *in vivo* data. The longitudinal motion was modeled as a sinusoidal function because there is no conclusive information about the mathematical modeling of this motion. Based on a similar *in vivo* examination, the spatial dependence of radial and longitudinal motions, which are independent of the axial position, was also incorporated.

The longitudinal motion, a new, non-invasive parameter for elasticity measurement is still not fully exploited for evaluating cardiovascular risk, therefore it has a lot of potentials. Also, computational ultrasound imaging must deal with the quantitative comparison of simulation and experiment evaluating uncertainties before the simulation of US RF signals or B-scan images for the development of methods for endogenous motion detection. All these facts raise scientific-technological problem and a working hypothesis.

Scientific-technological problem and working hypothesis

Methods, based on endogenous motion detection, are not applied in clinical practice these days. First, these methods should have three “in” steps before wide usage: 1) approach justification *in-silico* to understand, develop and verify the method, 2) testing *in-vitro* to optimize, double-check and validate pilot results, and finally 3) certification *in-vivo* to fine-tune and confirm the reliability of the proposed method. Due to this, before *in-vitro* and *in-vivo*, computational ultrasound imaging could be used to simulate US RF signals or B-scan images from measurements using algorithms that are dedicated for this purpose. There is no 3D artery model capable of fully reproduce the biomechanical behavior of human CCA and appropriate for simulation of US RF signals and B-scan image sequences with Field II.

The working hypothesis of this thesis: tissue endogenous microdisplacements, induced mainly by the blood pulsation in vessels, could be used for tissue elasticity (or stiffness) evaluation and early detection of atherosclerosis.

Research object

The research is based on the development and investigation of the algorithms for simulation of common carotid artery wall motion for early diagnosis of atherosclerosis.

The aim of the research

The aim of this doctoral thesis is to develop and investigate an ultrasound radiofrequency signals-based algorithm for common carotid artery wall motion simulation associated with the early diagnosis of atherosclerosis.

The objectives of the research

To achieve the aim, the following objectives were formulated:

1. To develop and investigate a virtual scanning simulation adequate to physical ultrasonic scanning.
2. To create a 3D artery model capable to reproduce the biomechanical behavior of human CCA for simulation of US RF signals.
3. To investigate and evaluate the accuracy of the proposed motion detection algorithms using simulated CCA US RF signals.
4. To investigate the capability to differentiate arteries by motion slope profiles.
5. To collect US RF data from healthy volunteers and patients at increased risk of CVD group, investigate and compare motion parameters between two different populations.

Scientific novelty

In this doctoral thesis, a quantitative evaluation of the main resolution uncertainties arising in digital US linear scanning simulation by Field II and comparing them with physical phantom's scanning results was done. This leads to the conclusions on quantitative uncertainties of point spread function (PSF) and resolution in elevation plane using standard phantoms.

A dynamic 3D artery model capable of reproducing realistic dynamic RF signals of pulsating human blood vessels surrounded by viscoelastic tissue was developed.

Practical significance

Quantitative ultrasound imaging allows simulating raw RF signals adequate to those obtained from real ultrasonic scanning.

The proposed dynamic 3D artery model allows simulation for 3D deformation elastography, development and verification of elastography algorithms, 3D elastography experiments, and feasibility studies.

The approaches provided in this thesis were being developed and used in support of the following project "Investigation of radiofrequency based ultrasonic strain elastography algorithms (ELASTUS)". No.: S-MIP-19-8, work was funded by Research Council of Lithuania in the frame of Researchers group project, 2019-2022.

The statements presented for defense

1. Virtual scanning simulation adequate to physical ultrasonic scanning was developed. Digital scanning shows a good agreement with the physical one: full width at half maximum (FWHM) estimates of PSF in the axial and lateral directions are according to practical estimates with a discrepancy of less than 12 % and 16 % correspondingly.
2. A 3D artery model capable to reproduce the biomechanical behavior of human CCA for simulation of US RF signals has been created. The echoscopy simulation shows that the artery model represents an A, B and M-mode image structure like an *in vivo* artery wall has. The evaluated simultaneous radial and longitudinal motion of the virtually scanned 3D

structure over a single pulse is visually almost indistinguishable from generated motion pattern.

3. The accuracy of the proposed motion detection algorithms using simulated CCA US RF signals was investigated. The results demonstrate that the variety of accuracy evaluation parameters for radial and longitudinal motions detection are capable to access not only error but also evaluate dissimilarities between estimated and theoretical motion signals.
4. The capability to differentiate arteries by motion slope profiles was investigated. The results demonstrate that the variety of slope profiles of radial and longitudinal motions that defines different elasticity tissues may be used for the differentiation of healthy volunteers and at-risk patients.
5. The US RF data from healthy volunteers and patients at increased risk of CVD group was collected, motion parameters of two different populations were calculated and those parameters diagnostic ability to diagnose patients with and without the atherosclerosis was evaluated. The highest sensitivity of the proposed time and frequency domain parameters has displacement, *i.e.* 0.77 and spectral spread, *i.e.* 0.86. The velocity and spectral centroid assigned as parameters with the highest specificity resulting 0.88 and 0.71 correspondingly.

Approval of the results

In total, the results of the dissertation were published in 9 publications, of which 5 articles were published in the Journals of the Master List of Thomson Reuters Web of Science (with impact factor). The results were presented in 2 international and 1 national scientific conference: World Congress on Medical Physics and Biomedical Engineering (IUPESM 2018), 2019 IEEE International Ultrasonics Symposium (IUS), and Bioateitis: gamtos ir gyvybės mokslų perspektyvos 2019. In 2020, a doctoral scholarship, granted by the Research Council of Lithuania, was received. In 2019 and 2020, PhD Students Scholarships for Achievements, granted by KTU was received.

Structure of the Doctoral Thesis

The dissertation consists of an introduction, 3 chapters, general conclusions, summary, the list of references, the list of publications and conferences of the author and 2 appendixes. The thesis consists of 149 pages, 54 figures, 4 tables, 21 formulas, and 175 references. The content of the thesis is organized as follows: Chapter 1 describes the CCA anatomy and histology, longitudinal motion of artery wall, currently proposed digital artery models, adequate simulation of real ultrasound echoscopy, and algorithms for artery wall motion tracking. Chapter 2 presents the CCA US examination, developed modeling and verification of a digital simulation of physical US scanning, created a digital artery model, and developed RF US signals post-processing algorithms. Chapter 3 shows the experimental results of modeling, investigation of motion detection accuracy, and *in vivo* radial motion parametrization. Chapter 4 is dedicated to general conclusions.

1. AN OVERVIEW OF THE MOTION OF THE COMMON CAROTID ARTERY AND APPROACHES FOR MOTION DETECTION

1.1. Common carotid artery anatomy and histology

The left common carotid artery CCA originates in the neck from the aortic arch in the thorax, while the right common carotid artery from the bifurcation of the brachiocephalic trunk. The left and right common carotid arteries in the thorax extend on both sides of the throat and go through the superior thoracic aperture to the neck where enters the carotid triangle (see Figure 1.1). This triangle is situated at the front of the neck and bounded by the sternocleidomastoid muscle, omohyoid muscle, and the posterior belly of the digastric muscle ^[47].

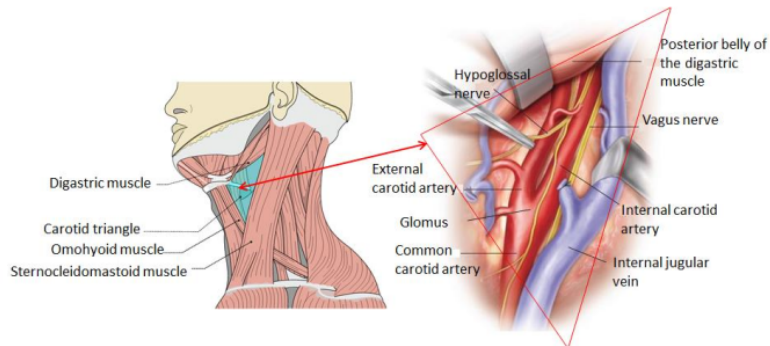


Figure 1.1. Anatomy of the common carotid artery. The left side of the neck is represented (adapted from ^[48])

The main contents of the carotid triangle are made up of the common carotid artery, the hypoglossal and vagus nerves, and the internal jugular vein. At the level of the superior margin of the thyroid cartilage or at the level of the fourth cervical vertebra (C4), the common carotid arteries split into the external and internal carotid arteries ^[49]. The carotid artery is close enough to the outer skin to press down on it and feel the carotid artery pulse. It is one of the larger arteries that the throb of the artery as the walls distend or widen could be felt with each heartbeat.

The histological structure of the CCA wall consists of three layers (see Figure 1.2) ^[17,50]:

- The innermost layer is called the *tunica intima*. This layer is composed of endothelial cells. A membrane composed of an elastic fiber, which is called the *internal elastic lamina* separates the inner layer from the middle layer.
- The middle layer is called *tunica media*. mainly composed of longitudinal smooth muscle cells, surrounded by connective tissue mainly compose this layer. The combination of the inner and middle layers is called the *intima-media* complex.

- The outermost layer is called the *tunica adventitia*. This layer is composed of connective tissues, mostly collagen fibers. Finally, the outer layer gradually extends into the surrounding connective tissue.

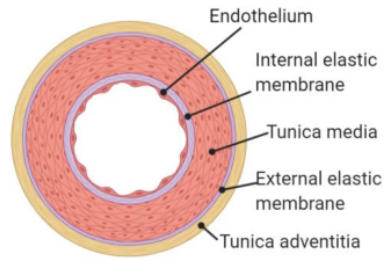


Figure 1.2. Histological structure of common carotid artery

1.2. Longitudinal motion of artery wall

During systole, ventricular contraction ejects blood into the major arteries resulting in expansion of the arteries, while during diastole when ventricles are relaxed, the elastic walls of the blood vessels return to their initial position thus pushing the blood to the periphery. In addition, the pulsating blood flow is caused by radial expansion of the arteries, most arteries (carotid, brachial, popliteal arteries) have a longitudinal motion, *i.e.* movement parallel to blood flow, which characterizes vascular elasticity. It has been assumed that longitudinal motion is negligible compared with the diameter change or radial motion. However, using modern ultrasound scanners, it has been noticed that *intima-media* complex during the heart cycle move in both radial and longitudinal directions ^[21,22]. The longitudinal motion of the arterial wall has been observed to have the same amplitude as the radial motion and reaches around one millimeter ^[23].

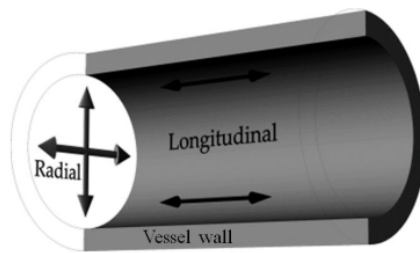


Figure 1.3. A schematic figure of a vessel showing the directions of the longitudinal and the radial motions (adopted from ^[22])

Distinct multiphasic bidirectional longitudinal motion of the *intima-media* complex could be observed during the cardiac cycle (see Figure 1.4.). The first

antegrade motion (1) (i.e. motion in the direction of blood flow) of the *intima-media* complex is observed at the beginning of systole. Later, still in systole, the first retrograde motion (2) (i.e. motion in the opposite direction of blood flow) of this complex appears. During diastole, the second antegrade motion (3) of the *intima-media* complex follows, and finally, it gradually returns to its original position (4). The first antegrade longitudinal motion (1) and the distension of the artery started almost simultaneously. The retrograde longitudinal motion (2) starts at almost the same time as positive and second antegrade motion (3) as the negative slope of the diameter. The direction of blood flow in the artery is antegrade throughout the length of systole and diastole and the longitudinal motion is of the same magnitude as diameter change ^[21].

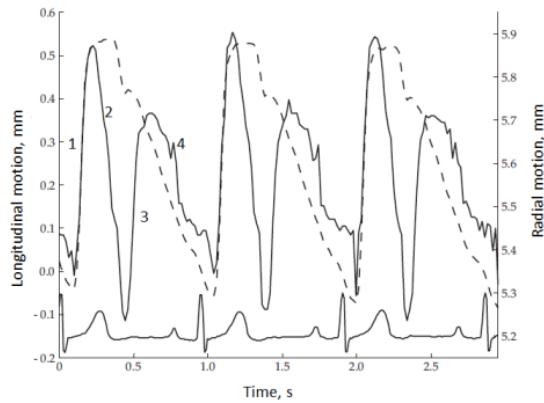


Figure 1.4. CCA longitudinal motion of the *intima-media* complex (—) and radial motion (---) in relation to the electrocardiogram (bottom trace). The numbers (1,2,3,4) indicate the phase of longitudinal motion during the cardiac cycle. Longitudinal motion is of the same magnitude as diameter change. Note pattern of multiphasic longitudinal motion: retrograde motion during late systole (2) and second antegrade motion during diastole (3) (adapted from ^[21])

Cinthio *et al.* ^[21] supported by Nillson *et al.* ^[51] shown that the *adventitia* layer of the artery wall had the same basic pattern of longitudinal motion, but the magnitude of motion is smaller than that of the *intima-media* complex thus demonstrating the presence of previously unknown substantial shear strain, and thus shear stress, intramurally. In demarcation between the *media* and the *adventitia* layers (likely at the external elastic lamina, which is a layer of elastic connective tissue lying between the abovementioned two layers) (see Figure 1.2), it seems that occurs the largest longitudinal shearing and thus shear strain. Summing up, it seems that the *media* and the *adventitia* slide against each other at the *external elastic lamina* (see Figure 1.5).

Later, this phenomenon was named by Zahnd *et al.* ^[52] as “longitudinal kinetics” (LOKI) – a cyclic shearing motion of the arterial wall when the *intima-media* complex moves with respect to the *adventitia* layer parallel to the direction of blood flow during the cardiac cycle. LOKI was observed in the abdominal aorta, carotid, brachial, popliteal arteries. Studies have shown that the parameter of “longitudinal kinetics” reflects the stiffness of the arteries and the presence of cardiovascular risk factors ^[21,52].

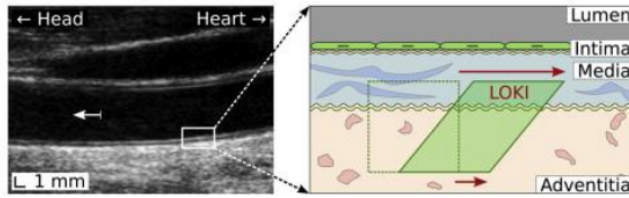


Figure 1.5. Longitudinal B-mode ultrasound image of a healthy CCA *in vivo* (left). The direction of the blood flow in the lumen is indicated by the white arrow. LOKI occurring within the concentric layers of the wall during the heartbeat (right). Please note that the tissue motion obeys a multiphasic and bidirectional pattern, in both retrograde and antegrade directions during the cardiac cycle. Source: Zahnd *et al.* ^[52]

The geometry of the walls of blood vessels is affected by the blood flowing through them. Elastic arteries (aorta, pulmonary arteries) have a “shock-absorbing” function that allows them to maintain a relatively constant pressure gradient despite the constant pumping action of the heart making the flow of pulsating blood from the heart continuous ^[53].

During systole, when the left ventricle contracts, blood is pushed out from the heart into the circulatory system. The ejected blood expands the elastic walls of the blood vessels and thus the blood vessels accumulate a portion of the blood ejected by the heart. During diastole, when the left ventricular valve closes, the walls of the blood vessels contract, pushing the blood away. This causes an arterial pressure wave to travel through the arteries, called a pulse pressure wave. This wave travels through the arteries at a much higher rate than the speed of blood particles. The PW depends on the elasticity of the artery wall, causing the almost simultaneous flow of blood in the arteries ^[54].

Despite the fact that the arteries expand in the radial direction as they propagate in a pulse pressure wave, the longitudinal motion of the arterial walls is also observed. As already mentioned, longitudinal motion of arterial walls has long been considered negligible or absent. The longitudinal motion was first observed by Lawton and Greene (1956) who performed studies with the abdominal aorta ^[55]. Later, the results were confirmed by Patel *et al.* (1961) in studies with the thoracic aorta ^[56]. Longitudinal movement of the thoracic aorta was very small and diaphragm movements during respiration were thought to be mainly the result of the onset of longitudinal arterial wall motion. Subsequent studies have shown that the inner layers of the arterial walls, *i.e.* *intima-media* complex, move not only in the radial but also

in the longitudinal directions during a pulse wave propagation^[57]. Breathing was thought to cause longitudinal movement of the arterial walls. However, much more reproducible longitudinal movement of the artery wall was observed when patients were asked to hold their breath during the examination^[23].

Another factor that would affect the longitudinal movement of the artery wall is the shear stress caused by shear strain, when the *intima-media* complex of the vessel moves more than the outer layer of the vessel^[58]. Artery wall shear stress is dependent on the blood viscosity and the blood velocity gradient at the vessel wall (wall shear rate). As the blood velocity increases, does the shear rate. Later studies had shown that there is no correlation between the longitudinal motion and the wall shear rate and thus, the wall shear stress^[59].

The cardiac cycle consists of systole and diastole, during which blood pressure in the blood vessels changes. Normally, systolic blood pressure is 120 mmHg and diastolic blood pressure is 80 mmHg^[53]. Studies have shown that adrenaline can significantly increase the longitudinal movement of the artery wall, and during systole, the longitudinal movement of the *intima-media* complex can increase by more than 200 % at the highest blood pressure levels as compared to baseline^[15]. Also, the administration of drugs that increase heart rate and blood pressure (such as norepinephrine) has an effect on the increased longitudinal movement of the artery wall^[58].

Recent studies have shown that longitudinal motion of the carotid artery is progressively attenuated along the length of the artery as it is located away from the heart. As an obvious decrease in the amplitude of motion along the carotid artery exists, it is quite clear that cardiac factors can affect the amplitude of longitudinal motion in the wall of the carotid artery. However, no studies have been performed to directly measure the influence of cardiac mechanics on the longitudinal motion^[52].

It has been hypothesized that there is a simultaneity between the timing of retrograde longitudinal motion and left ventricular mechanics, and the timing of anterograde longitudinal motion and the local blood flow events at the carotid artery. Studies have shown that there is no difference in time between peak blood velocity and peak anterograde motion. However, in terms of time, a difference was obtained between the time at peak retrograde longitudinal motion and the time of peak apical and basal rotations of the left ventricle. Amplitude studies revealed a strong correlation between peak retrograde longitudinal motion and peak basal rotation of the left ventricle, but no correlation between apical rotation or basal septal longitudinal motion. The researchers concluded that there is a temporal relationship between the anterograde longitudinal motion of the carotid artery wall and blood velocity. Meanwhile, the retrograde longitudinal motion in terms of time and amplitude is related to the rotation of the left ventricle, but not to the longitudinal septal displacement as originally hypothesized. The determinants of the phases of longitudinal motion remain unknown despite preliminary evidence of a link between longitudinal motion and cardiovascular health^[16].

1.3. Review of digital dynamic artery models

The literature on digital dynamic artery models shows a variety of approaches and the motion of the carotid artery wall has been modeled by many authors. Gemignani *et al.* [42] simulated the artery as a cylinder and radial motion as Sawtooth function. Synthetic images were obtained by using the Field II ultrasound simulation program. Within the volume of the phantom, 100 000 scatterers were randomly distributed and strong scatterers were placed to simulate boundaries. Images were made by simulating a 13 MHz linear array probe with 192 elements. Only several parameters were presented for B-mode imaging and ultrasonic probe simulation what is a limitation of this study. A total of 100 images were created to simulate five cardiac cycles. The main purpose of this simulation was to estimate the accuracy of the algorithm in assessing the diameter by using the absolute error parameter.

Another solution is presented by Solomou *et al.* [43] where artery radial motions had a triangular function. In this approach, synthetic images were based on the clinical structure of the CCA and the grayscale median levels for each area, i.e. blood, *intima-media* layer, *adventitia*, were proposed. Nonetheless, realistic B-Mode ultrasound videos of the artery were generated by using MATLAB based simulation procedure instead of Field II. Speckle noise in ultrasound videos was applied using a random distribution with a noise variance of 0.01 to 0.06. The simulated video consisted of 120 images which correspond to three cardiac cycles. Mean squared error was used to compare the result of automated and manual measurements of the CCA diameter.

As reported by Deng *et al.* [44], they proposed a geometric model of CCA where a blood vessel was represented as a concentric cylinder (see Figure 1.6).

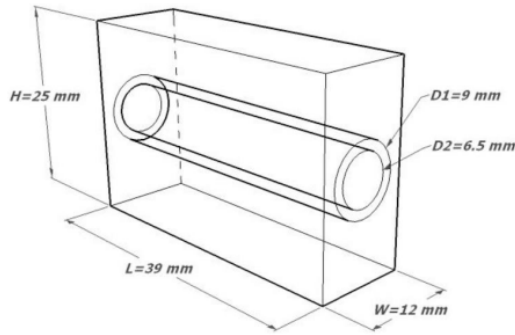


Figure 1.6. Geometric model of a segment of the CCA. Source: Deng *et al.* [44]

The scatterers in the artery model were randomly distributed within the volume of the model and the amplitudes of the scatterers followed Gaussian distribution. The intensity of the scatterers of the blood flow was set to zero, while the vessel walls were set to five times the intensity of the surrounding tissue. Even though the abovementioned studies do not take into account the number of scatterers per resolution

cell (resolution cell is the minimum volume that can be extracted by the imaging system^[60]), but Deng *et al.* did it. What is more, parameters of the B-mode imaging and ultrasonic probe used in the ultrasound simulation based on the Field II program were presented in detail, for example, center frequency 10 MHz, sampling frequency 100 MHz, frame rate 1333 Hz, ultrasound velocity 1540 m/s, etc. The motion in the dynamic scatterers model of the artery is constructed by moving the positions of the scatterers according to the synthesized PW. The PW is estimated from the *in vivo* RF signals of the vessel wall using a 1-D NCC algorithm based on echo tracking. The artery model was proposed to provide a realistic data source for validation pulse wave velocity (PWV) estimation algorithms. To quantitatively verify the effectiveness of the simulation model, the normalized root mean squared error (NRMSE) was used to compare the estimated and preset PWV.

For the motion in the radial direction, Hu *et al.*^[45] proposed an isotropic pulse model with elasticity to describe the relationship between radial displacement and blood pressure. For the motion in the axial direction, longitudinal motion of *intima-media* complex was extracted from a healthy subject and directly used to get a realistic simulation of pulsatile motion in the longitudinal direction. Hu *et al.* suggested that to obtain the values of parameters of scatterers distributions, including the shape parameter, density, and intensity, for arterial layers and blood, the envelope signals simulated from different configurations of scatterers distribution could be compared with those from different kinds of tissue of CCA *in vivo* through a statistic analysis and this seems an innovative approach. As Deng *et al.*^[44], Hu *et al.* also detailed parameters of the B-mode imaging and ultrasonic probe used in the ultrasound simulation based on the Field II program. The artery model was proposed for the validation of two-dimensional wall motion and blood velocity estimation algorithms.

However, neither of the previous studies considers the radial and longitudinal motions slope deep into the tissue. To the author's best knowledge, very few publications can be found in the literature that addresses the issue of artery motion slope. It was done by Stoitsis *et al.*^[46]. The radial motion was defined in a piece-wise fashion using pulse function which parameter values were determined based on experiments with *in vivo* data. The longitudinal motion was modeled as a sinusoidal function because there is no conclusive information about the mathematical modeling of this motion. Based on a similar *in vivo* examination, the spatial dependence of radial and longitudinal motions, which are independent of the axial position, was also incorporated. Later, Golemati *et al.*^[61] proposed to use pulse function to model not only radial motion but also longitudinal. Function parameters were accessed during an experiment with real data, but only five subjects were incorporated in this investigation. Such a small sample of subjects is not sufficient to describe pulse function parameters. What is more, there is a large variety of longitudinal motion patterns between individuals^[58,62,63] making longitudinal motion modeling difficult.

1.4. Adequate simulation of real ultrasound echoscopy

US imaging is the most widely used imaging modality in clinical practice due to its low cost, non-ionizing nature, noninvasiveness, and real-time imaging. US imaging technologies are continuously evolving. A lot of imaging advancements are related to the processing and parametrization of raw RF echoscopy signals, opening new possibilities in tissue elastography, quantitative imaging, and parametric mapping of quantitative tissue parameters valuable for differential diagnostics.

A powerful tool for further developments and modifications is modeling and simulation of all echoscopy processes, especially in the RF domain. This *in silico* approach potentially allows simulating new concepts, methods, and implementations, which are unavailable in a clinical environment and even in laboratory experiments. However, success decisively depends on the quantitatively evaluated adequacy of simulation to the real echoscopy situation. Therefore, the simulation method and quantitative evaluation of involved simulation uncertainties are highly important. The general method of uncertainty quantification in simulation models proposed in [64] is based on consecutive forward uncertainty propagation (from the system under simulation towards the output of the system model) and the backward uncertainty quantification (consecutive evaluation uncertainty components from system model output to the real system). In the case of US echoscopy, the simulation uncertainty components are related to models of multi-element transducer and beamforming, US wave propagation and 3D field, backscattering, and speckle formation in nonhomogeneous tissue, transmit-receive mode, RF data acquisition, and preprocessing. Therefore, echoscopy deals with complex interlinked modeling and simulation tasks and requires reliable simulation methods and software tools.

Adequate modeling of US wave propagation in the biological tissue involves solving the nonlinear KZK equation which can also be derived as the parabolic approximation to the Westervelt equation [65]. The direct solution of equations is quite complicated and limited to directional wave propagation. From the KZK equation was derived computational resource-saving K-wave model and angular spectrum approach (ASA), which are based on some simplified assumptions of linearity and space invariance of PSF [66,67,68]. These methods balancing between adequacy and needed computational resources are used for US field modeling and simulation of the wave propagation in tissue [69], but not directly applicable for the transmit-receive scanning of scattering media by multi-element transducer arrays.

The most popular simulation software packages are CREANUIS [35] (based on KZK equation) for nonlinear propagation and simulation of harmonic imaging and Field II [36] (based on Huygens principle and hybrid digital-analytic method) which gained a wide application since the publication of model in 1991 [37] and software package in 1996 [38]. The popularity of Field II lies in considerable flexibility to accommodate a wide range of transducers, beamforming options, and imaging possibilities. It is still a powerful and evolving tool for simulation of various scanning and focusing modalities as well as whole echoscopy mechanism including scattering in the tissues and organs [39]. Scanning by a linear array transducer simulated by both Field II (as a reference) and ASA shows that Field II is effective in the simulation of

the US field generated by the transducer, while ASA – in nonlinear propagation^[70]. Comparison of several new resources-saving simulation tools for fast simulation of US data has shown^[71] that methods based on the principle of convolving a set of point scatterers with a PSF do not simulate the process of US field and beam formation and interaction in echo mode in contrast to Field II. Simulations of plane wave images made with Field II using wire phantom and a tissue-mimicking phantom having anechoic cysts^[72] have shown a high value of simulation which could be applied for optimization of imaging.

Digital models of tissues and organs are also a component of *in silico* echoscopy and a source of simulation uncertainty. Nonhomogeneous tissue is usually simulated by discrete digital phantoms based on the small scatterers distributed in space. The proper setting of scatterer maps is essential for the realistic resulting image of ultrasonic wave interference (speckle) pattern^[73]. Mean scatterer spacing (MCS) for different tissues was reviewed in^[74] showing the potential to simulate tissue microstructure by fitting the MCS parameter. Scatterer maps also could be generated from real images, by solving the inverse-problem of US speckle formation^[75].

Most simulation results are for the case of the linear scanning transducer arrays. Articles mainly use Field II simulation results as a reference for the analysis of some US imaging development without prior assessment of simulation adequacy. Although there are a lot of Field II applications described in many articles, only a few publications deal with a quantitative comparison of simulation and experiment evaluating uncertainties. The brief comparison of Field II simulation and experimental results provided on wire images was presented in^[40,41,76].

As reported by Pham et al.^[41], to validate simulated PSF physical wire phantom was used. In both, physical experiments and digital simulation 10 MHz linear array transducer was used. The simulated wire phantom was adequate to the measured one, *i.e.* the positions of the point scatterers were the same as in the measured wire phantom: 41.8 mm, 51.7 mm, 61.6 mm and 71.6 mm away from the transducer in the axial direction. The discrepancy between the FWHM of the measured and simulated resolutions were 6.7 %, 0.6 %, 0.1 %, and 10.4 % in the lateral direction and 17 %, 15 %, 16.7 %, and 21 % in the axial direction, respectively.

The same methodology as Pham *et al.*^[41] used Mattausch and Goksel^[40]. The difference between parameters was that Mattausch and Goksel used the 6.6 MHz linear array transducer for measurement and simulation instead of 10 MHz as Pham *et al.*^[41] done. The positions of the point scatterers were the same as in the measured wire phantom: 40.4 mm, 60. mm, 86.6 mm away from the transducer in the axial direction. The error between the FWHM of the measured and simulated resolutions were 0 %, 6.3 %, and 0.5 % in the lateral direction and 6.5 %, 12.4 %, and 4.9 % in the axial direction, correspondingly.

Another group of researchers^[76] obtained wire phantom images by both 35 MHz linear array and Field II simulation of the array. The measured –6dB lateral width at the wire targets was 175 μm , 165 μm , 200 μm , 260 μm , while the simulated –6dB lateral width by Field II was 155 μm , 165 μm , 175 μm , 245 μm accordingly.

quantitative assessment of adequacy. The comparison of Field II simulation and experimental results was presented without a quantitative assessment of adequacy.

Quantitative results of simulation and dealing with experimental verification of such simulations are presented further when the other types of arrays were incorporated into research. Phased array lateral PSF width at 60 mm depth was simulated with Field II for 5 MHz frequency by ^[77] and FWHM was obtained 1.4 mm without experimental verification of this result since experiments were provided with a curvilinear array transducer. Field II simulations performed for a 3.5 MHz phased array with focal depth at 30 mm and spatial resolution was quantified by measuring lateral FWHM width in resolution target phantom ^[78]. Simulated resolution (FWHM) with the phased array at focal depth was 1.01 mm lateral and 0.6 mm axial. But again, simulations were not verified since compared with experimental results of curvilinear array transducer of 3.1 MHz. Simulated lateral FWHM which is found minimal at a focal distance is almost double wider in the near field (1.5 mm at 1cm) or far field (2.41mm at 5cm). Field II calculation results were obtained for point reflector at a distance of 2d, where d is the length of the phased array with 64 elements ^[79]. At frequency 3.5MHz and distance of 2d the FWHM of the lateral main lobe was obtained about 2 degrees of angle; without experimental verification of this result.

By the Field II simulation of phased 1.75D array was shown that beam width in elevation direction (or scanning slice thickness) has a significant influence in B-image contrast reproduction ^[80]. This was shown by experimental contrast verification with a phantom of spherical inclusions, but no verification of quantitative beamwidth estimates in elevation direction was provided. Experimental analysis of elevation beamwidth profiles made for the freehand ultrasound calibration purposes have shown the importance of scanning slice thickness for linear-array transducer calibration accuracy ^[81], but no results for linear array provided and no digital simulations. Improvement of ultrasound transducer radiation beam profile was verified by hydrophone scanning of the pressure field ^[82], but not simulated. So quantitative comparison of linear array simulation with an experiment including analysis of resolution in elevation direction remains limited.

The problem of simulation adequacy is especially crucial for USE, where tissue displacements could be extremely small and resolution in strain estimation is important ^[83]. For example - Field II could be used not only for static US images but also for pulsating carotid artery simulation ^[46]. It is also effective in combination with a convolution-based method ^[84] which shows the potential of 3D moving scatterers and tissue deformation modeling using the finite element method and then the corresponding pre-/post-deformation RF signals comparison using Field II ^[85,86]. Despite the very wide use of Field II simulation software, the remaining problem actual for the development of new imaging modalities including USE is a quantification of simulation uncertainty, especially for sector scanning. Adequate simulation of tissue deformations would open a way for more rapid development of USE, which enables differential tissue diagnostic ^[28,87] including the use of the endogenous motion of tissue induced by cardiovascular activity, where experiments are limited because of technical and principal constraints ^[31].

1.5. Motion tracking algorithms

The motion tracking algorithms described in this section have been published in “Carotid Wall Longitudinal Motion in Ultrasound Imaging: An Expert Consensus Review”^[27].

“Since the initial evaluation of carotid wall longitudinal motion in humans *in vivo*^[22,88], an increasing number of motion tracking techniques have been designed to address this task^[61,89]. Several challenges inherent to either ultrasound imaging (*e.g.*, speckle noise and artifacts) or vessel physiologic behavior (*e.g.*, abrupt motion patterns) must be considered for reliable motion tracking. As a result, specialized and advanced methodologies were gradually developed to specifically extract longitudinal motion.”

1.5.1. Wall motion extraction based on B-mode images

B-mode is the most well-known representation of ultrasound imaging: this modality, characterized by a specific gray-scale speckle pattern, is used to represent structural information that can be interpreted visually on the scanner monitor. Three major motion-tracking approaches are used to extract the motion from B-mode ultrasound image sequences: block matching (BM), optical flow (OF) and feature matching (FM). These techniques, and the related studies focusing on longitudinal motion, are listed in Table A1.1 in Appendix A1 and discussed thereafter.

Block matching. BM is a conventional technique in the field of motion estimation and is widely used to perform speckle tracking in image sequences.

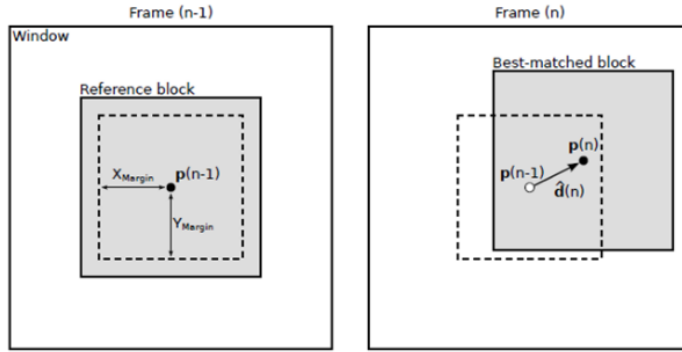


Figure 1.7. Block matching schematic diagram. The displacement $\hat{d}(n)$ corresponds to the motion from the reference block centered on the point $p(n-1)$ to the location of the best matched block centered on the point $p(n)$ between the $(n-1)$ st and the n th frames. The search window corresponds to the whole investigated neighborhood defined by the maximal displacement margins $[X_{Margin}, Y_{Margin}]$, delimited by the dashed square. Source: Zahnd *et al.*^[19]

The general underlying principle (see Figure 1.7) is to find, within the $(n + 1)$ st image, the most probable location of a target region, denoted as the reference pattern, from the n th image. Estimation is performed either by minimizing a difference metric with operators such as the sum of squared differences or by maximizing a similarity metric with operators such as the normalized cross-correlation. Among the most critical parameters are the size of the analyzed speckle pattern and the size of the maximal authorized displacement (*i.e.*, the “block” and the “search window,” respectively).

Strategies directly based on traditional BM have been successfully applied to assess longitudinal motion. In an early study^[88], the extracted motion waveforms were rather coarse, likely because of a large block size and no sub-pixel interpolation. However, thus obtained reproducible and well-defined patterns contributed to the feasibility of *in vivo* examinations. A BM method known as “echo tracking,” using a small block size (originally defined as a 0.7×0.7 -mm² region), enabled accurate tracking of salient speckles in carefully acquired images^[23]. Nevertheless, reduced block sizes are unlikely to provide robust results in general routine clinical scans, where image quality is often poor.

Adaptive BM approaches were introduced to tackle the issue of speckle decorrelation across time. Such approaches generally correspond to a mathematical model involving a control scheme, as well as an evolution scheme, capable of representing the expected temporal motion and compensating for tracking errors. The Kalman filter was exploited to model the temporal changes in the location of the target block^[90,91], as well as in its gray levels^[19,90,91] during the cardiac cycle.

A BM approach based on the consideration of two previous frames (as opposed to only one in the classic techniques) was proposed to increase the tracking robustness^[92]. Adding one extra reference block in a BM scheme was proposed to use different reference blocks^[92]: here, the actual pixel values of the previous frame were used, as opposed to Kalman-based methods, where the reference block was predicted. A more advanced method was later proposed, involving an affine block motion model, able to consider rotation and scaling of the tracked pattern, in addition to rigid translation^[61]. A scheme based on luminance optimization was also proposed to take into consideration the progressive variations of pixel values across time and to maximize the matching potential^[63].

A non-linear state-space approach based on an elasticity model of the carotid wall and including an H1 filter was further proposed and adapted to carotid wall motion estimation^[93,94,95]. The major benefit of these approaches is their ability to deal with noisier data and provide robust and accurate tracking results when a conventional BM approach would likely fail.

The combined use of multiple blocks was investigated in several studies. These approaches are based on the following principle: At a given time step, the motion is independently estimated with a series of adjacent or partly overlapping blocks, and the resulting motion is obtained *via* the averaging of all contributions. The rationale for multiblock matching is to increase the robustness by diminishing the influence of any single block that may fail. Such approaches include five^[25], six^[96] or sixteen^[97]

blocks. A method based on the consideration of multiple frames per estimation and a parabolic sub-sample interpolation in high-frame-rate cine loops (1300-1500 Hz) was further developed^[98]. Several advanced search strategies, initially introduced in RF imaging^[99,100], were successfully applied in B-mode imaging to improve computation time, such as a coarse-to-fine interpolation scheme^[25] and a sparse-to-dense tracking scheme^[92].

Going one step further, the extraction of a dense motion field was recently addressed^[101]. Here, the temporal motion across the full width of the image is estimated by placing a block in each column (typically, >350). A combinatorial analysis scheme based on dynamic programming is used to simultaneously extract the motion of each block (as opposed to one after the other), while enforcing motion rules and enabling fast computational times. Results from this study enabled assessment of the degree of motion homogeneity across the length of the vessel.

Optical flow. OF consists in determining the velocity field across different temporal frames^[102]. The fundamental difference between OF and BM is the adoption of the Eulerian paradigm (*i.e.*, motion is evaluated through a static window) instead of the Lagrangian scheme (*i.e.*, motion is evaluated by dynamically following a target). Complex motions involving rotations and deformations are usually better captured *via* OF-based approaches than BM^[103].

Applied in the context of carotid longitudinal motion, OF has been successfully used in several studies^[61,104,105], as listed in Table A1.1 in Appendix A1. It was reported that the general waveform shape of the wall motion was different when extracted by BM and OF, although their peaks occurred at the same time instants of the electrocardiogram signal^[106]. The maximum velocity and extracted motion in the radial and longitudinal direction were reported to be greater using BM^[106]. The estimated wall motion on the same B-mode images by OF and BM in the radial direction were reported to be more similar compared with those in the longitudinal direction^[106]. In the presence of either Gaussian or speckle noise, it has been reported that weighted least-squares OF outperforms BM, particularly in poor quality images that are typically observed in clinical populations^[61].

Feature matching. An original approach based on automatic extraction of several salient image regions was recently introduced^[107]. Detectors such as scale-invariant feature transform, speeded-up robust features and maximally stable extremal regions were used to identify target points. The main advantage of this approach is its robustness because only salient points are considered for tracking and are re-selected at each time step. Moreover, this method has potential to be fully automatic because regions are determined by the above-mentioned descriptors. Additionally, shear strain evaluation in different anatomic layers is also possible by using FM *via* the tracking of points located in different anatomic layers, offering a similar potential for depth-specific shear evaluation as provided by certain BM approaches^[108,109]. However, a generally encountered drawback of FM approaches is the constant re-selection of target points and the averaging of their respective motion vectors, making both precise single-point and full dense-field motion estimation impossible.

1.5.2. Wall motion extraction based on RF signals

Tracking methodologies based on RF signals were introduced in 1985 to estimate the radial motion via an autocorrelation approach^[110]. As opposed to B-mode imaging, RF-based motion tracking involves the computation of the phase shift (i.e., in the frequency domain) between two subsequent time steps to determine the corresponding spatial displacement. Of note, acquisition and export of RF signals usually necessitate research-oriented scanners, as this functionality is generally not available in clinical devices. An overview of the approaches developed toward carotid wall motion estimation is provided in Table A1.2 in Appendix A1 and detailed thereafter.

Concerning small interframe displacements, a BM based method has been developed in an iterative manner^[98]. Phase-based estimation on RF signals has been applied on phantom and *in vivo* carotid for simultaneous wall motion and flow estimation^[111,112,113,114]. Phase-sensitive methods have recently been applied for 2-D motion estimation using 2D frequency spectra of RF echo signals using the complex analytical signal obtained by modulating the ultrasonic field^[115], by the Hilbert transform^[116,117,118,119] or by the wavelet transform^[120,121]. The Hilbert transform was repeatedly used to generate a complex analytical signal from RF data using correlation-based estimators^[116]. In line with a similar approach, phase correlation and subsample interpolation were successfully applied^[122]. Fourier-based methods^[123,124,125] were also introduced. A paired 1D and 2D motion estimation technique with shifted cross-spectra developed to assess the phase shift was put forward, and exhibited increased accuracy with a smaller spatial window than conventional 2D motion estimators^[116]. One advantage of Fourier-based approaches is their intrinsic ability to achieve sub-pixel accuracy without the need for spatial interpolation, which can result in greater accuracy compared with speckle tracking in B-mode^[126,127]. It was reported that the 2D phase-sensitive method^[127] outperformed the BM method in terms of accuracy (bias errors and standard deviations) in motion estimation at a high frame rate that was realized by parallel beamforming^[126]. This is especially important along the longitudinal direction of the artery because the image across this axis is generally coarser than the radial counterpart.

An approach relying on synthetic aperture imaging was specifically designed as an unconventional beamforming strategy to generate a pressure field with a controlled carrier frequency in the transverse direction^[115]. This real-time technique, referred to as “US tagging” (in reference to the principle of magnetic resonance imaging tagging), consists of the transmission of an unfocused wave, subsequently received with a dynamic quadratic focusing combined with dynamic apodization^[119,128]. Building upon the potential offered by such marked signals, a local phase-based OF method was devised for subpixel estimation^[129], and was applied *in vivo* in the context of longitudinal motion on so-called RF-2-D images^[20]. A similar approach leveraging high-frame-rate imaging (10 kHz) was also introduced^[117], bridging the gap between the association of longitudinal motion and PWV. For 2-D velocity vector estimation of tissue motion, plane wave imaging has been used along with transverse oscillation and an efficient frequency domain estimator^[117]. It is noteworthy that unitary

displacements greater than half of the signal wavelength (be it determined by the carrier frequency along the radial direction or by the synthetic aperture along the longitudinal direction) cannot be ascertained *via* phase-tracking methods because they fall under the effect of aliasing ^[116,129], therefore justifying the demand for a sufficiently high frame rate.

Inspired by the field of computer vision, an approach known as “motion video amplification” was proposed to magnify the tiny and subtle deformation of the vessel wall in B-mode ultrasound carotid image sequences ^[130]. While large-scale deformations are not amplified, low-amplitude deformations within the vessel wall (such as longitudinal motion, radial motion, deformation caused by the passage of the pulse wave) are substantially magnified up to a factor of 1000, and can be easily perceived by a clinician with the naked eye. This technique opens up new possibilities for the evaluation of complex motion patterns, such as the small phase W and phase X displacements described under Characterization Based on Directional Wall Displacements. Of note, this technique requires the acquisition of high-frame-rate sequences (>2500 Hz), which is available on only a limited number of research-oriented ultrasound systems.

1.5.3. Available tools

The velocity vector imaging (VVI) software platform (VVI, Research Arena 2; TomTec Imaging Systems GmbH, Unterschleissheim, Germany) is a commercially available tool that was used to investigate the association of longitudinal motion with cardiovascular risk in human and mouse ^[18,24,131]. This technique, initially designed to measure heart dynamics, involves the positioning of a multisegment horseshoe-shaped skeleton in the image, using a total of 20 control points. Applied to the carotid artery, one segment (approximately 5 mm long) can be positioned on a region of interest in the intima-media complex. Of note, the VVI displays the measured temporal trajectory, together with the corresponding motion amplitude, but does not support any export of the time series for finer analysis. Despite relevant clinical findings ^[18,24,131], a thorough evaluation of the tracking performance ^[19] revealed poor accuracy and reproducibility, while being tedious and time consuming because of substantially large amount of manual operations required to run VVI.

The MyLab desktop analysis software (Esaote, Firenze, Italy) is a commercially available tool that was used to extract longitudinal shear values ^[132]. However, although this technique was specifically designed for ultrasound carotid data, quantitative reports of the tracking performance *per se* are not publicly available to the best of the authors’ knowledge.

The CAROLAB software platform ^[133] is a freely available (available at: <https://www.creatis.insa-lyon.fr/carolab/>) tool that has been put forward to analyze ultrasound image sequences of the carotid artery. The motivation behind CAROLAB is to encapsulate several previously published and thoroughly validated methodologies for wall segmentation ^[134] and motion estimation ^[19,101] within an efficient graphical user interface.

A web-based platform named CAROTID has been developed that integrates motion-based computer-aided diagnosis functionalities for patients with carotid atherosclerosis^[135].

1.6. Conclusions of the 1st chapter

1. Atherosclerosis is a chronic disease of the arterial wall that is not noticeable until the atherosclerotic plaques build up. However, it has been proven that significant changes in the mechanical properties of arterial walls occur much earlier than anatomical changes appear. Longitudinal motion of the arterial wall - a parameter reflecting the mechanical properties of the arterial wall, described as a bidirectional motion of the *intima-media* complex parallel to the blood flow during the cardiac cycle. Although the longitudinal movement of the carotid artery wall is associated with cardiovascular health, the determinants of longitudinal motion remain unknown.
2. The motion of the carotid artery wall has been modeled by many authors. Nonetheless, to model a dynamic 3D artery model many parameters must be incorporated, *i.e.* scatterers amplitude, number of scatterers per resolution cell, radial and longitudinal motions amplitude and waveform, motions slope deep into the tissue, *etc.* However, most of the previous studies do not take into account all the abovementioned parameters. Therefore, a new artery model, capable of reproducing a realistic dynamic 3D artery model surrounded by viscoelastic tissue is necessary.
3. Since digital simulation is increasingly important for US imaging and elastography developments a quantitative assessment of uncertainties involved by all interrelated components of the simulation process as well as revealing of the possible factors causing those uncertainties remains a problem. Besides, quantitative comparison of simulation with an experiment including analysis of resolution in axial, lateral, and elevation direction remains limited.
4. A number of motion tracking algorithms are proposed for radial and longitudinal motion detection. Some of them are freely or commercially available for the investigation of longitudinal motion. But none of them are applied in clinical practice these days. Firstly these methods should be carefully investigated before wide usage.

2. DEVELOPED APPROACHES FOR SIMULATING ARTERY AND SURROUNDING TISSUE PULSATION AND ACCURACY EVALUATION OF MOTION DETECTION

This section is organized as follows: Subsection “*Carotid artery ultrasound examination*” presents the ultrasonic scanner used in *in vivo* examination, scanning preset, CCA examination methodology, study population, and estimated radial and longitudinal motion signals used in motion modeling. After this, the subsection “*Modeling and verification of a digital simulation of physical US scanning*” outlines a digital scanning simulation and modeling of digital resolution phantoms adequate to physical scanning and phantoms. When digital scanning is presented and *in vivo* radial and longitudinal motion signals are estimated, a digital model of the artery and real *in vivo* signals used in it are proposed for simulation of sequential US data. Finally, subsection “*RF ultrasound signals post-processing algorithms*” are devoted to both motion tracking algorithms and their testing with model data, and *in vivo* signal processing and parameterization to compare two groups: healthy volunteers and at-risk patients.

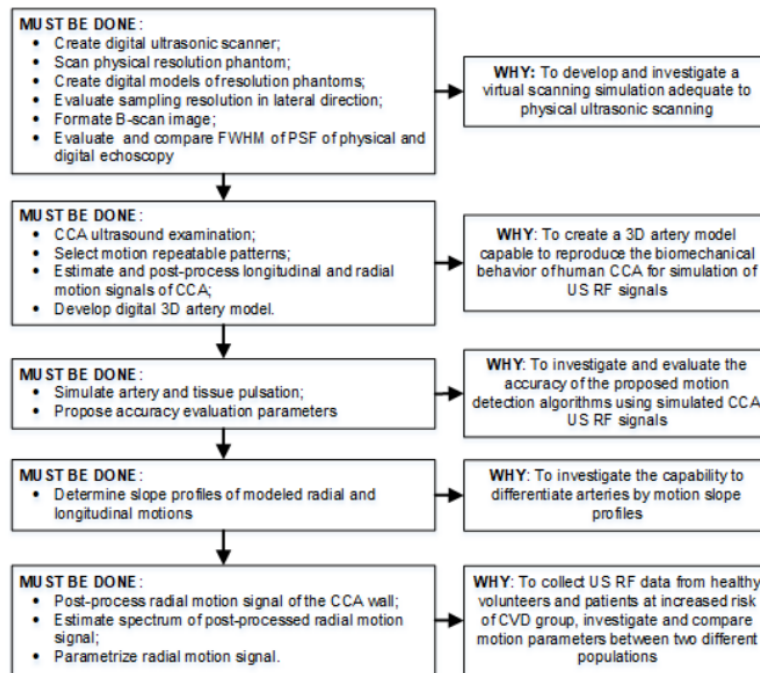


Figure 2.1. Schematic diagram illustrating the workflow structure

To highlight the purpose of the performed experiments, the schematic diagram illustrating the workflow structure is given (see Figure 2.1) representing what was done and why.

2.1. Carotid artery ultrasound examination

2.1.1. Physical ultrasonic scanner

Research dedicated ultrasonic scanner Ultrasonix SonixTouch (Analogic Ultrasound, Canada), equipped with a linear array probe (L14-5/38) was used for data collection during the *in-vivo* examination of CCA. US scanner is capable to open access to RF signals and the ability to control scanning algorithms. The main parameters of US scanning and RF signals digitization were as follows: frequency of US waves 13.3 MHz, transmit focal single depth – 1.5 cm, scanning depth – 2.5 cm, frame rate – 52 Hz, number of frames – 629, number of post-beamformed scanning lines – 640, scanning sector – 50 %, sampling frequency 40 MHz, ADC resolution 16 bits. The data, US RF signals, and B-mode image sequences were stored in a cine-loop as consecutive frames for later offline analysis in MATLAB R2018b (The MathWorks, Inc., Natick, USA).

In the axial direction, the RF signal sampling resolution is 19.25 μm (when the speed of sound waves is 1540 m/s), while in the lateral direction, the sampling resolution is dependent on the preselected line density. The sampling resolution in lateral direction was evaluated throughout the experiment where a special phantom made^[136] using a fishing line was used. Later, evaluated sampling resolution in lateral direction was used in digital ultrasonic scanner simulation B-scan formation (see 2.2.1 section).

A picture of the phantom is given in Figure 2.2 a. The monofilament fishing line of small diameter was wound on the screw thread at equal distances ($L = 1.25 \text{ mm}$) and serves as point target reflectors (see Figure 2.2. b). Since the diameter of the fishing line is $d = 0.1 \text{ mm}$ only, it can be considered as a point target reflector, and the recorded image of the reflector is a PSF which can be used to evaluate the spatial resolution of an ultrasonic scanning system.

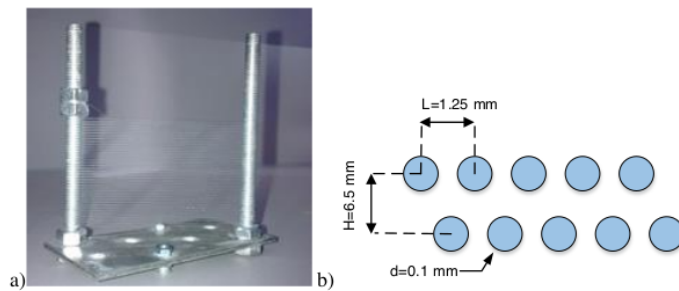


Figure 2.2. Special phantom made using a fishing line (a), cross-section structure of the phantom (b)

The phantom was placed in the container of distilled water and scanned maintaining the main parameters of the US scanning, only scanning depth was changed from 2.5 cm to 3.5 cm. By scanning the stretched threads with a linear array probe (L14-5/38) whose scanning plane is perpendicular to threads, a cross-sectional view of the threads was got. The acquired B-scan image of the point targets is presented in Figure 2.3 a, while the single line of the phantom image crossing point targets laterally is provided in Figure 2.3 b.

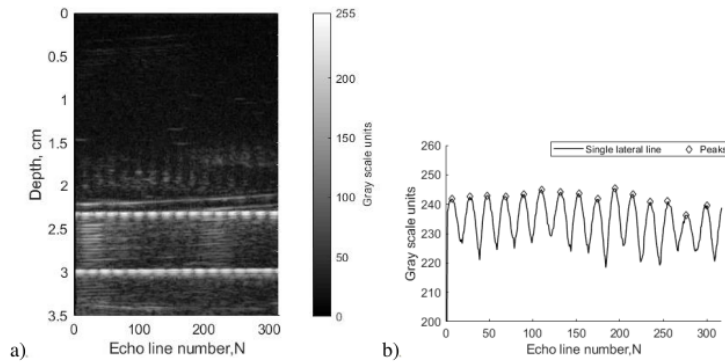


Figure 2.3. Evaluation of sampling resolution in lateral direction using the special phantom made using a fishing line: the B-scan image of the point targets (a) and single lateral line of the B-scan image with a seen point targets and preselected peaks whose position was used for evaluation of sampling resolution in the lateral direction (b)

Using a single line of the B-scan image and preselected peaks, distances between adjacent point targets (peaks) were detected, i.e. 20.36 ± 0.48 post-beamformed scanning lines. Sampling resolution in the lateral direction was calculated by dividing the distance between point targets ($L=1.25$ mm) of a detected number of post-beamformed scanning lines between two adjacent point targets, i.e. 20. It was found that the sampling resolution in the lateral direction is 0.0625 mm.

2.1.2. CCA ultrasound examination methodology

Thirty young healthy volunteers (21 females, 9 males) and twenty-eight older at-risk patients (10 females, 18 males) were involved in this study (see Table 2.1). As assessed by a written questionnaire healthy subjects had no cardiovascular risk factors, while older subjects had a high risk of cardiovascular disease and participate in the preventive program of CVD ^[137].

Clinical data were collected at the Lithuanian University of Health Sciences Hospital, Department of Cardiology, during May–October 2018. The study was approved by the Kaunas Region Biomedical Research Ethics Committee (2018-08-02, No. BE-2-51, Kaunas, Lithuania). Every participant provided written

consent to participate in the study and allowed the usage of the obtained US RF signal and B-mode image sequences under the principle of confidentiality.

Table 2.1. Characteristics of the subjects

	Young volunteers (n=30)	At-risk patients (n=28)
Age (year)	28.03 ± 9.01	50.00 ± 6.24
Height (cm)	174.60 ± 6.11	172.68 ± 9.60
Weight (kg)	73.43 ± 11.76	92.54 ± 16.03
Body mass index (kg/m ²)	24.02 ± 3.35	30.91 ± 3.69

Two cardiology physicians performed the acquisition of US RF signal and B-mode image sequences of radial and longitudinal motions of CCA. Before the examination, all volunteers were asked to rest in the supine position for at least 15 min. During the US data registration, the volunteers were lying in the supine position, stretching their neck and turning it 45 degrees to the right or left, depending on the examined neck side. Both right and left CCA were scanned since artery motion amplitude does not depend on the echoscopic neck side ^[18]. Measurements of the longitudinal and radial motions of the CCA were performed 2–3 cm proximate to the bifurcation during at least two full heart cycles. To avoid motion artifacts, an ultrasonic transducer was mounted in a stationary holder that was attached to the couch. Sequences of US RF signals and B-mode images were recorded by volunteers holding their breath for about 10–15 seconds ^[16,19,21,25].

All analyses were performed using a Clinical scanner Ultrasonix SonixTouch (see Physical ultrasonic scanner). During the examination, no pressure was applied to the transducer, i.e. it is not pressed against the neck to not deform the artery. Ultrasound examination of the artery was started at the root of the neck by moving the transducer toward the head cranially along the course of the artery. Initially, an ultrasound transducer was held across the CCA to monitor the transverse image of the artery (see Figure 2.4).

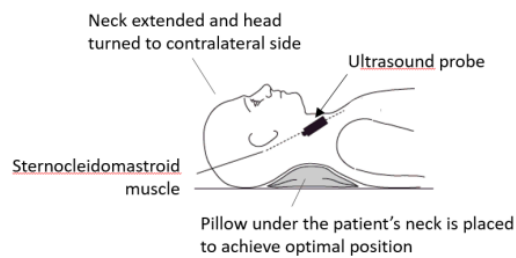


Figure 2.4. An ultrasound probe in the transverse position (adopted from ^[138])

The sternocleidomastoid muscle can be used as a reference point. Following these instructions, the location of the splitting of the CCA into the internal and the

external arteries was found, or signs of vascular disease were observed (e.g. thickening of the artery wall). This results in a transverse section of the artery (see Figure 2.5) ^[138].

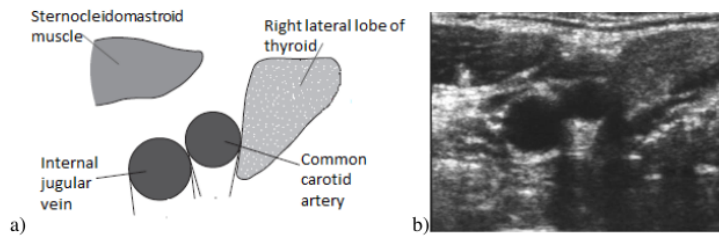


Figure 2.5. Transverse section of the CCA: a) structured and b) real. The right side of the neck was scanned (adapted from ^[138])

By capturing the location of the CCA, the ultrasound transducer was rotated 90 degrees clockwise to image a longitudinal view of the artery. The internal and external carotid arteries are in different planes. Therefore, when a bifurcation of the CCA was found, the lower part of the probe was kept over the CCA and the upper part was rotated through small angles to image the internal and the external carotid arteries separately ^[138]. A representative ultrasound image identifying the carotid artery in a longitudinal direction is given in Figure 2.6.

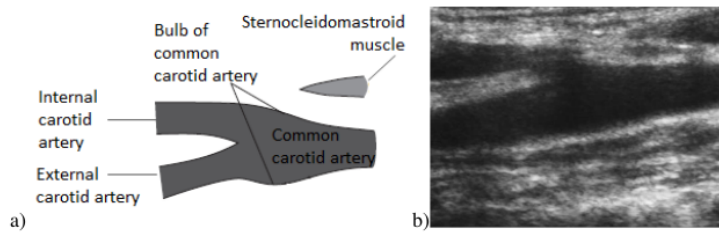


Figure 2.6. Longitudinal section of the CCA: a) structured and b) real. The scanned right side of the neck (adapted from ^[138])

To ensure that the CCA US RF signals and B-mode image sequences were of acceptable quality, both the longitudinal movement had to be clearly visible along the preselected segment of the arterial wall and CCA walls have to appear as double-line patterns ^[21]. When an acceptable view of CCA was seen on the ultrasound scanner screen, the cardiology physician unhanded the transducer, and the subject was asked to hold their breath for about 10–15 seconds until data sequences were recorded. Finally, all sequences were stored digitally and transferred to a computer for further analysis with MATLAB R2018b (The MathWorks, Inc., Natick, USA).

2.1.3. Selection of motion repeatable pattern

Sonography of tissue motion in-vivo is challenging. Quality thresholding of *in-vivo* ultrasound data is the first step in the analysis. Au et al ^[139] proposed to average the four consequent heart cycles for representative measurement of motion in CCA. The author noticed that indices of variability were reduced when two to four heart cycles were averaged. When more than four heart cycles were averaged, any improvements in indices of variability were not observed. This indicates that there is no need to record more than four heart cycles. According to these recommendations, subjects presenting low-quality data sequences (motion artifacts due to patient motion, unclear *intima-media* complex in B-mode ultrasound image sequences, etc.) or having less than four full heart cycles were rejected from the study.

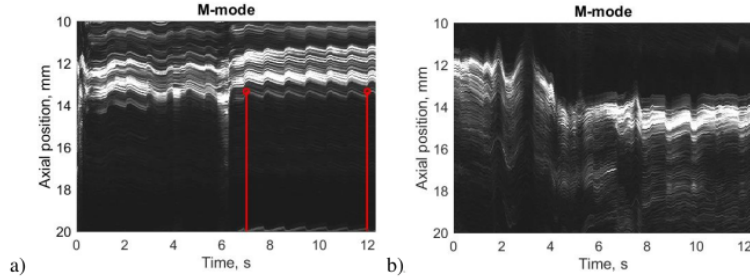


Figure 2.7. High-quality data (a) vs low-quality data (b) of CCA. Red stems in (a) indicate the time interval which was used for further analysis

Data quality assessment was performed based on visual inspection of one ultrasonic scan line (A-mode) in the M-mode of each subject. The echoscopic line covered both the proximal and distal walls of the CCA.

The ultrasound line displayed in M-mode clearly showed which time interval is corrupted by motion artifacts, which interval is qualitative, and how many full repetitive cardiac cycles there are in the latter interval. After visual inspection, eight healthy volunteers and four at-risk patients were excluded from the study, and qualitative time intervals of each subject were manually preselected for further analysis.

2.1.4. Estimation and post-processing of longitudinal and radial motion signals of CCA

The methodology described in this section has been published in “Ultrasonic Parametrization of Arterial Wall Movements in Low and High-Risk CVD Subjects”^[140].

For this study, CAROLAB software was used to estimate longitudinal and radial motions of CCA ^[133,134]. This software is used for the analysis of ultrasound B-mode image sequences and assesses both longitudinal and radial motions with a speckle-tracking approach that is based on the BM method ^[19]. The main point of

the BM framework is to detect the motion $d(n)$ between two consequent frames by comparing pixel blocks of consecutive images $I(n-1)$ and $I(n)$. The motion corresponds to the displacement between the center point $p(n-1)$ of the reference block and the center point $p(n)$ of the best-matched block. This results in the shift of the center point $p(n)$ between images $I(n-1)$ and $I(n)$. Pixel blocks alignment in images $I(n-1)$ and $I(n)$ takes place only within the search window, i.e., in the defined maximum margin around the center point of the reference and best-match blocks. After summing up all the displacements $d(n)$ received, the $p(n)$ point motion trajectory is estimated. To cope with the issue of speckle decorrelation, a pixel-wise Kalman filter is used to update the reference block^[19].

A region of interest (ROI) containing a well-contrasted speckle pattern of the distal vessel wall for longitudinal and radial motion evaluation was chosen in the first B-mode sequence frame of a qualitative time interval. A kernel of the ROI was selected manually, with a size 3×0.5 mm. Estimated signals of longitudinal and radial motion, were saved for further post-processing in MATLAB R2018b (The MathWorks, Inc., Natick, USA).

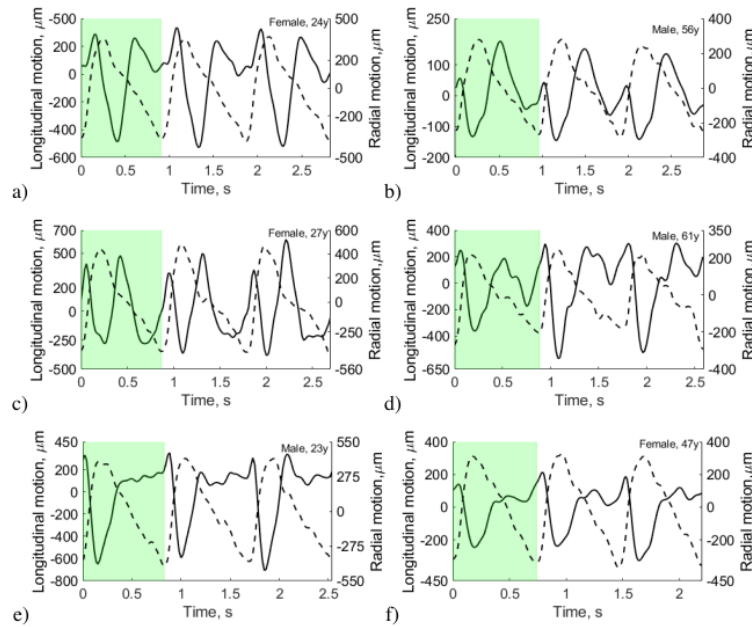


Figure 2.8. *In vivo* radial (dashed line) and longitudinal (solid line) motions of CCA of different ages, illustrating different patterns of longitudinal motions: a), c), e) young volunteers and b), d), f) at-risk patients. Preselected periods (green shadowed area) were used to model artery and tissue pulsation

Motion signals were then filtered with a band-pass IIR filter ($f_{\text{pass-lower}} = 0.5$ Hz and $f_{\text{pass-higher}} = 8$ Hz, filter order 2nd) and then detrended, subtracting the mean or a best-fit line (in the least-squares sense) from the resulting signal. After this, three consequent heart cycles were selected manually in time. Only one heart cycle (see the green shadowed area in Figure 2.8 for an example) was used in motion modeling, especially since other periods are quasi-periodic with the cardiac cycle.

2.2. Modeling and verification of a digital simulation of physical US scanning

Quantitative evaluation and comparison of digital US scanning with physical US scanning is needed for adequate digital US echoscopy simulation. FWHM of PSF was used as the main parameter for the determination of the image resolution and discrepancy evaluation between physical and digital US scanning.

In ultrasonography, the spatial resolution of an ultrasound beam can be divided into three dimensions: 1. axial resolution (along the axis of the ultrasound beam, Z-axis), 2. lateral resolution (perpendicular to the axis of the ultrasound beam, X-axis), and 3. elevation resolution (width of ultrasound beam, Y-axis) ^[141]. According to these three dimensions of spatial resolution, the adequacy was assessed by comparing the digital simulation of the US scanning with physical US scanning.

2.2.1. Digital ultrasonic scanner and B-scan formation

A digital ultrasonic scanner based on a physical ultrasonic scanner (see Section 2.1.1) was simulated using the Field II package for MATLAB ^[36,142]. To reach adequacy between experiments and simulation results, the parameters of a physical scanner Ultrasonix SonixTouch and linear array probe L14-5/38 were identified and incorporated into the Field II program. The height and width of the array elements, kerf, pitch, number of elements, and elevation lens focus were found in the Transducer Specification Sheet ^[143] of the linear array probe. Speed of sound, transmit focal depth, element excitation, etc. was identified from the physical ultrasonic scanner.

To increase the accuracy of the simulation, *e.g.* elevation lens focus, apodization in the YZ plane, the physical elements must be divided into the sub_x by sub_y mathematical elements. This could be done by changing the number of physical element sub-division in x and y directions and investigating the influence on the pressure field of the simulated transducer.

Evaluation of the number of physical element sub-division in x and y directions was started by calculating the pressure field when sub_x and sub_y were 1 and 1 accordingly. As can be seen from Figure 2.9., element sub-division in the y -direction is not sufficient, side lobes are observed in the pressure field in YZ plane.

To identify the sufficient number of element sub-division in the y -direction, when side lobes amplitude would be 30 dB lower compared to the main lobe amplitude, the main lobe and side lobe patterns at 15 mm axial distance from pressure field in YZ plane were investigated. For a visual representation of the dependence of side lobes amplitude to the number of sub-divisions in the y -direction, Figure 2.10. is given. From this figure, it can be seen that when the number of element sub-division

in the y-direction is from 1 to 8, side lobes amplitude is from -17.48 dB to -28.86 dB correspondingly. When the number of element sub-division in the y-direction is 9 or more, side lobes amplitude is lower than -30 dB. It is worth noting that the simulation time of a single ultrasound RF frame in the Field II program is dependent on the volume of the model, the number of scatterers, or in this instance, the number of element sub-division.

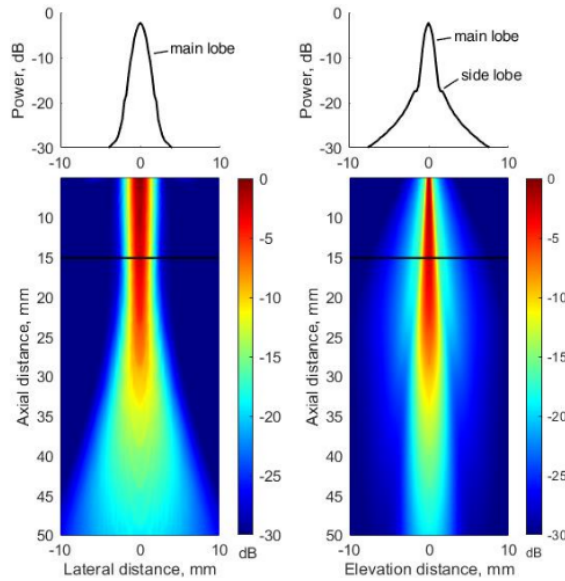


Figure 2.9. Simulation of linear array transducer pressure field in XZ plane (*left*) and YZ plane (*right*). Black lines at a 15 mm axial distance depict the position from where the main lobe and side lobe patterns are taken and represented above the corresponding pressure field. Sub-divisions in the x-direction and y-direction were the same and equal to 1

In concordance with this statement, it was decided to use the lowest number of element sub-division in the y-direction, i.e. 9, and in this way optimize both apodization in y-direction and simulation time of single or sequence of ultrasound RF frames.

A similar analysis as presented above was done. In this case, the main lobe and side lobe patterns at a 15 mm axial distance from the pressure field were investigated in the XZ plane. Figure 2.11 indicates that the number of element sub-divisions in the x-direction does not influence the sides lobes amplitude, and in all cases, it is lower than -30 dB.

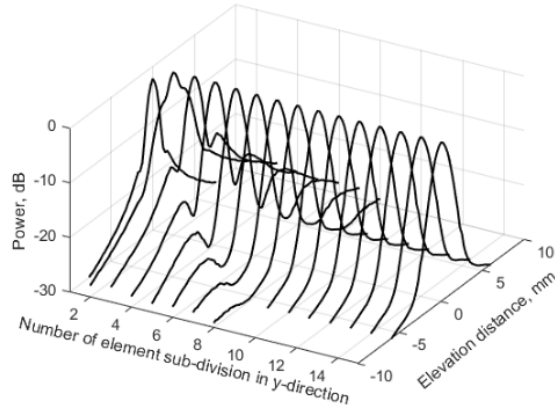


Figure 2.10. Representation of the main lobe and side lobe patterns at 15 mm axial distance from pressure field in YZ plane when a different number of sub-divisions in the y-direction of the element was used in the simulation

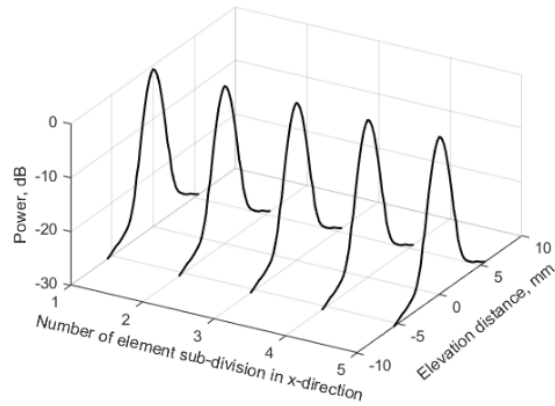


Figure 2.11. Representation of the main lobe and side lobe patterns at 15 mm axial distance from pressure field in XZ plane when a different number of element sub-divisions in the x-direction was used in the simulation

Summing up the given result above, it was decided to divide physical elements into the $sub_x = 1$ by $sub_y = 9$ mathematical elements. Simulation result of linear array transducer pressure field in XZ and YZ planes with corresponding physical element sub-division is presented in Figure 2.12. The illustration confirms the fact that the

determined number of physical element sub-division in the x and y direction is sufficient to model appropriate apodization in both XZ and YZ planes and suppress side lobe amplitude lower than -30 dB.

Finally, parameters that were used to simulate scanning with linear array transducer, are listed in Table 2.2.

Table 2.2. Parameters of virtual scanning with Field II

Parameter	Value
Array type	Linear array
Transducer center frequency	5 MHz
Number of physical elements	128
Element excitation	Hanning-modulated sinusoid of two cycles
Height of element	4 mm
Width of element	0.279 mm
Kerf	0.025 mm
Pitch	0.304 mm
Element sub-division in x-direction	1
Element sub-division in y-direction	9
Elevation lens focus	16 mm
Transmit focal distance	15.5 mm
F-number in transmit	3
F-number in receive	1.7
Apodization	Hanning
Sampling frequency	40 MHz
Speed of sound	1540 m/s
Assumed frequency-dependent attenuation	0.5 dB/cm/MHz@ 3.5MHz

The simulated B-scan image consists of 317 echo lines, the distance between two adjacent echo lines was 0.0625 mm and the image width was 19.8 mm.

To have the same formation of the B-scan image in both physical and digital scanning, it was chosen to load registered (i.e. physical scanning) and modeled (i.e. digital scanning) US RF signals into MATLAB R2018b (The MathWorks, Inc., Natick, USA). Then B-scan formation consists of the following steps: 1. RF signals envelope detection; 2. log-compression from 0 to -70 dB.

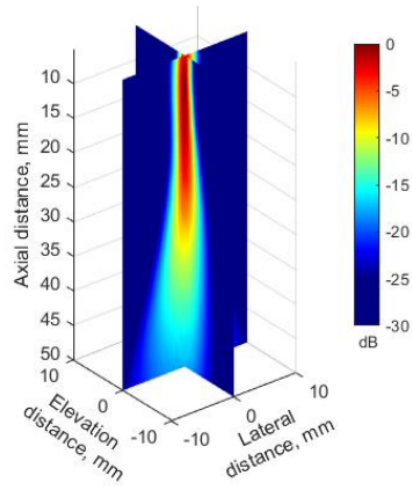


Figure 2.12. Simulation of linear array transducer pressure field in XZ and YZ planes. Element sub-divisions in the x-direction and y-direction were 1 and 9 accordingly

2.2.1. Physical resolution phantoms

For the echoscopy experiments, two ATS Laboratories Inc. physical phantoms were used: Model 549 General & Small Parts phantom (physical wire phantom) ^[144] and Model 538NH Beam Profile & Slice Thickness phantom (physical slice thickness phantom) ^[145]. Figure 2.13 shows which areas of the physical phantoms were used for the evaluation of axial, lateral, and elevation resolutions.

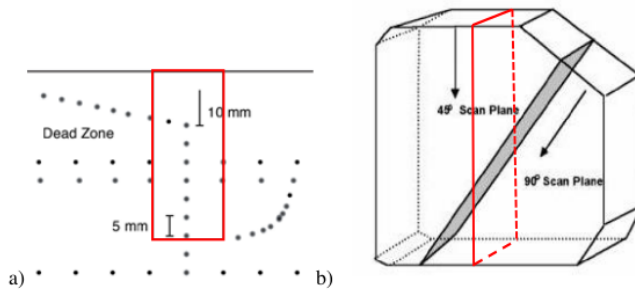


Figure 2.13. Structure of ATS Laboratories Inc. Phantoms: a) Model 549 (physical wire phantom) and b) Model 538NH (physical slice thickness phantom) with preselected scanning areas shown (adapted from ^[144,145])

Physical wire phantom was used for assessment of axial and lateral resolutions, while physical slice thickness phantom was used for assessment of elevation resolution. B-scan slice thickness or beamwidth in the elevation plane was evaluated according to the method pioneered by Goldstein and Madrazo^[146] and updated later^[147].

According to the technical passport of the phantom, as a point targets in the physical wire phantom are monofilament Nylon wires with a diameter of 0.05 mm. The spacing between wires is 10 mm. In the physical elevation plane phantom, there is no information about plane characteristics, i.e. material, thickness.

During the echoscopy of physical phantoms, physical ultrasonic scanner parameters were set the same as in Section 2.1.1, except scanning depth which was set to 4 cm.

2.2.2. Digital models of resolution phantoms

Digital models of resolution phantoms described in this section have been published in “Main Uncertainties in the RF Ultrasound Scanning Simulation of the Standard Ultrasound Phantoms”^[34].

To create a digital model of resolution phantom, a 3D scattering map should be created, which is defined by the scatterer's positions, scattering strength, and a number of scatters. A 3D scattering map of digital models of resolution phantoms was generated according to the structure of physical wire and elevation plane phantoms (see Section 2.2.1).

A 3D scattering map defines the medium, which will be scanned with modeled linear array transducer. Firstly, the number of scatterers within the volume of the digital model is defined according to a corresponding resolution cell of the physical ultrasonic transducer^[41] and the volume of the digital model. The resolution cell is the minimum volume that can be extracted by the imaging system^[60]. To model the fully developed speckle pattern of simulated ultrasound B-scan image, the number of scatterers in the resolution cell was equal to 10^[41,148,149]. A resolution cell is calculated by^[148]:

$$resolution\ cell = \lambda \cdot N \cdot FWHM_{lat} \cdot FWHM_{azi}; \quad (1)$$

where λ is the wavelength, N is the number of cycles in the pulse, $FWHM_{lat}$ and $FWHM_{azi}$ are FWHM laterally and azimuthally respectively of the physical transducer PSF at the focus point.

The number of scatterers within the volume of the digital model was calculated by^[148]:

$$number\ of\ scatterers = 10 \cdot \frac{volume\ of\ model}{resolution\ cell}. \quad (2)$$

Secondly, a predefined number of scatterers were randomly distributed within the volume of the model. The scattering strength of the scatterers followed a Gaussian distribution. The variance of the distribution for wire and plane modeling is determined by the backscattering cross-section of the particular object, i.e., from the real B-scan image of the physical phantom (see Figure 2.14). The amplitude of the

B-scan image is used to scale the variance ^[150]. The amplitude of the B-scan image, which is normalized from 0 to 255 and represents the brightness of each pixel, was used to scale the variance. In summary, the variance value used for wire modeling was 177.6, while for plane modeling it was 132.

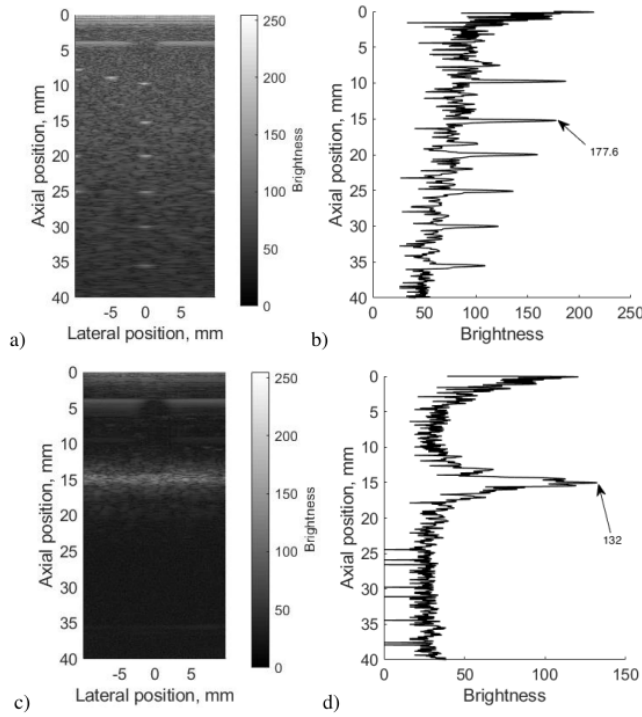


Figure 2.14. Determination of scatterers scattering strength in the digital phantoms: a) B-scan image of physical wire phantom, b) central echo line of B-scan image of physical wire phantom used for assignment of variance value for digital wire phantom, c) B-scan image of physical elevation plane phantom, and d) central echo line of B-scan image of physical elevation plane phantom used for assignment of variance value for digital elevation plane phantom

Digital wire phantom. Since physical phantom used for resolution and PSF estimation contains monofilament wires with a 0.05 mm diameter [31]. But PSF is correctly defined as a result of US wave reflection from the point scatterer, not from a wire. Therefore the digital phantom containing point scatterers located at the same positions was designed (see Figure 2.15 a). The positions of seven scatterers were set from 10 mm every 5 mm to 40 mm away from the transducer in the axial direction. The variance value used for point scatterer modeling was 177.6.

Digital slice thickness phantom. Digital slice thickness phantom (see Figure 2.15 b) for simulation of resolution parameters in the elevation plane (transverse to the plane of scanning) was designed following physical phantom Model 538NH (see Figure 2.13 b). The model has a 45-degree inclined reflecting plane simulated as a slice of scatterers. Because there was no information about plane characteristics i.e., thickness, of physical slice thickness phantom, it was decided that the thickness of the slice would be the same as monofilament wires diameter in physical wire phantom i.e., 0.05 mm. The variance value used for elevation plane modeling was 132.

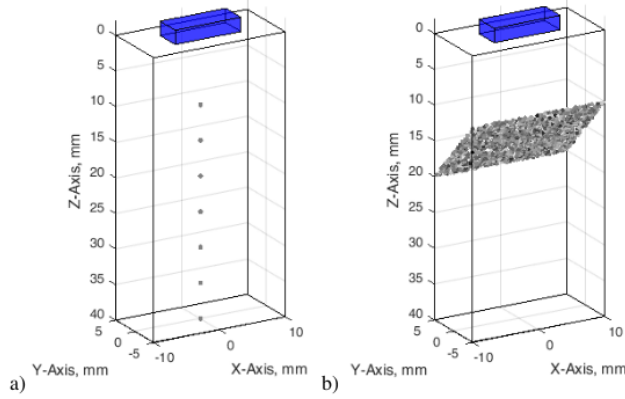


Figure 2.15. Configuration of digital phantoms: a) wire, b) slice thickness. The cuboids on the top of digital phantoms have marked the position of the digital ultrasound transducer

Since phantoms like real tissues have frequency-dependent attenuation, this feature was also considered in the simulation. Initial attenuation parameters were taken from the phantom's documentation.

2.3. Digital artery model

The materials and methods section is organized into four sub-sections and each of them stands for the corresponding four stages of the proposed algorithm as shown in Figure 2.16. The purpose of this algorithm flow is to show the input and output parameters and highlight the ability of the simulation algorithm to modify the input parameter in order to adapt it to a specific simulation task.

At Stage 1, the artery is modeled by the static scatterer's distribution accordingly to the vessel geometry and position. Subsequently, a static artery model is modified to the dynamic one by giving the radial and longitudinal motions to 3D distributed scatterers of the artery (Stage 2). Moving scatterers were used to simulate the sequence of scanning US RF signals for one cardiac cycle (Stage 3). At Stage 4, US RF signals for consecutive cardiac cycles could be composed, noise and artifacts could be added thus approaching a more realistic model for the application of chosen signal processing algorithms. Finally, processing of simulated US RF signals, motion

estimation, comparison of motion detection results with artery and surrounding tissue pulsation data set in Stage 2 as a reference, relative errors of motion detection were estimated.

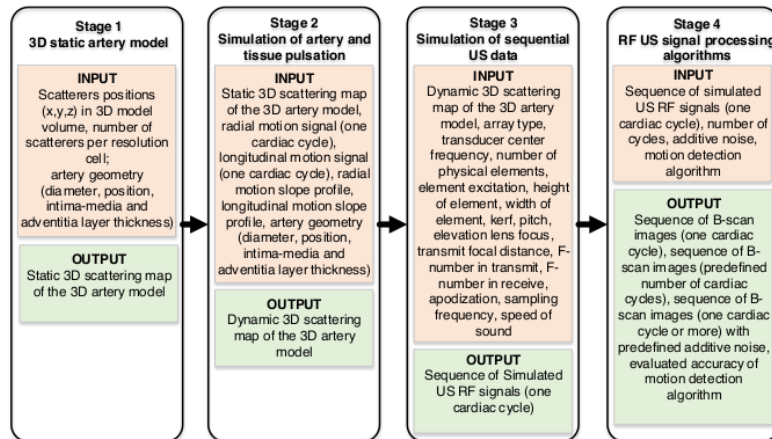


Figure 2.16. Overall simulation algorithm flow

2.3.1.3D artery model

The artery was modeled by a 3D map of scatterers, which is defined by scatterer number, positions, and scattering strength. A scattering map of the 3D artery model was generated according to the histological structure of the CCA^[17]. The geometry and structure of the artery model are shown in Figure 2.17. The structure consists of three layers (see Section 1.1).

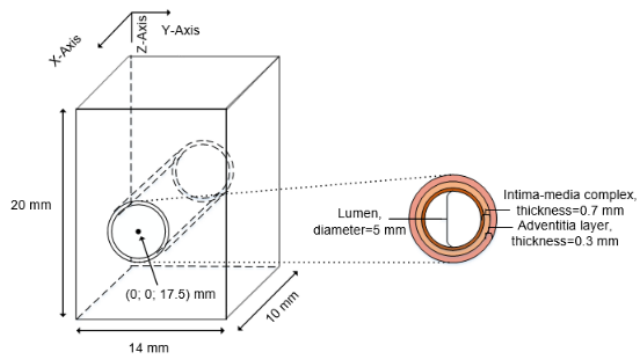


Figure 2.17. The general geometry of the artery model

The artery was modeled as three concentric pipes, which correspond to three layers of the artery wall, i.e., *tunica intima*, *tunica media*, and *tunica adventitia* keeping geometric dimensions of layers close to the dimensions of the *in vivo* CCA. For illustrative example dimensions were chosen as follows: the lumen diameter was $D_0 = 5$ mm; the thickness of the *intima-media* complex was 0.7 mm; the thickness of the *adventitia* layer was 0.3 mm; the artery center is 17.5 mm deep from the surface (see Figure 2.17).

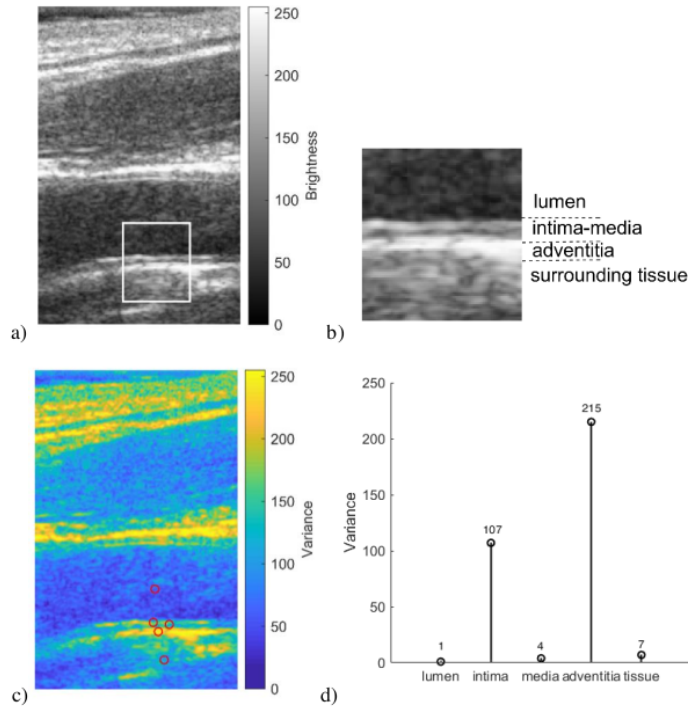


Figure 2.18. Determination of scatterers scattering strength in the artery model: a) B-scan image of CCA, b) detailed region (white rectangle in the B-scan image of CCA) of the distal wall with the lumen, the intima-media complex, the adventitia, and surrounding tissues, c) variance map of CCA with preselected points from where variance values are selected to use in the artery model and d) variance values assigned for a particular tissue of artery model

The first step in simulation is to define the medium, in which scattering structures will be embedded and finally digitally scanned with modeled linear array transducer. Scatterers were randomly distributed within the volume of the artery model. The number of scatterers within the volume of the artery model is defined

according to a corresponding resolution cell of the modeled linear array transducer^[148]. A fully developed speckle pattern of simulated ultrasound B-scan image would be achieved if there were 10 scatterers per resolution cell^[41]. Therefore, this constant was used in the calculation of the scatterer's number in the artery model. The scattering strength of the scatterers followed a Gaussian distribution with a mean set to zero and the variance set according to the backscattering cross-section of the particular tissue^[150], i.e., from the real *in vivo* B-scan image of CCA (see Figure 2.18). The amplitude of the B-scan image, which is normalized from 0 to 255 and represents the brightness of each pixel, is used to scale the variance.

Scattering strength was attributed for each scatterer according to its coordinates, i.e., if the scatterer belongs to the *intima* layer, its scattering strength was determined by variance of the *intima* layer, etc. Finally, a 3D scattering map of the 3D artery model was generated (see Figure 2.19).

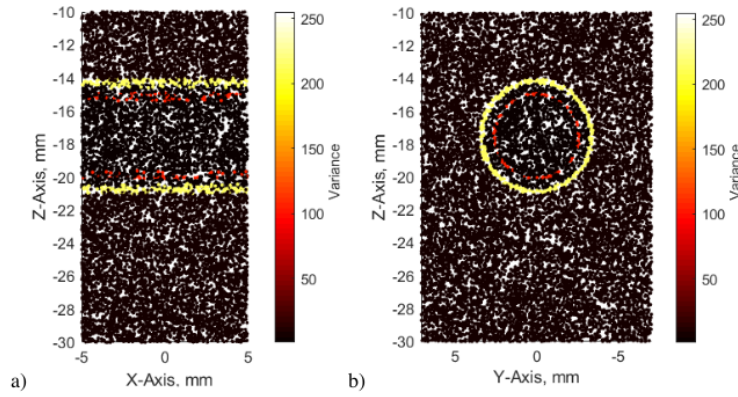


Figure 2.19. 3D map of scatterers at different viewpoints representing the artery model: a) longitudinal, b) axial

Limitations of the 3D artery model. Blood flow, blood pressure were not incorporated into 3D artery model. The main interest is to model determinate amplitude artery motion and evaluate capability of motion tracking algorithms to detect it. Simulation of artery and tissue motion is presented in the next subsection.

2.3.2. Simulation of artery and tissue pulsation

The main purpose was to model not a single B-mode ultrasound image but to simulate a sequence of B-mode images that would reflect radial and longitudinal motions of the artery and surrounding tissue. Since the simulation of a single ultrasound RF frame in the Field II program can take up to several hours (depending on the volume of the model and the number of scatterers), cardiac cycles are similar and quasi-periodic with heart rhythm, it was decided to model only one cardiac cycle of complex (longitudinal and radial) motion.

In vivo radial and longitudinal motion signals of CCA chosen for simulation of artery and tissue pulsation were evaluated and presented in Section 2.1.4.

As mentioned before, only one heart cycle (see the green shadowed area in Figure 2.20 a) for an example) was used in motion modeling. To cut out one cardiac cycle from motion signals, a rectangular window was used. The length of the motion signal segment depended on how long the heartbeat takes, and the beginning and the end of the segment were the moments of systole and diastole correspondingly.

For simulations, the amplitude of preselected and cut-out periods of longitudinal and radial motion signals were normalized taking peak-to-peak amplitude in three levels: 0.5 mm, 0.75 mm, and 1 mm for young healthy volunteers, and 0.25 mm, 0.5 mm, and 0.75 mm for older at-risk patients group. The time axis was not normalized.

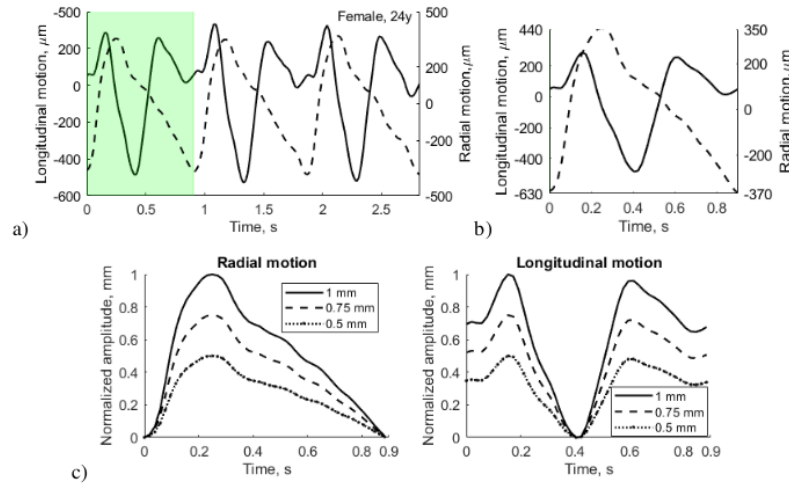


Figure 2.20. Motion signals post-processing for simulation of artery and tissue pulsation: a) *in vivo* radial (dashed line) and longitudinal (solid line) motion signals of CCA with preselected period (green shadowed area) which would be used to model artery and tissue pulsation, b) preselected heart cycle cut out from motion signals, c) motions signals amplitude normalization in three levels

As reported by Golemati *et al.* ^[61], radial and longitudinal motions *in vivo* are weakening away from the artery lumen and express the spatial dependence of displacements which is defined as exponential functions of the axial position. To simulate realistic *in vivo* artery motion, motion slope deep into the artery wall and surrounding tissues were incorporated into the artery model. According to Golemati *et al.* ^[61], $b_1 = -0.1722$ and $b_2 = -1.075$ express the slope of the radial and longitudinal motion amplitude of healthy volunteers accordingly. However, there are no studies that propose slope of the radial and longitudinal motion amplitude of at-risk patients.

Nonetheless, previous studies have shown a relationship between the decrease in longitudinal motion of the CCA wall, arterial stiffness and CVDs^[12]. Taking that into account, the slope of motion's amplitude should be higher in modeling artery motion of at-risk patients. So, it was decided to use 1.5 times bigger b_1 and b_2 values for that purpose.

Table 2.3. Motion modeling parameters of artery model

	Healthy volunteers	At-risk patients
Waveforms of motion signals	see Figure 2.8 a), c), e)	see Figure 2.8 b), d), f)
Radial and longitudinal motions amplitude, μm	1000, 750, 500	750, 500, 250
Slope of radial motion b_1	0.17	0.26
Slope of longitudinal motion b_2	1.08	1.62
Total:	9 cases	9 cases

Mechanical deformation of the arterial wall consisting of two motions was simulated in this stage: 1. radial motion and 2. longitudinal motion. Even though the scatterers are randomly distributed within the artery model volume their coordinates and scattering strength (scatterers amplitudes) are available for the simulation algorithm as a static map. This static map is an input of the Stage 2 simulation where at each scatterer's coordinates a definite magnitude (the increment motion signal for the next time moment) and nature (radial or longitudinal) displacement were added (see Figure 2.20 a). The scatterer's strength for particular tissue was kept constant as assigned at the initiation of modeling.

Each step of the artery and surrounding tissue pulsation simulation is explained in detail below following a functional diagram of Stage 2 in Figure 2.21.

Step 1. Initially, the artery center of the artery model is set at 17.5 mm in depth (see Figure 2.17). Before adding radial and longitudinal displacement to a particular scatterer, the coordinate system is centered at the artery center (coordinates (0; 0) are at the artery center). In the next steps, Cartesian and polar coordinates were used for longitudinal and radial scatterer's movement simulation accordingly.

Step 2. Simulating radial motion component, before adding displacement to a particular scatterer, the Y and Z coordinates of scatterers were recalculated from Cartesian to polar. Scatterers not belonging in static map to the artery lumen (diameter $D_0 = 5$ mm) are then selected and radial displacement $d_{radial}(f)$ in the polar coordinate system was applied to each scatterer. Since the radial motion of the artery in the sequence of B-mode images is the sum of the motions of the proximal and distal artery walls (the motion of the proximal wall is equal to the motion of the distal wall), only the half of displacement of radial motion is added in the artery model. The magnitude of the displacement of artery layers and surrounding tissues depends on the coordinates of the scatterers, i.e. the farther the scatterer is from the lumen radius, the lower magnitude of the displacement $d_{radial}(f)$ was added:

$$Slope_{radial} = \begin{cases} 1, & |y| = r_l \\ e^{b_1|y-r_l|}, & |y| > r_l \end{cases}, \quad (3)$$

where y is the radial position, $r_l = 2.5$ mm is the initial lumen radius, b_l expresses the slope of the radial displacement.

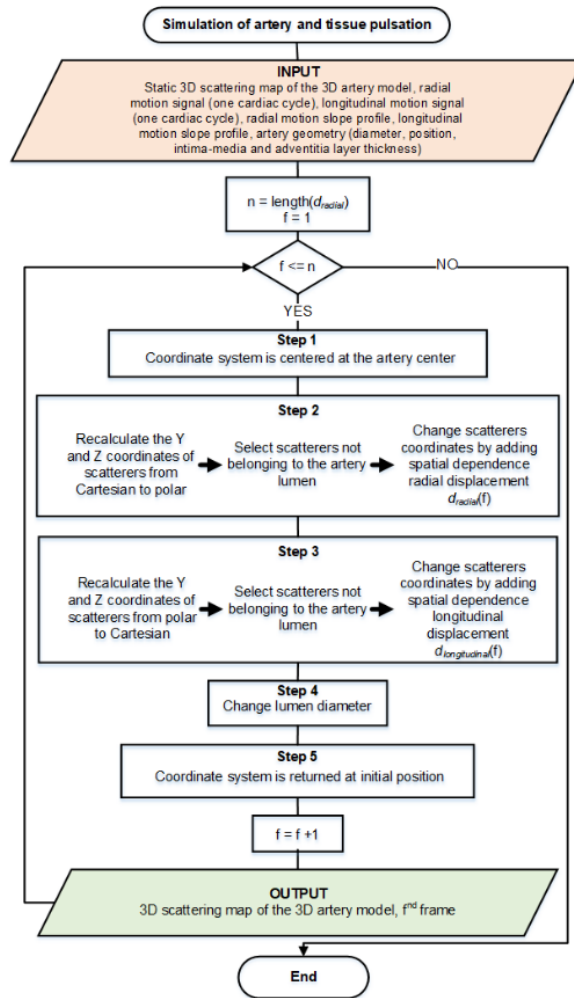


Figure 2.21. Functional diagram of Stage 2, simulation of the complex artery and tissue pulsation. Here f corresponds to the currently analyzing frame number in the motion signal and n – total number of such frames

In this way, the field of spatial-dependent radial displacements (see Figure 2.22) propagating away from the artery lumen radially and declining in surrounding tissues is modeled.

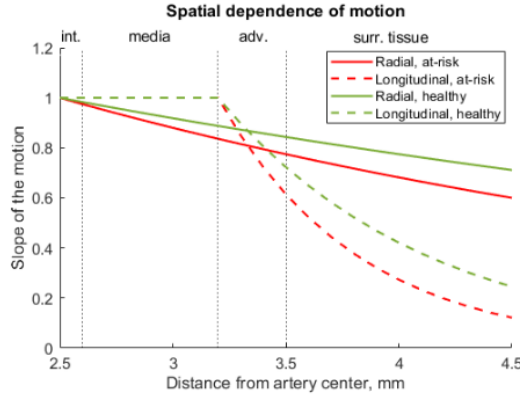


Figure 2.22. Spatial dependence of radial and longitudinal motions for healthy (slope of radial and longitudinal motions $b_1=0.17$, $b_2=1.08$) and at-risk (slope of radial and longitudinal motions $b_1=0.26$, $b_2=1.62$) subjects. The amplitude of radial motion is greatest at the surface of the artery (2.5 mm) and decreases exponentially into the surrounding tissues; the amplitude of longitudinal motion is greatest at the *intima-media* complex (at 2.5–3.2 mm), decreases significantly into the *adventitia* layer (3.2 – 3.5 mm), and finally, longitudinal motion amplitude is negligible in the surrounding tissues

Step 3. After adding the radial displacement, the coordinates of the scatterers were again converted from polar to a Cartesian coordinate system.

Scatterers not belonging to the artery lumen in static map (diameter $D_0 = 5$ mm) are then selected, and longitudinal displacement $d_{longitudinal}(f)$ in the X-Z plane is added to each scatterer. Other studies ^[52,151] have demonstrated that the *intima-media* complex shows a larger longitudinal motion than the *adventitia* layer. Therefore, for scatterers that were outside the *intima-media* complex, i.e. *adventitia* layer and surrounding tissues, longitudinal displacement was added with sloping according to distance from the artery center (see Figure 2.22):

$$Slope_{longitudinal} = \begin{cases} 1, & r_l \leq |y| \leq r_{ma} \\ e^{b_2|y-r_{ma}|}, & |y| > r_{ma} \end{cases}, \quad (4)$$

where y is the radial position, $r_l = 2.5$ mm is the lumen radius, $r_{ma} = 3.2$ mm is the radius of the *media-adventitia* boundary, b_2 expresses the slope of the longitudinal displacement.

Step 4. In Step 2 the artery wall was displaced, the lumen diameter had changed therefore at each next frame of the sequence lumen was modeled as a cylinder with variable diameter:

$$D_{lumen}(f_2) = D_0 + d_{radial}(f_1), \quad (5)$$

where $D_{lumen}(f_2)$ – lumen diameter for the 2-nd frame of the sequence, D_0 – lumen diameter (const.), $d_{radial}(f_1)$ – radial displacement between the two artery walls at the 1-st frame of the sequence.

Step 5. The coordinate system is returned to its initial position, i.e. at 17.5 mm in depth. Thus, in each subsequent frame (f_2, f_3 , etc.) the coordinates of the scatterers in the artery model were recalculated and lumen with varying diameter what yield all remaining frames of artery motion was modeled.

2.3.3. Simulation of sequential US data

Using Field II software ^[36,38] the RF ultrasound signals were simulated from a time sequence of scattering 3D maps of the artery model. While simulating RF signals, a model of linear array transducer was used. Field II parameters used to simulate scanning with linear array transducer are listed in Table 2.2. From the simulated US RF signals, the sequences of B-scan images were calculated. Example of the B-scan image presented in Figure 2.23.

The resulting simulated B-scan image, in this case, consists of 160 echo lines, the distance between two adjacent echo lines was 0.0625 mm and the image width was 10 mm. One cardiac cycle consisted of 43 image frames or more (frame rate: 52 frames per second) depending on cycle length. Several quasi-periodic cycles were compiled from the first one, while analysis of the one cycle peculiarities was the main concern in this dissertation.

2.3.4. Simulated RF US signal processing algorithms and accuracy evaluation of motion detection

From the simulated US RF data, patterns of radial and longitudinal motion could be evaluated using chosen signal processing algorithms. Two algorithms were employed: one to estimate only radial motion, and one to estimate both radial and longitudinal motions. When the interest is in tissue properties based on motion only in one direction, a classical 1D cross-correlation is an option. The inter-frame radial motion of the artery and surrounding tissue was detected along the beamlines using cross-correlation function, calculated between obtained RF signal segments, and parabolic interpolation of the peak of the correlation function ^[30,152]. This method is presented in detail in section 2.4.1. To get radial motion, the integral of inter-frame radial motion must be calculated. To evaluate both radial and longitudinal tissue motions between adjacent frames, an OpenOpticalFlow algorithm ^[153] was chosen. This method is presented in detail in 2.4.1. The inter-frame displacements were later converted into the accumulated motion relative to the first frame.

Accuracy of motion detection was evaluated in the midline (i.e. a middle scanning line) for various axial positions, i.e. starting from 11 mm every 1 mm to 29 mm. The preselected points, where the accuracy of motion detection was evaluated, are depicted in Figure 2.23.

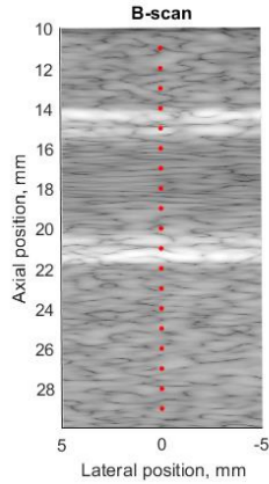


Figure 2.23. Simulated B-scan image of artery model with preselected point (red dots) where the accuracy of motion detection algorithms was evaluated

When evaluating the accuracy of motion detection algorithms, it is important to know how much the observed motion corresponds to predicted motion. For this purpose, different parameters were chosen. The first one is the mean absolute error (MAE) – one of the simpler errors to understand which corresponds to the average of absolute errors, *i.e.* is the difference between the measured value and “true” value:

$$MAE = \frac{1}{N} \sum_{n=1}^N |y_e(n) - y_t(n)|, \quad (6)$$

where MAE – mean absolute error, $n=1 \dots N$, N is the number of samples in motion signal, $y_e(n)$ – estimated motion, and $y_t(n)$ – theoretical motion. But, MAE is not standardized within a predefined range as Pearson correlation coefficient, making it difficult to decide which value of MAE is high and which is low. Also, the magnitude of the error depends on the amplitude of the signal.

The error criterion often uses an estimate of the mean squared error (MSE), which estimates the error between estimated motion $y_e(n)$ and the theoretical motion $y_t(n)$:

$$MSE = \frac{1}{N} \sum_{n=1}^N (y_e(n) - y_t(n))^2, \quad (7)$$

where MSE – mean squared error, $n=1 \dots N$, N is the number of samples in motion signal.

The disadvantage of such an estimate is that square units of error are obtained and it is, therefore, difficult to evaluate the error obtained. Also, the value of the error depends on the amplitude of the motion. Therefore, it makes sense to normalize the

MSE estimate after subtracting the square root from the MSE estimate. The MSE is normalized to the standard deviation of the estimated motion σ_e :

$$NRMSE = \frac{\sqrt{MSE}}{\sigma_e}, \quad (8)$$

and the parameter evaluating the resulting error is called the NRMSE. $NRMSE = 0$ describes the ideal similarity between the estimated and theoretical motions.

In addition to the NRMSE, the accuracy of the algorithms for motion detection was quantified by the Pearson correlation coefficient. The correlation coefficient evaluates the similarity between the estimated and theoretical, and it is also easier to interpret. If we have an estimated motion y_e with a number of data points N and \bar{y}_e – mean of y_e together with the theoretical motion y_t with a number of data points N and \bar{y}_t – mean of y_t , then the correlation between these two motion signals is calculated according to the formula:

$$r = \frac{\sum_{n=1}^N (y_e - \bar{y}_e)(y_t - \bar{y}_t)}{\sqrt{\sum_{n=1}^N (y_e - \bar{y}_e)^2 \cdot \sum_{n=1}^N (y_t - \bar{y}_t)^2}}. \quad (9)$$

The Pearson correlation coefficient r shows the strength of the similarity between the two signals. The values of the correlation coefficient vary within the range $[-1; 1]$. $r = -1$ indicates absolute opposite similarity, $r = 0$ means that the relationship between the two signals does not exist, $r = 1$ indicates absolute positive similarity. An important advantage of the correlation coefficient over the MSE parameter is that the correlation coefficient is automatically normalized within a predefined range. However, the correlation coefficient does not take into account the effect of changes in the constant component (DC component) and amplitude of the signal, but only the morphological similarity of the signals. When estimating radial or longitudinal motion, a less accurate algorithm will evaluate a smaller amplitude of motion signal, although partial morphological similarity would be maintained. Taking into account such a possibility, the Pearson correlation coefficient and NRMSE are important parameters to evaluate the accuracy of the motion detection algorithms.

2.3.5. Evaluation of slope profiles of radial and longitudinal motions

As mentioned before, radial and longitudinal motions *in vivo* are weakening away from the artery lumen and express the spatial dependence of displacements which is defined as exponential functions of the axial position^[61]. This concept was incorporated into the 3D artery model. The question was raised, if it is possible to differentiate arteries having a variety of motion amplitudes and waveforms only by motion slope profile deep into the tissue?

For that purpose, slope profiles of modeled radial and longitudinal motions were determined. The first step is to estimate both radial and longitudinal motion signals from simulated RF US signals at the preselected points as depicted in Figure 2.23. Algorithms for radial and longitudinal motion detection are presented in the 2.4.1 section. Then the maximal values of radial and longitudinal motion signals were found at the preselected axial positions. These values were normalized according to

the initial radial and longitudinal motions amplitude in the 3D artery model (see Table 2.3). For example, 1 mm longitudinal motion amplitude was incorporated into the 3D artery model. At the preselected axial position, the estimated peak-to-peak amplitude of the longitudinal motion signal is 0.96 mm. After normalization (0.96 mm/1 mm), the slope of the motion is 0.96. The same normalization procedure was done with all preselected points at different axial positions (see Figure 2.23).

Slope profile evaluation was done with all cases of modeled data, i.e. as a result, 18 estimated slope profiles (9 for radial motion and 9 for longitudinal motion) are for a healthy volunteers group and 18 (9 for radial motion and 9 for longitudinal motion) – for an at-risk patient group. Mean values and standard deviations of slope profiles were calculated for healthy volunteers and at-risk patients groups for every preselected axial position.

2.4. RF ultrasound signals post-processing algorithms

2.4.1. Algorithms for radial and longitudinal motion detection

The methodology described in this section has been published in “Quantification of Endogenous Brain Tissue Displacement Imaging by Radiofrequency Ultrasound”^[30].

The same ultrasonic RF signal processing algorithm was used for both the motion signal of a short segment of the RF signal and radial motion estimation of the CCA wall. Combining the classical 1D cross-correlation function, calculated between the obtained RF signal segments, and parabolic interpolation of the peak of the function, the motion along the scanning line was estimated^[30,152].

The cross-correlation lag between the segments at adjacent scanning frames f and $f+1$ represents the inter-frame estimate (velocity) of motion magnitude. The correlation peak was estimated as follows^[152]:

$$C_f[n] = \max_{-T \leq z \leq T} \left[\mathcal{F}^{-1} \left\{ \mathcal{F} \left[w[z] \cdot S_f^*[z] \right] \cdot \mathcal{F} \left[w[z] \cdot S_{f+1}[z] \right] \right\} \right], \quad (10)$$

where S is the RF signal segment at a certain scanning line and scanning depth, \mathcal{F} is the Fast Fourier transform, acquisition instance (frame number) $f = 1 \dots F$, * the asterisk denotes the complex conjugate. The empirical threshold value T was set at $\pm 150 \mu\text{m}$, w is the Hamming window function, $z = 1 \dots Z$, Z is the number of samples of RF the signal segment (0.924 mm of six periods of US wave) used for the assessment of displacements, n is the correlation lag at the peak of the function. To prevent false peaks of the cross-correlation function, which occur when a secondary correlation peak exceeds the primary peak, the threshold is used. The threshold was set after analyzing the outcomes of the algorithm—the estimated motion signals. To suppress the leakage in the frequency domain and to increase the probability of the right correlation peak detection, the tapering function was applied. Nonetheless, when the tissue motion is higher than a quarter of the wavelength of the ultrasound echo data, the probability of identifying false correlation peaks increase. This results in large tracking errors that are known as “peak hopping” errors^[154]. To overcome these errors, it was decided to attribute “Not-a-Number” value to inter-frame motion that is

higher than a quarter of the wavelength. Finally, the inter-frame estimate with integer accuracy of motion magnitude $IF_motion_{integer}[f]$ was defined as follows:

$$IF_motion_{integer}[f] = \Delta d \cdot C_f[n], \quad (11)$$

where $C_f[n]$ is the largest sample of the cross-correlation function, Δd is the RF signal sampling period ($\Delta d = 19.25 \mu\text{m}$).

Nevertheless, only at the integer sample level, the magnitude of the cross-correlation function can be estimated. A variety of approaches in the literature have been suggested to achieve sub-sample accuracy^[155,156,157,158,159]. The fundamental concept behind these methods is to fit the (discretely estimated) magnitude of the function of cross-correlation into an underlying analytical function. Consequently, it is possible to analytically resolve the position of the true correlation peak^[154] (see Figure 2.24). Due to its efficiency and simple implementation, parabolic interpolation^[155] of the correlation peak was applied to obtain a sub-sample resolution of the inter-frame estimates of motion magnitude since the estimated inter-frame estimate of motion magnitude had integer accuracy. Sub-sample accuracy of the inter-frame estimate of motion magnitude $IF_motion_{sub}[f]$ was defined as follows^[152]:

$$IF_motion_{sub}[f] = \Delta d \cdot \frac{C_f[n-1] - C_f[n+1]}{2(C_f[n-1] - 2 \cdot C_f[n] + C_f[n+1])}, \quad (12)$$

where $C_f[n-1]$ and $C_f[n+1]$ are the nearest neighbors of the largest sample of cross-correlation function $C_f[n]$, f is the acquisition instance (frame number), $f=1 \dots F$.

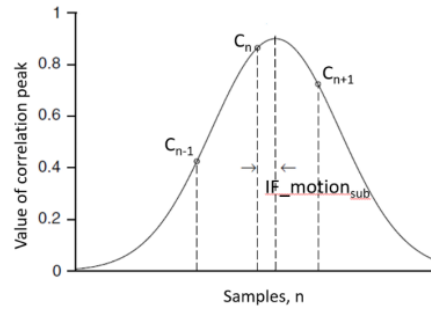


Figure 2.24. Interpolation of the correlation peak for sub-sample estimation

Finally, summing up both inter-frame estimates of motion magnitude with integer and sub-sample accuracies, the inter-frame motion IF_motion was estimated as follows:

$$IF_motion[f] = IF_motion_{integer}[f] + IF_motion_{sub}[f]. \quad (13)$$

Since the distance is the integral of velocity, the motion signal relative to the transducer was calculated by the integral (cumulative sum) of the inter-frame motion signal.

Radial motion estimation of the CCA wall was done by using the cross-correlation functions and parabolic interpolation methods described above. In the case of the artery wall motion, the radial motion was detected in the ROI, which covered the proximal and distal walls of the artery (see Figure 2.25). The width of ROI in all cases was 5 mm (81 echoscopic lines, lateral resolution $62.5 \mu\text{m}$) while the height of ROI was 10 mm on purpose to cover both walls of the artery. The ROI was then divided equally into two parts: the top of the ROI (proximal arterial wall and upper part of the lumen) and the bottom of the ROI (distal arterial wall and lower part of the lumen). Cross-correlation and parabolic interpolation methods were then applied to the RF signal segments in the length of 5 mm in these two ROIs. After calculating the inter-frame motion for each echoscopic line, integrating them, and summing the top and bottom motion signals, the radial motion signals of the ROI were found ($n = 81$). Averaging these signals over time yielded an average signal of CCA wall motion in the 5 mm segment.

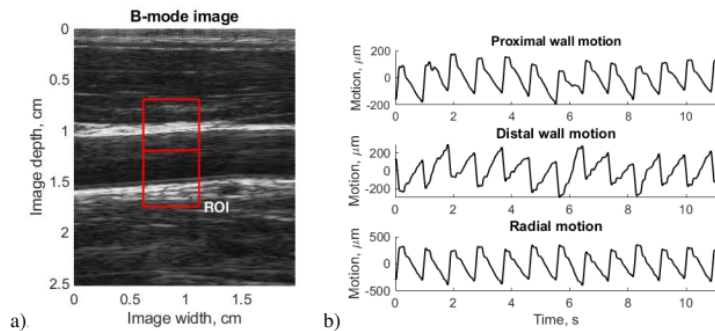


Figure 2.25. B-scan image with outlined ROI (a) and proximal, distal artery wall motion together with a total radial motion of CCA wall (b). The motion detected in the upper and lower part of outlined ROI corresponds to the proximal and distal wall motion accordingly. Summing the proximal and distal motion signals, the radial motion signals of the ROI were found. 53 years old female

Intending to detect larger tissue motion, the main disadvantages of the 1D cross-correlation method become apparent: 1. Motion only in the axial direction (along beamline) could be detected, 2. “peak hopping” errors results if motion is higher than a quarter of the wavelength. To avoid the abovementioned 1D cross-correlation drawback, another motion detection algorithm could be used. One of those kinds of algorithms – modern optical flow algorithms, which allow the estimation of motion in the plane, is more resistant to the rotation of the parts and can be used to evaluate both macro and micro level motion ^[154].

OpenOpticalFlow – an open-source optical flow program in MATLAB for extraction of high-resolution velocity fields from various flow visualization images

by Tianshu Liu ^[153] (freely available at: <https://github.com/Tianshu-Liu/OpenOpticalFlow>).

The simulated RF signals were normalized to 1, an envelope (Hilbert transformation) of simulated RF these signals were presented in decibels, the resulting data stronger than -90 dB was normalized from 0 to 255, and then passed as an input for OpenOpticalFlow to identify motion between adjacent frames. Parameters used for OpenOpticalFlow: size filter 4, Horn-Schunck estimator for initial field $\lambda_1 = 120$, Liu-Shen estimator for refined estimation $\lambda_2 = 3000$; these parameters were selected as optimal combination after preliminary investigation within size filter values from 1 to 30, λ_1 values from 1 to 1000, λ_2 from 100 to 10000 by comparing results with theoretical scatters movement and evaluating movement precision and smoothness. The inter-frame displacements were later converted into the accumulated motion relative to the first frame.

2.4.2. Post-processing of radial motion of the CCA wall

Post-processing of radial motion signal of the CCA artery consist of three main steps:

- motion signal filtering;
- detection of the end of diastole moments in motion signal;
- detection of correlated periods.

Motion signals were filtered with a band-pass IIR filter ($f_{pass-lower} = 0.5$ Hz and $f_{pass-higher} = 8$ Hz, filter order 2nd) and then detrended, subtracting the mean or a best-fit line (in the least-squares sense) from the resulting signal. Then, detection of diastolic moments in radial motion signal was done by calculating the second derivative of motion signal, *i.e.* acceleration signal, and searching for peaks spaced at least 1 second time interval with a minimum peak height of 1/3 of the maximum value in the acceleration signal. The time interval between two adjacent peaks was chosen according to that for adults, the normal resting heart rate varies between 60 and 100 beats per minute, while the minimum peak height value was chosen experimentally. The peaks in the acceleration signal over time coincide with the diastolic moments ^[160,161] in the radial motion signal (see Figure 2.26).

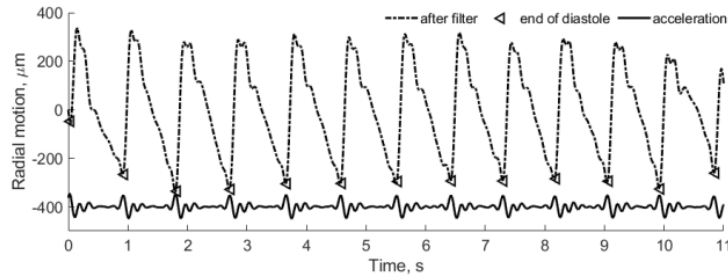


Figure 2.26. End of diastole detection in radial motion signal according to the peaks in the acceleration signal. 53 years old female

The motion signal, from the first to the last peak found in the acceleration signal, was divided into separate periods and those periods were aligned according to the diastolic moments (see Figure 2.27 b).

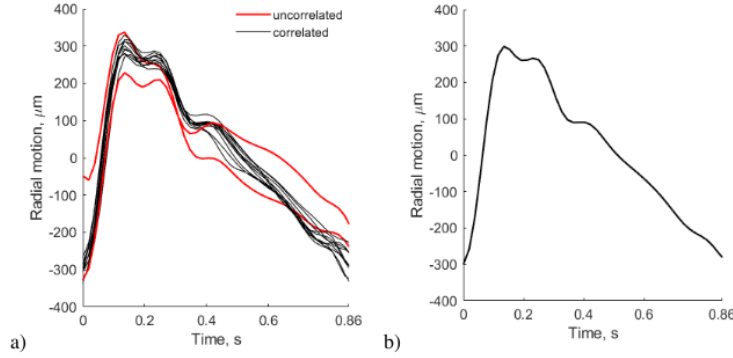


Figure 2.27. Detection of the average period for radial motion parametrization in time and frequency domain: a) periods of motion signal alignment according to the end of diastole and detection of both correlated and uncorrelated periods, and b) the average period of radial motion signal. 53 years old female

The length of all periods was set equal to the shortest period in the motion signal as proposed in [162]. This gives a $\mathbf{P}[p \times l]$ matrix, where p – number of periods, l – period length. In the next step, correlation coefficient matrix $\mathbf{R}[p \times p]$ between the motion signal periods was estimated, and diagonal was removed as it represents autocorrelation result:

$$\mathbf{R} = \begin{bmatrix} 1 & R_{12} & R_{13} & \dots & R_{1p} \\ R_{21} & 1 & R_{23} & \dots & R_{2p} \\ R_{31} & R_{32} & 1 & \dots & R_{3p} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ R_{p1} & R_{p2} & R_{p3} & \dots & 1 \end{bmatrix}. \quad (14)$$

Then an averaging was done to obtain a row vector $\mathbf{S}[1 \times p]$ with the mean of the correlation coefficient in each column. Vector \mathbf{S} indicates periods similarity. The periods were assumed similar if the correlation coefficient value exceeded 0.95 [29,30,152]. Applying the threshold of 0.95, periods that correlate less with the remaining periods were determined and excluded from the calculation of the average period of radial motion signal. Meanwhile, similar periods were averaged over time and an average period of radial motion signal is obtained, which was used to parametrize motion in the time domain. Moreover, spectrum estimation approaches were applied to detect frequency domain parameters.

2.4.3. Spectrum estimation approaches

Fourier based power spectrum estimates are referred to as classical methods. The advantages against other methods is that Fourier transform methods are most robust of the spectral estimators, require no assumptions about the origin or nature of the data, and accurately estimates the spectrum of the signal with the noise while usually the spectrum is wanted of the noise-free signal. Modern approaches for the spectrum estimation are designed to overcome the distortions produced by the classical approach are particularly effective if the data segments are short ^[163]. Therefore, to estimate the spectrum of average period of radial motion as it length is about one second (normal heart rate 60 beats/minute, frame rate 52 Hz, average period of radial motion length about 52 samples) will be more constructive to use modern approaches instead of classical methods.

One of the classes of modern techniques is parametric or model based. To estimate the power spectrum, parametric methods make use of an linear time-invariant model. The basic strategy of this approach is that model is assumed to be driven by white noise. Then, output of model is compared with the input waveform, and the model parameters are adjusted for the best match between model output and the waveform of interest. Finally, spectrum is computed ^[163].

Autoregressive power spectral density estimate — Yule-Walker method and autoregressive power spectral density estimate — modified covariance method were selected and investigated in detail to chose the better approach and optimal model order for the average period of radial motion signal spectrum estimation. Yule-Walker and modified covariance approaches to spectral estimation are implemented in the MATLAB R2018b (The MathWorks, Inc., Natick, USA) Signal Processing Toolbox (*pyulear*, *pmcov*). To determine optimal model order, an investigation was carried out. Firstly, a sinusoidal signal of 1 Hz, 1 s duration, and 52 Hz sampling frequency was modeled. Then changing the model order from 1 to 20, spectrum was computed using *pyulear* and *pmcov* functions, and maximal value of spectrum was detected reflecting the modeled sinusoidal signal frequency. Frequency dependence on model order is depicted in Figure 2.28.

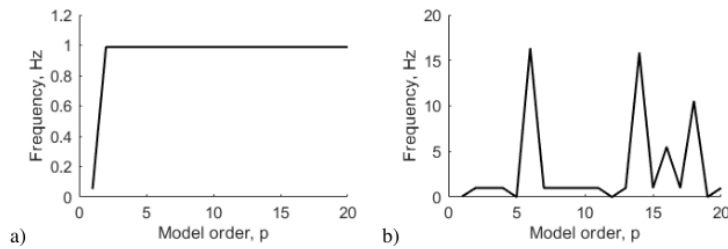


Figure 2.28. Frequency detection dependence on model order: a) Yule-Walker method and b) modified covariance method.

As follows from the figure shown above (see Figure 2.28), model order does not influence detected frequency when the Yule-Walker method was used rather than modified covariance. When the modified covariance approach was used, the detected frequency was highly similar to the frequency of the modeled signal. Going into deeper analysis, not only frequency dependence on the model order but both model order and signal-to-noise ratio (SNR) were investigated choosing the better approach to compute the average period of radial motion signal spectrum.

During the investigation of Yule-Walker and modified covariance methods for a capability to detect 1Hz frequency the model order was changed from 1 to 30, while the SNR of modeled sinusoidal signal was from -5dB to 10 dB by every 1dB. If the maximal value of spectrum rounded to the nearest integer is equal to 1 Hz, then the result of model order and SNR combination is represented as green, otherwise as red (see Figure 2.29).

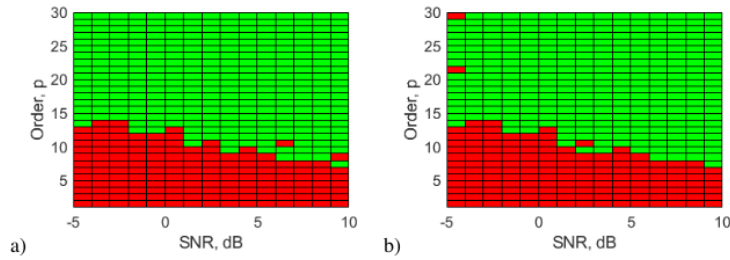


Figure 2.29. Frequency detection dependence on model order and SNR: a) Yule-Walker method and b) modified covariance method

It is seen from Figure 2.29 that Yule-Walker and modified covariance methods are capable to detect 1Hz frequency when the model order is 14 or more despite the SNR value. Taking into account these results, model order was chosen to be constant and equal to 14 for further analysis.

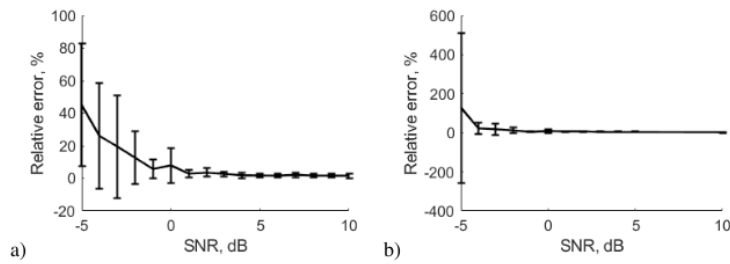


Figure 2.30. The relative error between modeled and detected frequency dependence on SNR: a) Yule-Walker method (model order const.=14) and b) modified covariance method (model order const.=14). Errorbar represents the mean and standard deviation of relative error (n=40)

The relative error between modeled and detected frequency was evaluated when the model order was 14 and SNR was from -5dB to 10 dB by every 1dB. As can be seen from Figure 2.30, mean relative error is from 6 % to 45 % and 6 % to 127 % when Yule-Walker and modified covariance methods were used correspondingly and SNR is 0 dB or lower. If SNR is higher than 0 dB, mean relative error is from 1.6 % to 3.5 % and 2.3 % to 6.7 % when Yule-Walker and modified covariance methods were used accordingly.

Summing up all the above presented results, the Yule-Walker method was chosen for spectrum computation of the average period of radial motion signal due to its robustness to detect modeled signal frequency against the modified covariance method.

2.4.4. Parametrization of radial motion signals

The focus of recent researches has been only on the longitudinal motion amplitude in different heart cycle phases. Predominantly, measure the first antegrade, the first retrograde, and the peak-to-peak amplitude of the longitudinal motion during the heart cycle was measured [21,164,165]. The entire longitudinal motion pattern (waveform) can be useful even though the longitudinal motion amplitude is used and can distinguish healthy volunteers from at-risk patients [164,166]. Moreover different individuals are characterized by different longitudinal motion patterns [62,165]. To the best knowledge of the author of this dissertation, the frequency domain estimates for arterial wall motion were not tested in healthy controls and at-risk patients.

Therefore time and frequency domain parameters were chosen for parametrization of the average period of radial motion signal (see

Table 2.4).

Table 2.4. Time and frequency domain parameters for parametrization of the average period of radial motion signal

Time domain parameters	Frequency domain parameters (in range of 0-10 Hz)
• Heart rate	• Spectral centroid
• Motion amplitude	• Spectral spread
• Velocity amplitude	• Spectral skewness
• Acceleration amplitude	• Spectral kurtosis

The peak-to-peak value of the average period of radial motion signal was referred to as motion amplitude in the time domain. Taking the first and the second derivatives of the average period of radial motion signal, velocity and acceleration signals were calculated, and the peak-to-peak values of those signals were referred to as velocity and acceleration amplitudes in the time domain correspondingly.

The length of all correlated periods of radial motion signal was determined and heart rate was estimated by:

$$BPM = \frac{FPS \cdot 60}{\frac{\sum_{n=1}^N L}{N}}, \quad (15)$$

where *BPM*—beats per minute, *FPS*—frames per second (radial motion signal discretization in time), *L*—the length of the correlated period by samples, $n=1:N$, *N* is the number of correlated period in radial motion signal.

Frequency domain parameters were evaluated from the power spectrum of the averaged period of radial motion signal and presented further (see Figure 2.31).

Spectral centroid μ_1 characterizes the "center of gravity" of the spectrum ^[167]:

$$\mu_1 = \frac{\sum_{k=b_1}^{b_2} f_k s_k}{\sum_{k=b_1}^{b_2} s_k}, \quad (16)$$

where f_k is the frequency in Hz corresponding to bin *k*, s_k is the spectral value at bin *k*, b_1 and b_2 are the band edges, in bins, over which to calculate the spectral centroid.

Spectral spread μ_2 is the standard deviation around the spectral centroid ^[167]:

$$\mu_2 = \sqrt{\frac{\sum_{k=b_1}^{b_2} (f_k - \mu_1)^2 s_k}{\sum_{k=b_1}^{b_2} s_k}}, \quad (17)$$

where f_k is the frequency in Hz corresponding to bin *k*, s_k is the spectral value at bin *k*, b_1 and b_2 are the band edges, in bins, over which to calculate the spectral spread, μ_1 is the spectral centroid.

Spectral skewness μ_3 measures symmetry around the spectral centroid ^[167]:

$$\mu_3 = \frac{\sum_{k=b_1}^{b_2} (f_k - \mu_1)^3 s_k}{\mu_2^3 \sum_{k=b_1}^{b_2} s_k}, \quad (18)$$

where f_k is the frequency in Hz corresponding to bin *k*, s_k is the spectral value at bin *k*, b_1 and b_2 are the band edges, in bins, over which to calculate the spectral skewness, μ_1 is the spectral centroid, μ_2 is the spectral spread.

Spectral kurtosis μ_4 measures the flatness, or non-Gaussianity, of the spectrum around its centroid. Conversely, it is used to indicate the peakiness of a spectrum ^[167]:

$$\mu_4 = \frac{\sum_{k=b_1}^{b_2} (f_k - \mu_1)^4 s_k}{\mu_2^4 \sum_{k=b_1}^{b_2} s_k}, \quad (19)$$

where f_k is the frequency in Hz corresponding to bin *k*, s_k is the spectral value at bin *k*, b_1 and b_2 are the band edges, in bins, over which to calculate the spectral kurtosis, μ_1 is the spectral centroid, μ_2 is the spectral spread.

Above-mentioned time and frequency domain parameters ability to discriminate healthy volunteers from at-risk patients were evaluated by calculating and plotting receiver-operating characteristic (ROC) curves, evaluating of area under curve (AUC) and estimating sensitivity and specificity of proposed parameters. Sensitivity is defined as:

$$\text{Sensitivity} = \frac{TP}{TP+FN}, \quad (20)$$

where TP is the number of the number of true positives and FN is the number of false negatives. Specificity is obtained by:

$$Specificity = \frac{TN}{TN+FP}, \quad (21)$$

where TN is the number of the number of true negatives and FN is the number of false positives.

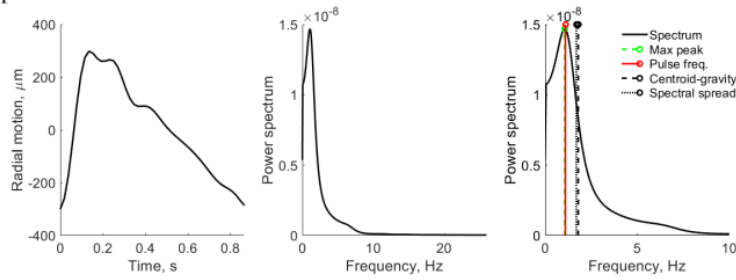


Figure 2.31. Averaged period of radial motion signal in the time domain (*left*), averaged period of radial motion signal in the frequency domain (*middle*), and spectrum with calculated frequency domain parameters in the range of 0-10 Hz (*right*). 53 years old female

2.5. Conclusions of the 2nd chapter

1. A virtual scanning simulation adequate to physical ultrasonic scanning was developed. It is based on a comparison of axial, lateral, and elevation plane resolution between physical scanning and digital simulation. An investigated virtual scanning could be used for the development and testing of complex echoscopy solutions in silico.
2. A 3D artery model capable to reproduce the biomechanical behavior of human CCA for simulation of US RF signals was created. The model enables the evaluation of both the artery geometry (artery diameter, intima-media complex thickness) and the amplitude, shape, and slope of elastic motions deep into the tissues. This opens possibilities for the development and validation of algorithms for the processing of RF signals or B-mode images, e.g. micro-motion tracking, elastography, etc.
3. The accuracy of the proposed motion detection algorithms using simulated CCA US RF signals was investigated and evaluated. That opens possibilities for further development and investigation of motion detection algorithm in vitro and endogenous motion detection application in clinical practice.
4. Parametrization of radial motion signals was proposed. It may prove valuable in risk stratification for the disease of atherosclerosis.

3. RESULTS

3.1. Fitting scanning model to physical PSF

Adequacy of the simulation depends on the conformance of the simulated ultrasound pulse shape to the experimentally measured one. Emitted ultrasound pulse model is 2 periods of 5 MHz oscillation modulated by Hanning function. Figure 3.1 is presented pulse shape and frequency spectra of reflection from wire target located 15 mm from the physical transducer, and simulated by Field II and experimentally measured in the same position. The comparison shows a relatively good agreement (Pearson correlation coefficient between measured and simulated pulse-echo waves is 0.91, while between their spectrum is 0.98) since results are influenced by ultrasound diffraction and other propagation effects.

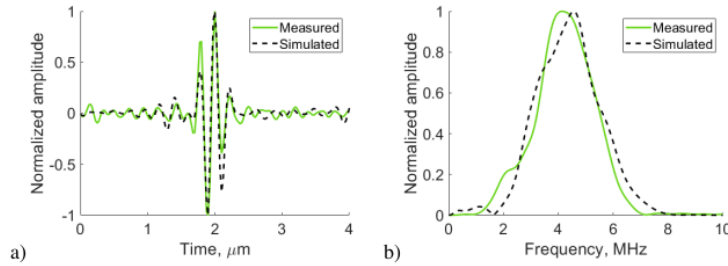


Figure 3.1. Comparison of measured physical and simulated digital a) pulse-echo waves reflected from wire targets at 15 mm depth (axial view) and b) their spectrum.

Regardless of good agreement of measured physical and simulated digital pulse-echo waves and their spectrum, it seems relevant to go deeper in the analysis trying to ensure similarity between experiment and simulation. Therefore, FWHM was used as a resolution parameter that determines quantitatively the axial, lateral, and elevation width of PSF of both measured physical and simulated digital phantoms.

Simulation of wire phantom using the scanning parameters, shown in Table 2.2, was compared with experimental scanning results and presented in Figure 3.2. PSF axial positions are compared using a common axis of depth (see Figure 3.2). Axial and lateral profiles of experimental and simulated PSFs are compared using common normalized axes. Summary of quantitative FWHM parameter comparison between experiment echoscopy and simulation are presented in Table 3.1. It shows that the average relative error of axial and lateral resolution is 11.6 and 15.2 percent accordingly. Results show some discrepancy in the lateral position of reflections from equidistant wires – scatterers lateral positions in experimental echoscopy did not were exactly at 0 mm positions and variates between -0.13 mm and 0.06 mm. Hypothesizing, this could be due to that the internal deformations could occur in urethane rubber with embedded scattering wires, as the phantom is already 10 years after manufacture. Thus, internal deformation influenced the average relative error of

axial and lateral resolutions as PSF of experimental echoscopy and simulation were not exactly at the same positions.

Table 3.1. FWHM parameter comparison of experimental echoscopy and simulation

Experimental echoscopy				Simulation				Axial resolution relative error, %	Lateral resolution relative error, %
Scatterers axial position, mm	Scatterers lateral position, mm	Axial resolution, mm	Lateral resolution, mm	Scatterers axial position, mm	Scatterers lateral position, mm	Axial resolution, mm	Lateral resolution, mm		
9.8	-0.13	0.23	0.80	10.3	0.00	0.26	1.01	13.0	26.3
15.3	0.06	0.24	1.02	15.4	0.00	0.27	1.05	12.5	2.9
20.1	0.06	0.25	1.18	20.4	0.00	0.27	1.03	8.0	12.7
25.2	0.00	0.26	1.37	25.4	0.00	0.27	1.16	3.8	15.3
30.1	-0.06	0.24	1.46	30.4	0.00	0.29	1.29	20.8	11.6
35.6	-0.06	0.26	1.69	35.3	0.00	0.29	1.31	11.5	22.5
Average, %								11.6	15.2

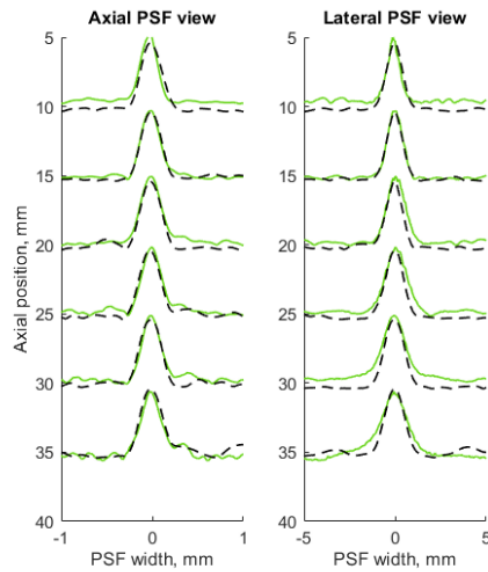


Figure 3.2. Comparison of the axial and lateral width of PSF: solid green line – experimental echoscopy of physical wire phantom, dashed black line – simulation of digital wire phantom. PSF amplitudes were normalized from 0 to 5

Figure 3.2 shows that simulation results of an axial view of normalized PSF coincide better with the experiment than a lateral one, which is influenced by difficult-to-account parameters of apodization, focusing, and other ultrasound diffraction effects.

Since PSF is the most important measure of resolution, a more detailed analysis in two dimensions is provided further (see Figure 3.3). The axial dimension of PSF is influenced by the pulse duration and spectrum which is quite similar both in simulation and experiment (see Figure 3.1) and is much smaller than the lateral one. At a focal distance zone ($z=15$ mm) lateral dimension is smaller than at a far-field ($z=35$ mm), but simulation and experimental results presented in Figure 3.3 have a good agreement. From the two-dimensional representation of PSF are seen some peculiarities of both experimental and simulation results: an asymmetrical profile in the lateral direction in experimental echoscopy, while PSF of simulation data are symmetrical in axial and lateral directions. Also, the fact that the lateral peaking coordinate of simulated PSF is observed centered at zero of the lateral position, while experimental PSF profiles are slightly deviating from this position.

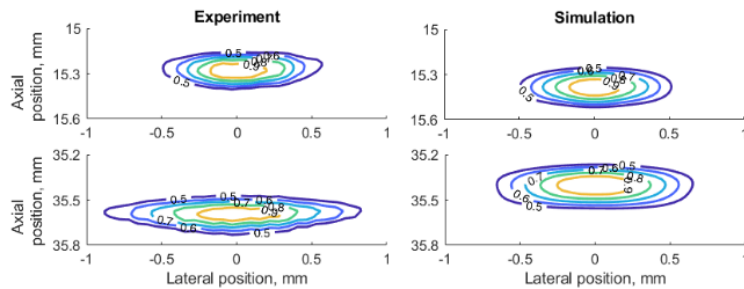


Figure 3.3. Comparison of PSF using isoline diagrams of RF signals reflected from targets at approximately 15 and 35 mm: experimental echoscopy of physical wire phantom (left column) and simulation of digital wire phantom (right column). Isolines presented at 0.1 intervals (from 0.5 to 0.9) of a normalized envelope of RF signals

Digital slice thickness phantom (see Figure 2.13 b) is used for evaluation of scanning resolution in an elevation plane, perpendicular to the scanning plane. B-scan slice thickness or beamwidth in the elevation plane was evaluated according to the method pioneered by Goldstein and Madrazo^[146] and updated later^[147]. In a physical experiment, the phantom with a 45° inclined scattering plane was used^[145]. The distance of the B-scan central line intersection with the scattering plane was 15 mm as observed in the scanner monitor and RF signals were saved for B-scan formation. Using Field II software, the 45° inclined scattering plane phantom was modeled (see Figure 2.15 b) RF signals were simulated and a corresponding B-scan image was composed. Experimental and simulated B-scan images of this case are presented in Figure 3.4, while the envelopes of the laterally averaged scanning lines obtained from the inclined plane of physical and digital slice thickness phantoms – at Figure 3.5. The

FWHM of the beam in the elevation plane was 1.21 mm in physical echoscopy while in digital elevation phantom simulation it was 1.38 mm.

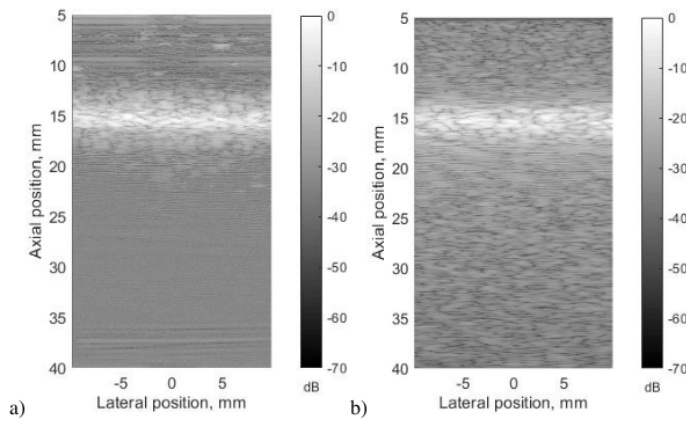


Figure 3.4. Comparison of slice thickness (elevation resolution) in a) physical and b) digital elevation phantoms B-scan images

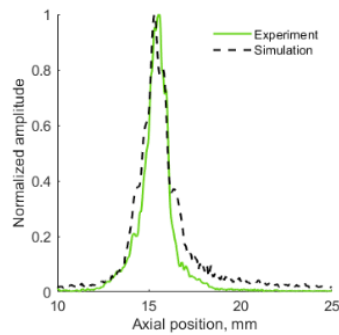


Figure 3.5. Comparison of elevation resolution along the laterally averaged scanning lines of physical echoscopy and digital elevation phantom simulation

Elevation resolution of physical echoscopy and simulation (see Figure 3.4 and Figure 3.5) is in qualitatively good agreement (Pearson correlation coefficient is 0.97). In simulated and practical B-images (see Figure 3.4) and in envelopes of laterally averaged scanning lines along axial scanning direction (see Figure 3.5) specular pattern is seen especially in the inclined plane zone, *i.e.* 15 mm. In sonography, the PSF width in the elevation plane usually is represented on the axis of axial distance [146,147]. According to estimation methods, the widths of PSF in axial and elevation directions are inter-related. In the experiment case (see Figure 3.5) the FWHM of the

beam in the elevation plane is 1.21 mm and in the simulation case is 1.38 mm *i.e.*, the simulated beamwidth appears wider than the experimental one. Supposedly, this is due to insufficient simulation accuracy of transducer aperture apodization in the elevation direction.

The final stage of echoscopy simulations is based on wave scattering from randomly distributed scattering centers representing tissue-mimicking material (TMM). Experimental and digital wire phantom B-scan images and central scanning line envelopes are compared in Figure 3.6.

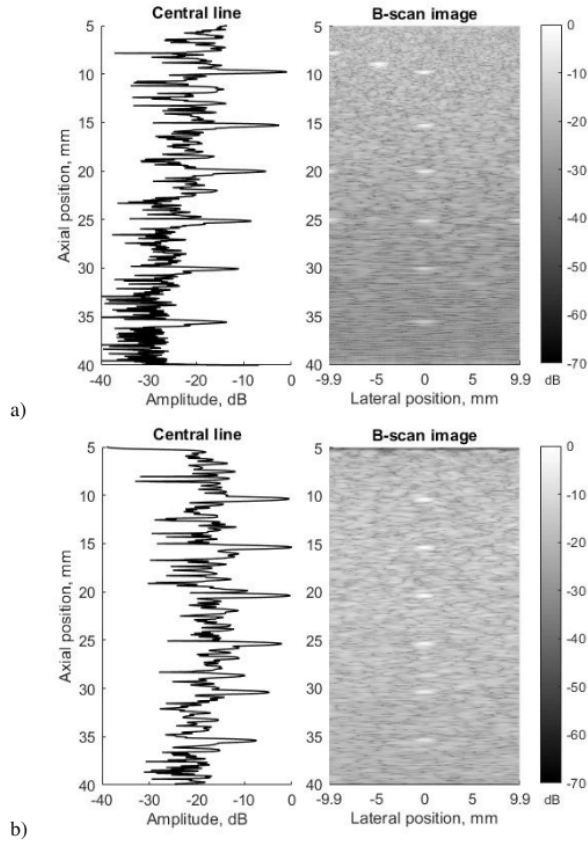


Figure 3.6. Comparison of scattering profile of point targets along central echoscopy line and whole B-scan images of a) measured US image of ATS Model 549 (physical wire phantom) b) simulated US image of digital wire phantom.

It is worth mentioning about the B-scan image formation algorithm that it was common for both RF signals from physical scanner output and RF signals from modeling. So, the proprietary scanner image preparation is excluded from all cases of comparisons. The main difference is seen in the signal scattering from wire targets and background TMM since the energy of ultrasound waves reflected from physical phantom wires is unknown and difficult to simulate adequately. Also, scattering in TMM of physical phantom is not identified in the available documentation and additional fitting of those parameters was out of the scope of the dissertation.

Discussion.

The result shows a good agreement of digital simulation with the physical one. FWHM estimates in the axial direction are according to practical estimates with a discrepancy of less than 12 %. Simulation results of an axial view of normalized PSF coincide better with the experiment than lateral one, which is supposedly influenced by difficulties to account in simulation parameters of apodization, focusing, and other ultrasound beamforming measures taken by the scanner. The FWHM estimates in the lateral direction are according to practical estimates with a discrepancy of less than 16 %.

Comparison of quantitative results with other researchers in Field II simulation of linear array scanning is quite difficult because of a limited number of articles dealing with experimental verification of such simulations. The results thus obtained are compatible with Pham *et al.* ^[41], who presented mean discrepancy between the FWHM of the measured and simulated resolutions were less than 5 % and 18 % in the lateral and axial directions respectively.

Limitations of the present research are related to the possibilities to know all parameters of the ultrasound transducer, beamforming, and standard phantoms as well as with the ability to control needed parameters of Field II software. Rather limited simulation accuracy of the lateral resolution is due to the lack of available information about the peculiarities of focusing and apodization both in transmit and receive. Apodization, especially in elevation direction for 1D apertures is practically defined by transducer technology and difficult to specify.

Simulation of echoscopy is a multitask issue because the outcome of real scanner – RF signals and quality of the B-scan image is a result of many transformations including those induced by the transducer, propagation in non-homogeneous media (tissue), focusing, apodization, filtering, and image presentation. In each stage of those transformations, simulation uncertainties related to insufficient knowledge of parameters to be used in the simulation model is faced with. The present results are an attempt to evaluate and discuss the main simulation uncertainties which are important for the use of simulated data for the developments of imaging technologies.

3.2. Results of simulated RF US signals and images of artery model

To compare *in vivo* US data and *in silico* model data in more detail, they were presented in three different ultrasound modes: A, B, and M. Comparing the

experimental and modeled data, it was found that in the A-mode the echoes from the lumen-intima and media-adventitia boundaries are clearly visible in both cases. In B-mode cases, the artery walls are visible as a double-line pattern. In summary, the artery model has a structure like an *in vivo* arterial wall has (see Figure 3.7 a and b).

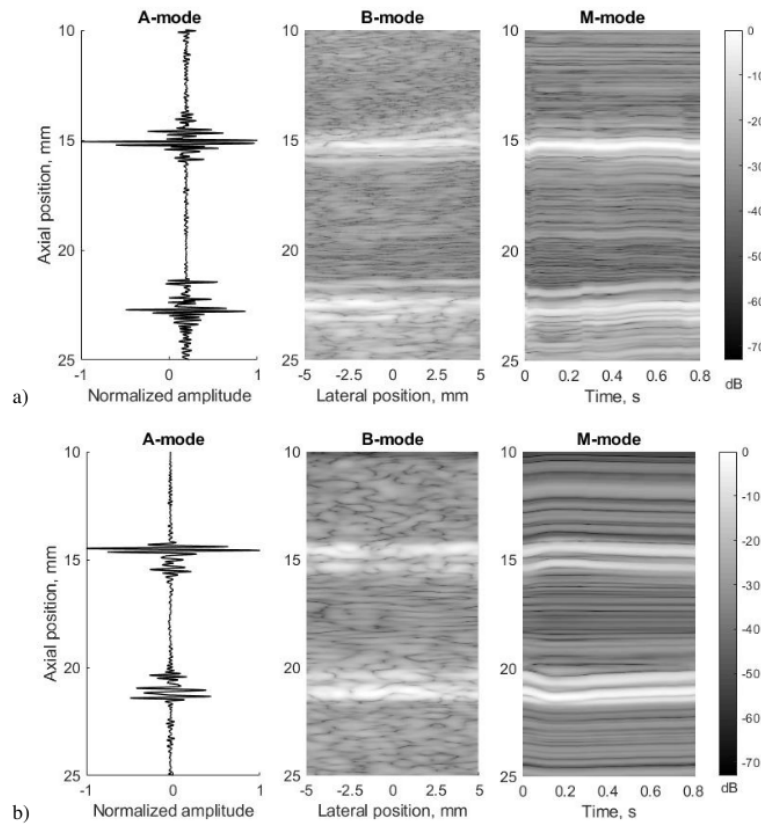


Figure 3.7. Comparison of RF signals form (A-mode, frame f_l , lateral position 0 mm), whole image (B-mode, frame f_l), and movement over time (M-mode) according to the artery: a) *in vivo* (23 years old female, motion amplitude were not normalized) and b) *in silico* model data (23 years old female, motion amplitude were normalized to 1 mm)

It is worth remembering, that for simulations, the amplitude of the preselected period of longitudinal and radial motion signals (see Figure 2.20 c) was normalized taking peak-to-peak amplitude. In the example below (see Figure 3.7 b), radial and longitudinal motions peak-to-peak amplitude was 1 mm. In the *in vivo* case, radial and

longitudinal motions peak-to-peak amplitude of the preselected period (see Figure 2.8 e) was not changed and were $827 \mu\text{m}$ and $982 \mu\text{m}$ accordingly. The time axis was not normalized. In M-mode, the movement of the artery model according to the radial motion signal is seen (see Figure 2.8 e). Both the proximal and distal walls of the artery move according to the same pattern, only in the opposite direction (see Figure 3.7 b), and the motion amplitude of the distal and proximal walls is radial motion divided by two as simulated. In the *in vivo* case, not so uniform motion pattern of both walls is seen (see Figure 3.7 a). Likely, the ultrasound transducer was not perfectly positioned at the center of the artery and 90-degree angle into the artery at the time of registration. It is also not ruled out that the ultrasound transducer was pressed into the neck during recording, which prevented the proximal wall of the artery from moving in the same pattern as the distal one.

Figure 3.8 depicts the B-mode images of the artery model at frames f_i and f_o , where $f_o = f_i + 0.15 \text{ s}$ and $f_i = 0 \text{ s}$ (frame rate was 52 frames per second). There is a $1000 \mu\text{m}$ motion difference between proximal and distal walls, and the difference between B-mode images could be seen. However, a detailed analysis of RF signals at frames f_i and f_o shows a clear difference (see Figure 3.9).

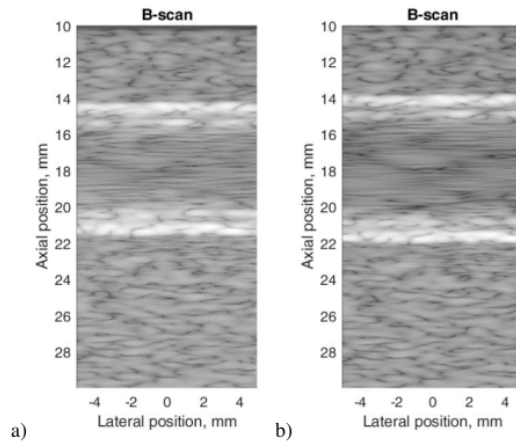


Figure 3.8. Simulated B-mode images of artery model at certain frames of the sequence: a) f_i and b) f_o . 23 years old male, motion amplitude were normalized to 1 mm

A calculated radial displacement of the virtually scanned artery model at 3.91 mm and 5.1 mm away from the artery model center between frames f_i and f_o is $400 \mu\text{m}$ and $330 \mu\text{m}$ (as observed in Figure 3.9), though displacement at those depths expected to be $390 \mu\text{m}$ and $320 \mu\text{m}$ correspondingly (expectation was based on the half radial motion $500 \mu\text{m}$ between these time instances and the theoretical healthy volunteer radial motion decrement 0.78 and 0.64 at selected depths accordingly (see Figure 2.22).

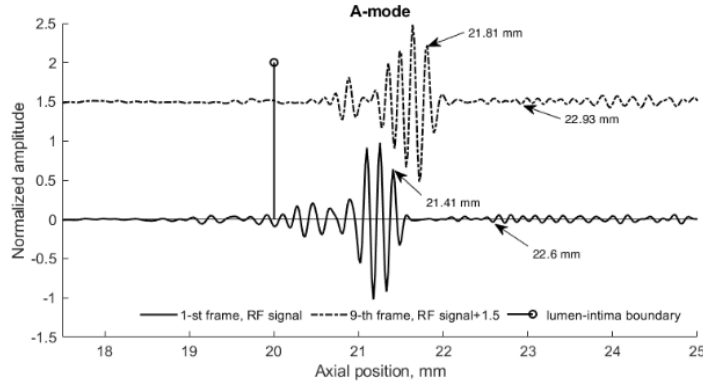


Figure 3.9. RF signals simulated by the model of a pulsating artery at frames f_1 and f_9 . Distal wall and surrounding tissues scattered RF signals (the artery center at 17.5 mm) depicting the radial wall displacement and its decrease in surrounding tissues. 23 years old male, motion amplitude was normalized to 1 mm

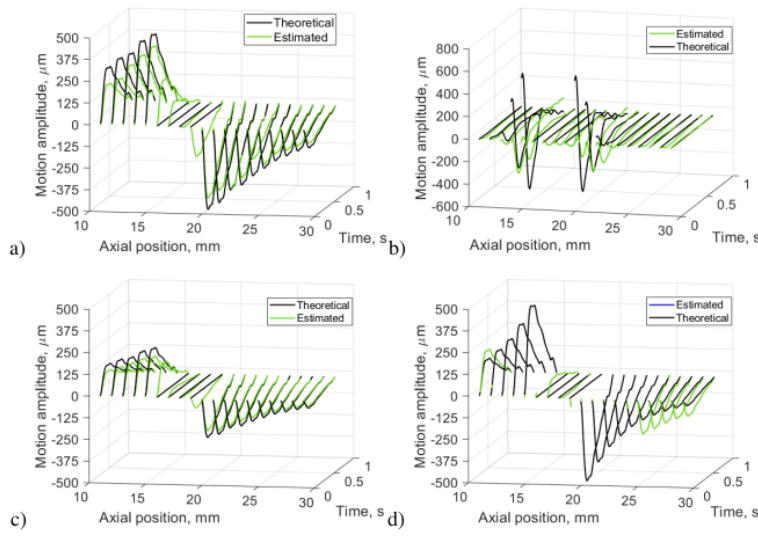


Figure 3.10. Motion of both proximal and distal wall of the artery and surrounding tissues: a) 1 mm peak-to-peak radial motion, estimated using OpenOpticalFlow, b) 1 mm peak-to-peak longitudinal motion, estimated using OpenOpticalFlow, c) 0.5 mm peak-to-peak radial motion, estimated using 1D cross-correlation, d) 0.5 mm peak-to-peak radial motion, estimated using 1D cross-correlation. 23 years old male

For comparison, results using 1D cross-correlation and OpenOpticalFlow algorithms were presented (see Figure 3.10). Further analysis of radial and longitudinal motions showed that the movements estimated from simulated scanning frames match the initially defined motion pattern used for modeling. Nonetheless, the 1D cross-correlation method is not capable to detect large inter-frame motion (higher than a quarter of the wavelength of the ultrasound echo data) due to “peak hopping” errors that result in discontinuity of radial motion signals (see Figure 3.10 d).

Dynamic 3D artery model has similar radial and longitudinal motions patterns, amplitude, and decrement into the tissue as theoretically predefined motions even though estimated motions amplitude is negligibly lower than a theoretical one. Here is important to note that motion estimation from simulated US RF signals is highly dependent on the estimation algorithm applied. Therefore, simulation errors cannot be attributed to the simulation method only.

Discussion.

The echoscopy simulation shows that the artery model represents an A, B and M-mode image structure like an *in vivo* artery wall has. The evaluated simultaneous radial and longitudinal motion of the virtually scanned 3D structure over a single pulse is visually almost indistinguishable from generated motion pattern.

Besides, a radial and longitudinal motion slope away from the artery lumen or lumen-*intima* boundary was modeled. These results go beyond previous reports ^[42,46] and show that the artery wall structure could be modeled in detail together with longitudinal and radial artery wall motion signal shape and amplitude. Because there is no conclusive information about the mathematical modeling of longitudinal motion, this motion in the model was defined according to data evaluated from *in vivo* experiments.

The limitation of this study is not verified *in vivo* the slope of the longitudinal and radial motion deep into the tissue. For this moment, the slope is described by an exponential function, which parameters were chosen according to Stoitsis et al ^[46]. Cinthio ^[21] evaluated such exponential function parameters from *in vivo* data, but in a limited study and only from a healthy subject. For a more accurate evaluation of slope, the artery diameter also should be concerned. With aging, arterial stiffness increase ^[168], so motion slope should be evaluated not only in healthy, but also in atherosclerotic patients to model different arterial stiffness.

The artery model, which uses both shape and amplitude of radial and longitudinal motion signals from real *in vivo* data has not been proposed in previous studies. Further investigations are necessary to evaluate and confirm the author's results ^[46] of the spatial dependence of radial and longitudinal motions *in vivo*.

3.3. Investigation results of methods for radial and longitudinal motion detection accuracy

For motion detection, two methods were chosen: 1. 1D cross-correlation for detection of radial motion and 2. OpenOpticalFlow for both radial and longitudinal motion detection. The difference between these two approaches is obvious, i.e.

OpenOpticalFlow deals better with large radial motion rather than 1D cross-correlation (see Figure 3.11 a and b). Inter-frame displacements are accumulated relative to the first frame resulting in motion. White areas in the motion map (see Figure 3.11 a) correspond to the regions where inter-frame motion is higher than a quarter of the wavelength and exist probability to identify false correlation peak resulting in large tracking errors that are known as “peak hopping” errors. OpenOpticalFlow method is not faced with this issue, the motion map is smooth, without any discontinuity.

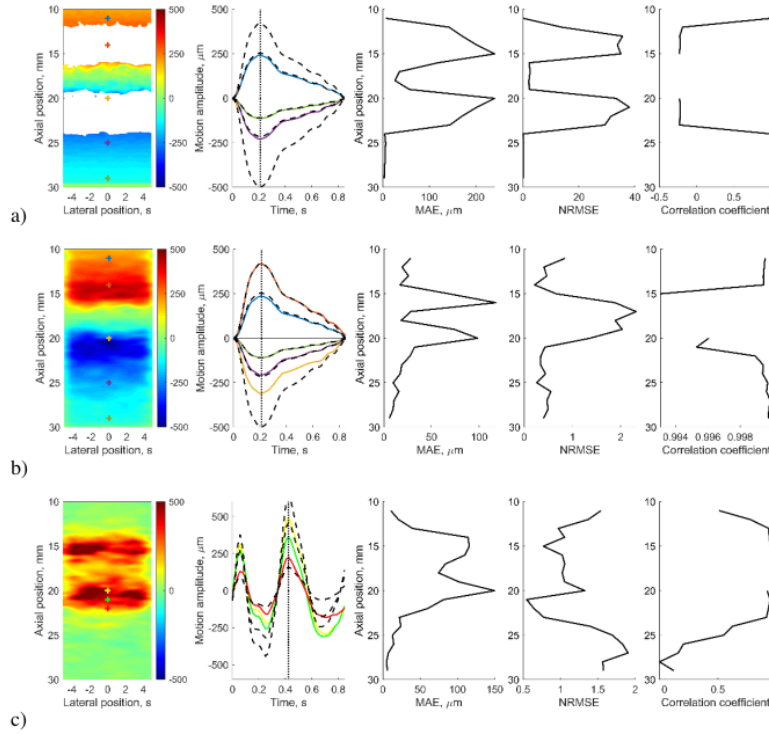


Figure 3.11. Investigation results of methods for radial and longitudinal motion detection accuracy: a) radial motion, 1D cross-correlation, b) radial motion, OpenOpticalFlow, and c) longitudinal motion, OpenOpticalFlow. Radial motion map in scanning plane with preselected points from where the estimated motion is taken and depicted together with theoretical. Here, the vertical dashed line corresponds to the time moment of maximal theoretical displacement. At this time moment, a motion map is depicted. Finally, MAE, NRMSE, and Pearson correlation coefficient are evaluated in the midline of the motion map at the different axial positions, i.e. starting from 11 mm every 1 mm to 29 mm. 27 years old female, theoretical motion peak-to-peak amplitude is 1 mm

Large MAE values exceeding $150\ \mu\text{m}$ (modelled motion amplitude was $1\ \text{mm}$) are seen at the boundary of the artery wall and lumen when longitudinal motion was detected with the OpenOpticalFlow method. This may be explained by that longitudinal motion mainly are exhibited in *intima-media* complex, which thickness is only $0.7\ \text{mm}$ what causes difficulties in the detection of longitudinal motion in such small ROI. Nonetheless, the correlation coefficient shows the higher similarity between the estimated and theoretical motion signals at the artery wall (from $14\ \text{mm}$ to $22\ \text{mm}$ according to axial position) rather than in surrounding tissues (from $10\ \text{mm}$ to $14\ \text{mm}$ and from $22\ \text{mm}$ to $30\ \text{mm}$ according to axial position) where the relationship between the two motion signals is pure or does not exist.

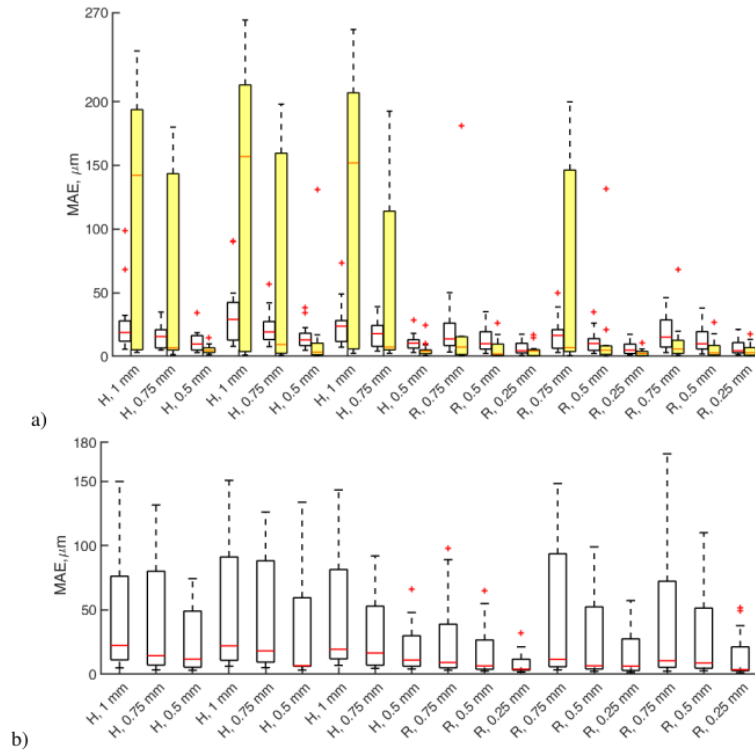


Figure 3.12. Box plots of MAE of estimated and theoretical motion signals evaluated in the middle scanning line starting from $11\ \text{mm}$ every $1\ \text{mm}$ to $29\ \text{mm}$: a) radial motion detection, b) longitudinal motion detection. White and yellow boxes correspond to 1D cross-correlation and OpenOpticalFlow methods accordingly ($n=19$). Median values are shown as a horizontal red line. Whiskers represent the minimum and maximum values. Outliers are indicated by red +. H – healthy volunteer, R – at-risk patient

Further analysis of MAE showed that great errors occur when the 1D cross-correlation method was used for radial motion detection and peak-to-peak motion amplitude is equal to or higher than 0.75 mm (see Figure 3.12 a). Once again, this is caused by the fact that inter-frame motion was higher than a quarter of the wavelength and exist probability to identify false correlation peak resulting in large tracking errors that are known as “peak hopping” errors. Nonetheless, for high values of peak-to-peak radial motion, median values of MAE were found to be lower than 25 μm when the OpenOpticalFlow method was investigated. As may be seen below (see Figure 3.12 b), median values of MAE were found to be lower than 25 μm when the OpenOpticalFlow method was investigated for a capability to detect longitudinal motion. Also, it could be seen that the average values of MAE are about 50 μm or lower and have a tendency to decrease when the detected motion amplitude is decreasing.

Discussion.

The results demonstrate that the variety of accuracy evaluation parameters for radial and longitudinal motions detection are capable to access not only error but also evaluate dissimilarities between estimated and theoretical motion signals.

Nonetheless, the accuracy in motion tracking was examined by others and presented in APPENDIX A1. Some authors state, that no quantitative evaluation of accuracy was introduced in their studies, while others use qualitative evaluation only. In contrast to these reports in the literature, there were studies where accuracy evaluation criteria mainly were average absolute error. As stated by Zahnd *et al.*^[19], the average absolute error of longitudinal motion was $20 \pm 19 \mu\text{m}$, while radial motion – $84 \pm 107 \mu\text{m}$ using Klamann-based block matching method for motion detection. Later, Zahnd *et al.*^[101] proposed dynamic block-matching approach for motion tracking and stated that the average absolute error of longitudinal motion was $150 \pm 163 \mu\text{m}$. In accordance with previous studies’ results, the average values of MAE of longitudinal motion lie between the results of Zahnd *et al.*^[19,101]. Also, it is worth mentioning, that only a few researchers groups incorporated *in silico* experiments in their studies^[90,92]. Most of the accuracy evaluation studies are based on *in vivo* studies. Here estimated motion was compared with manual tracing results which were performed by experienced ultrasound physicians and considered as the ground truth. Therefore, motion detection errors cannot be attributed to the motion detection method only. Errors can also occur due to manual tracing. Still, motion detection approaches should be carefully investigated *in silico* and *in vitro* before testing *in vivo*.

The main limitation of the accuracy evaluation of motion detection is that motion tracking approaches were not specialized to a specific motion, i.e. longitudinal motion, which demands particular solutions for motion tracking as longitudinal motion exists mainly in *intima-media* complex and is negligible in surrounding tissues.

Future investigations *in vitro* and *in vivo* are necessary to further investigate methods for motion detection and suggest even more reliable approaches for that purpose.

3.4. Comparison of theoretical and estimated slope profiles of radial and longitudinal motions

The results show the spatial dependence of radial and longitudinal motions (see Figure 3.13).

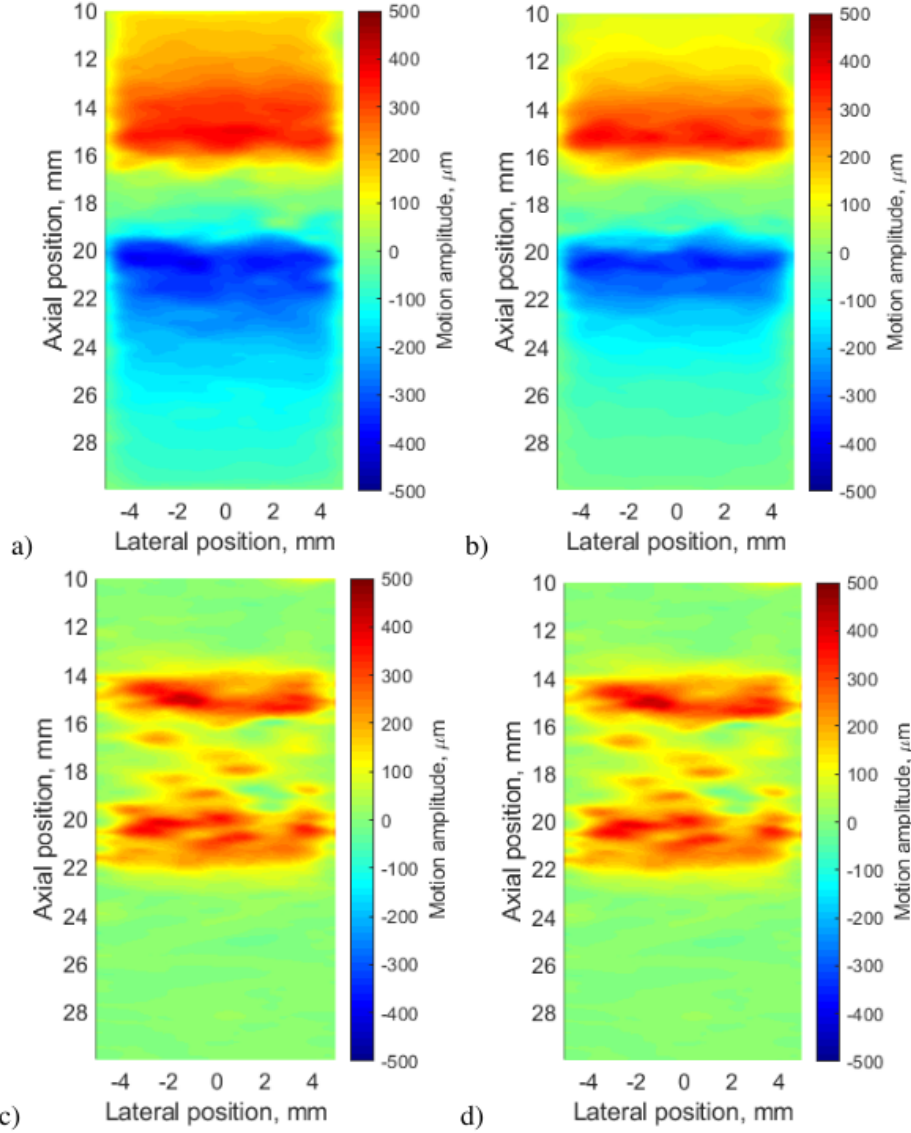


Figure 3.13. Motion maps of both proximal and distal wall of the artery and surrounding tissues estimated using OpenOpticalFlow: a) radial motion and its slope deep into the tissue (motion amplitude 0.75 mm, $b_1=0.17$, 27 years old female), b) radial motion and its slope deep into the tissue (motion amplitude 0.75 mm, $b_1=0.26$, 56 years old male), c) longitudinal motion and its slope deep into the tissue (motion amplitude 0.75 mm, $b_2=1.08$, 27 years old female), d) radial motion and its slope deep into the tissue (motion amplitude 0.75 mm, $b_2=1.62$, 56 years old male)

The amplitude of radial motion is greatest at the surface of the artery (16 and 20 mm) and decreases exponentially into the surrounding tissues; the amplitude of longitudinal motion is greatest at the artery wall (approximately at 16 mm and 20 mm), decreases significantly and longitudinal motion amplitude is negligible in the surrounding tissues. The apparent comparison between healthy volunteer (see Figure 3.13 a and c) and at-risk patient (see Figure 3.13 b and d) radial and longitudinal motions slope deep into the tissue is seen: more abrupt radial and longitudinal motions slope is observed in the at-risk patient rather than in healthy volunteer.

Figure 3.14 depicts the spatial dependence comparison of radial and longitudinal motions of the distal wall of the artery and surrounding tissues between theoretical and estimated values.

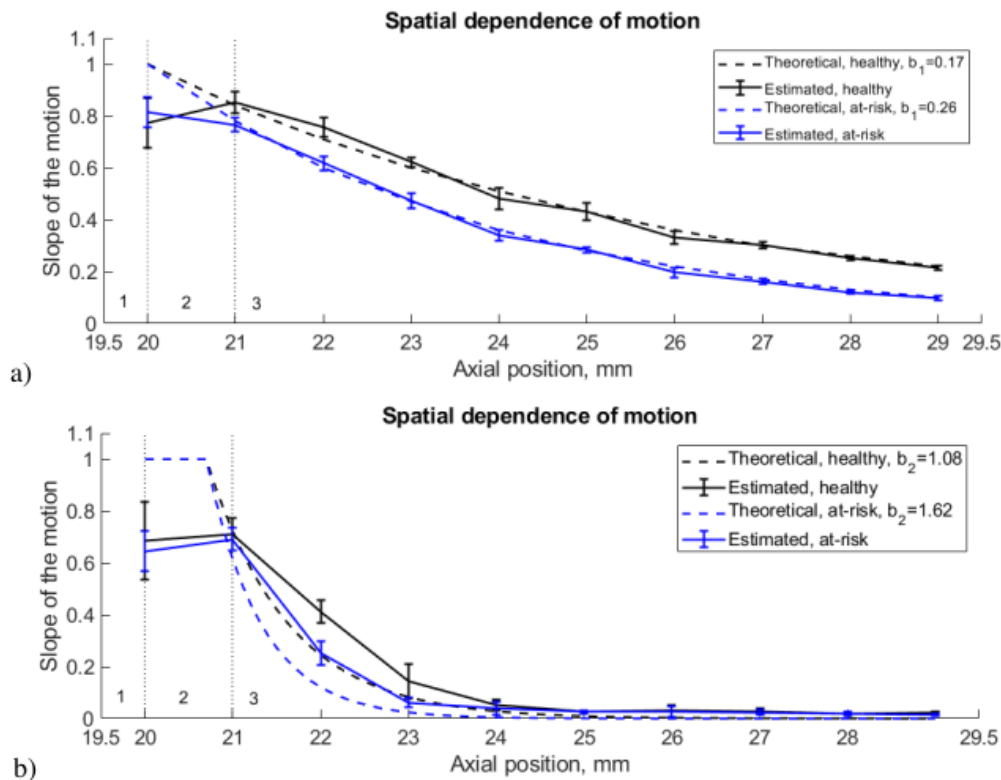


Figure 3.14. Spatial dependence comparison of radial and longitudinal motions of distal wall of the artery and surrounding tissues between theoretical values and estimated from OpenOpticalFlow algorithm of envelopes of simulated RF signals: a) radial motion slope in the artery wall and deep into the tissue, b) longitudinal motion slope in the artery wall and deep into the tissue. Error bars represent the mean ($n=9$) and standard deviation ($n=9$) of estimated values of slope profiles for healthy volunteers and at-risk patients groups for every preselected axial position. Numbers 1, 2, and 3 in the graph corresponds to the lumen, artery wall, and surrounding tissues respectively

There is a correlation between theoretical and estimated slope profiles of radial motion in the surrounding tissues. However, such a good coincidence is not seen in

the artery wall. This could be due to the insufficient number of preselected points in the artery wall where the slope profile was evaluated, i.e. only two axial positions at the boundary of the artery wall define the motion slope profile in the artery wall. The same number of preselected points was in the longitudinal motion slope profile definition in the artery wall. Here, even more discrepancy between theoretical and estimated slope profiles is seen (see Figure 3.14 b). What is more, estimated profiles of longitudinal motion had a bias relative to theoretical ones in the surrounding tissues. Despite the mismatch between theoretical and estimated profiles, especially in the case of longitudinal motion, it is capable to differentiate healthy volunteers and at-risk patients according to slope profiles of radial and longitudinal motions.

Discussion.

The results demonstrate that the variety of slope profiles of radial and longitudinal motions that defines different elasticity tissues may be used for the differentiation of healthy volunteers and at-risk patients.

Nonetheless, a radial and longitudinal motion slope in the artery wall and surrounding tissues was modeled by others ^[61], no artery motion maps or slope profiles were not investigated in detail. Recently, several authors ^[30,31] have proposed motion maps of liver and brain tissues. But, despite the clear difference between healthy and diseased tissues according to motion amplitude, motion slope was not thoroughly explored. The results obtained in ^[169] suggest that radial motion in tissue-mimicking phantoms with predicted Young modulus 10 kPa and 7kPa results in different motion amplitudes at the same axial position. Summing up, it was found that motion is dependent on phantom elasticity, i.e. with the increase of phantom stiffness decrease motion amplitude.

The main limitation of the modeling result is that the slopes of radial and longitudinal motions were modeled by a limited study and only from a healthy subject ^[21] while the slope for at-risk patients was selected at random, i.e. 1.5 times bigger than for healthy volunteers.

For a more accurate evaluation of slope, the artery diameter also should be concerned. With aging, arterial stiffness increase ^[168], and motion slope should be evaluated not only in healthy but also in atherosclerotic patients to model different arterial stiffness.

The tissue differentiation according to slope profiles of radial and longitudinal motions has not been proposed in previous studies. Further investigations of motion slope dependence of tissue elasticity *in silico* and *in vivo* are necessary.

3.5. In-vivo results of the parametrization of radial motion signals

Time and frequency domain parameters that were used for the parametrization of radial motion signals of healthy volunteers and at-risk patients were used as inputs for plotting ROC curves that were used to evaluate the performance of binary classification algorithms. MATLAB R2018b (The MathWorks, Inc., Natick, USA) was used to perform this analysis.

From now on, ROC curves are provided to evaluate diagnostic performance of a proposed time and frequency domain parameters to discriminate diseased cases from normal ones. Figure 3.15 a) demonstrates that the heart rate parameters has poor ability to distinguish healthy volunteers from at-risk patients as AUC is 0.63 (see Figure 3.15 a). Nonetheless, radial motion displacement, velocity and acceleration parameters has some predictive power as AUC is about 0.8 (see Figure 3.15 b, c and d).

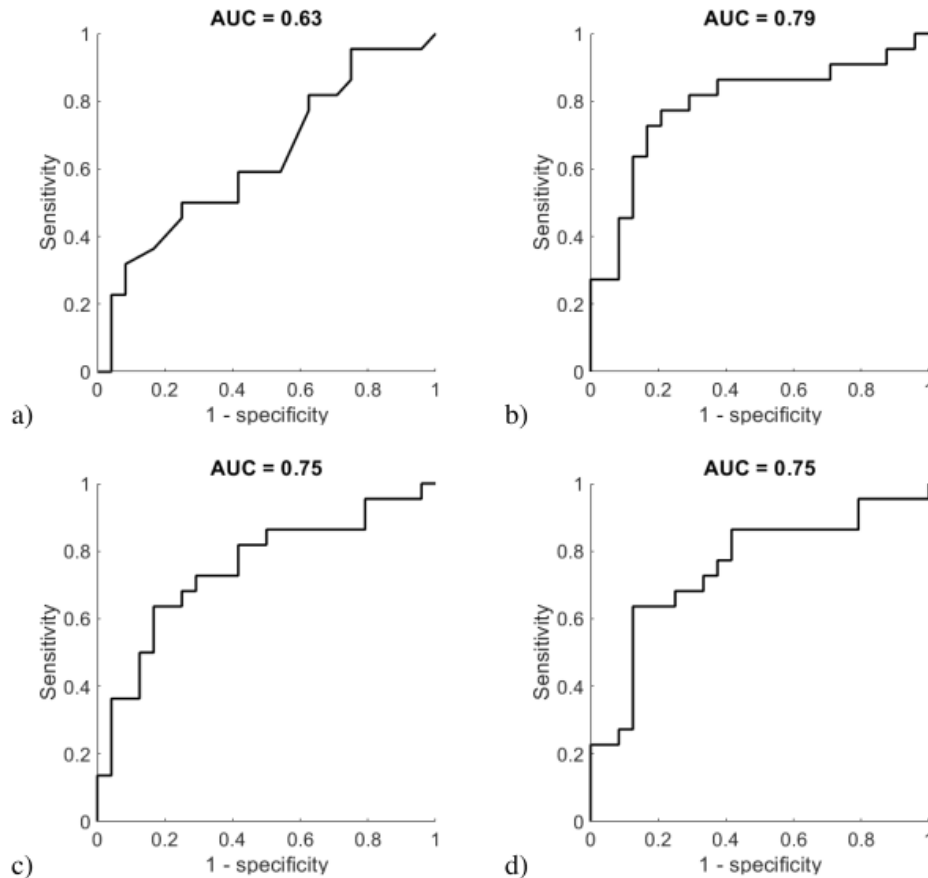


Figure 3.15. ROC curves of a) heart rate, b) radial motion displacement, c) velocity and d) acceleration proposed to compare their diagnostic performance in detecting atherosclerosis.

Comparing ability of frequency domain parameters (see Figure 3.16) to detect at-risk patients, it was found that spectral centroid and spectral spread has fair ability to diagnose patients with and without the atherosclerosis as AUC of the ROC curve of those parameters is about 0.7. ROC curves of spectral skewness, and spectral kurtosis shown that these parameters has some predictive power to discriminate diseased cases from normal ones, as AUC is 0.79 in both cases.

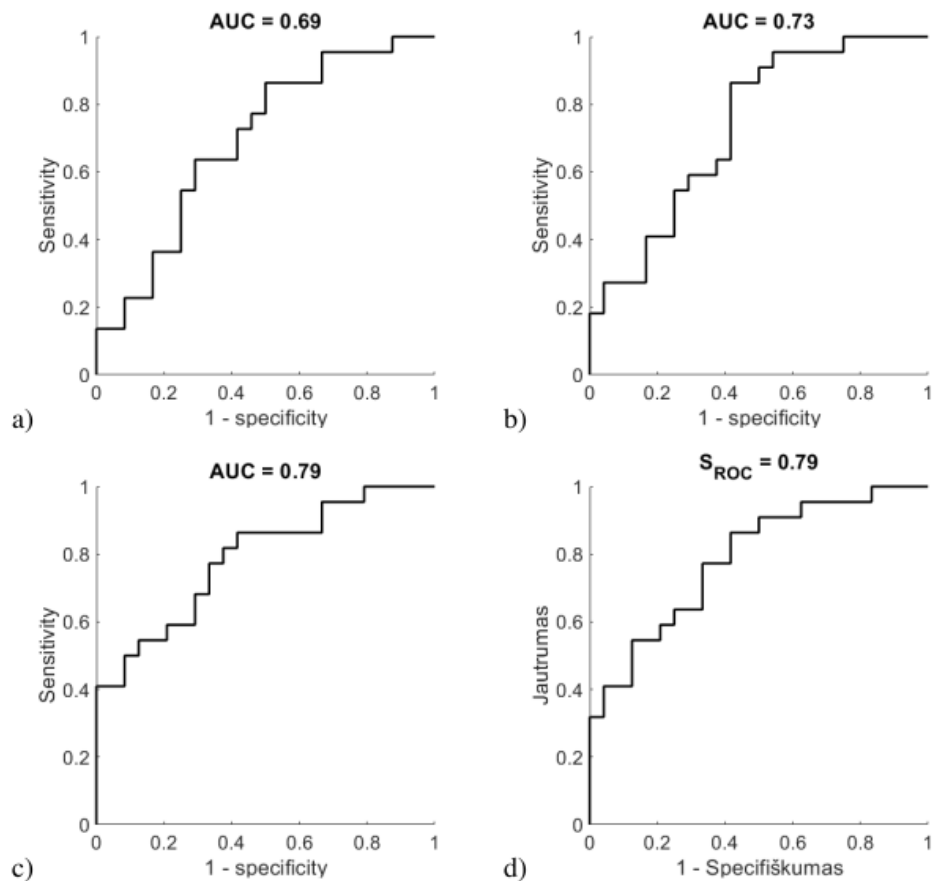


Figure 3.16. ROC curves of a) spectral centroid, b) spectral spread, c) spectral skewness and d) spectral kurtosis proposed to compare their diagnostic performance in detecting atherosclerosis.

Table 3.2. Diagnostic value of time and frequency domain parameters in distinguishing healthy volunteers from at-risk patients

		Sensitivity	Specificity
Time domain parameters	Heart rate, BPM	0.50	0.63
	Displacement, μm	0.77	0.79
	Velocity, $\mu\text{m/s}$	0.64	0.88
	Acceleration, $\mu\text{m/s}^2$	0.73	0.71
Frequency domain parameters	Spectral centroid, Hz	0.64	0.71
	Spectral spread	0.86	0.58
	Spectral skewness	0.77	0.67
	Spectral kurtosis	0.77	0.67

The highest sensitivity of the proposed time and frequency domain parameters has displacement, *i.e.* 0.77 and spectral spread, *i.e.* 0.86. The velocity and spectral

centroid assigned as parameters with the highest specificity resulting 0.88 and 0.71 correspondingly (see Table 3.2).

Discussion.

The results indicate that the proposed parametrization of radial motion signals is efficient for the differentiation of healthy volunteers and at-risk patients when radial motion displacement, velocity and acceleration spectral centroid, spectral spread, spectral skewness and spectral kurtosis parameters are used.

The results of motion parametrization in the time domain build on existing evidence of ^[21,164,165] that healthy volunteers could be discriminated from at-risk patients using displacement parameter. However, most of the previous studies do not take into account frequency domain parameters.

The current *in vivo* study was limited by CCA motion detection and parametrization only in the radial direction. Longitudinal motion evaluation requires a specific approach dealing with three challenges described by Zahnd ^[19]. Firstly there exist low contrast in the longitudinal direction due to the anatomical structure of the artery (*intima-media* complex is characterized by homogeneous profile, i.e. small variation of the image gray level along the wall). The second challenge is a small *intima-media* layer thickness of about 0.5 mm. Finally, speckle decorrelation, i.e. the degrading phenomenon caused by out-of-plane movements, low echoes, tissue deformation, and movement artifacts, must be deal with.

Future investigations are necessary to validate the conclusions that can be drawn from this study. New frequency domain parameters could be investigated in the larger study population in the future to distinguish healthy subjects from at-risk patients.

3.6. Conclusions of the 3rd chapter

1. The result shows a good agreement of digital simulation with the physical one. FWHM estimates in the axial direction are according to practical estimates with a discrepancy of less than 12 %. Simulation results of an axial view of normalized PSF coincide better with the experiment than lateral one, which is supposedly influenced by difficulties to account in simulation parameters of apodization, focusing, and other ultrasound beamforming measures taken by the scanner. The FWHM estimates in the lateral direction are according to practical estimates with a discrepancy of less than 16 %.
2. The echoscopy simulation shows that the artery model represents an A, B and M-mode image structure like an *in vivo* artery wall has. The evaluated simultaneous radial and longitudinal motion of the virtually scanned 3D structure over a single pulse is visually almost indistinguishable from generated motion pattern.
3. The results demonstrate that the variety of accuracy evaluation parameters for radial and longitudinal motions detection are capable to access not only error but also evaluate dissimilarities between estimated and theoretical motion signals.

4. The results demonstrate that the variety of slope profiles of radial and longitudinal motions that defines different elasticity tissues may be used for the differentiation of healthy volunteers and at-risk patients.
5. The results indicate that the proposed parametrization of radial motion signals is efficient for the differentiation of healthy volunteers and at-risk patients, i.e. proposed parameters has diagnostic ability to diagnose patients with and without the atherosclerosis.

4. GENERAL CONCLUSIONS

1. Literature review has shown that atherosclerosis is a chronic disease of the arterial wall that is not noticeable until the atherosclerotic plaques build up. However, it has been proven that significant changes in the mechanical properties of arterial walls (i.e., longitudinal and radial motion of the arterial wall) occur much earlier than anatomical changes (i.e., IMT) appear. Clinical investigations have linked longitudinal motion of the CCA to risk factors and CVDs and have shown a relationship between arterial stiffness, CVDs, and the decrease in longitudinal motion. A number of motion tracking algorithms are proposed for radial and longitudinal motion detection. Some of them are freely or commercially available for the investigation of longitudinal motion. But none of them are not applied in clinical practice these days. Firstly these methods should be carefully investigated before wide usage.
2. Virtual scanning simulation adequate to physical ultrasonic scanning was developed. Digital scanning shows a good agreement with the physical one: FWHM estimates of PSF in the axial and lateral directions are according to practical estimates with a discrepancy of less than 12 % and 16 % correspondingly. The FWHM of the beam in the elevation plane was 1.21 mm in physical echoscopy while in digital elevation phantom simulation it was 1.38 mm.
3. A 3D artery model capable to reproduce the biomechanical behavior of human CCA for simulation of US RF signals was created. The echoscopy simulation shows that the artery model represents an A, B and M-mode image structure like an *in vivo* artery wall has. The evaluated simultaneous radial and longitudinal motion of the virtually scanned 3D structure over a single pulse is visually almost indistinguishable from generated motion pattern.
4. The accuracy of the proposed motion detection algorithms using simulated CCA US RF signals was investigated. The results demonstrate that the variety of accuracy evaluation parameters for radial and longitudinal motions detection are capable to access not only error but also evaluate dissimilarities between estimated and theoretical motion signals. Median values of MAE were found to be lower than 25 μm when the OpenOpticalFlow method was investigated for both radial and longitudinal motion detection.
5. The capability to differentiate arteries by motion slope profiles was investigated. There is a good match between theoretical and estimated slope profiles of radial motion in the surrounding tissues, while the estimated profiles of longitudinal motion had a bias relative to theoretical ones in the surrounding tissues. The results demonstrate that the variety of slope profiles of radial and longitudinal motions that defines different elasticity tissues may be used for the differentiation of healthy volunteers and at-risk patients.
6. The US RF data from healthy volunteers and patients at increased risk of CVD group was collected, motion parameters of two different populations were calculated and those parameters diagnostic ability to diagnose patients with

and without the atherosclerosis was evaluated. The highest sensitivity of the proposed time and frequency domain parameters has displacement, *i.e.* 0.77 and spectral spread, *i.e.* 0.86. The velocity and spectral centroid assigned as parameters with the highest specificity resulting 0.88 and 0.71 correspondingly.

SUMMARY

Ivadas

Širdies ir kraujagyslių ligos (ŠKL) yra pagrindinė žmogaus mirties priežastis visame pasaulyje. Kasmet nuo šių ligų miršta vis daugiau žmonių nei nuo kitų ligų. 2019 metais, metais, kada paskutinį kartą buvo skaičiuota pasaulio statistika, pasaulyje nuo ŠKL mirė 18,6 milijono žmonių, kas atitinka 17,1 % padidėjimą per pastarąjį dešimtmetį ^[1]. 42,1 % mirčių pagrindinė priežastis, priskiriama ŠKL, buvo koronarinė širdies liga ^[1], o aterosklerozė yra pagrindinė šios ligos priežastis. Prognozuojama, kad iki 2030 metų mirtys nuo ŠKL pasaulyje pasieks 23,6 milijono ^[2]. Insultas, vienas iš kelių galimų ŠKL pasėkmių, yra antroji mirtingumo ir šeštoji ilgalaikės negalios priežastis ^[3,4]. Todėl širdies ir kraujagyslių sistemos ligų prognozavimas efektyviam pacientų gydymui yra pagrindinė visuomenės sveikatos problema ^[5,6,7,8,9]. Aterosklerozė, užslėptas, patologinis mechanizmas, yra lėtinė ir sisteminė kraujagyslių liga, dažnai vadinama „tyliuoju žudiku“, nes jo progresavimas ir raida yra nepaprastai sudėtingi ir gana nenusipėjami, lemiantis nepaprastai daug mirtimi pasibaigiančių atvejų, įvykusių be jokio įspėjamojo ženklo ^[10]. Apskritai, ateroskleroziniai pažeidimai ilgainiui yra nepastebimi, tačiau bendrieji šios ligos požymiai išryškėja tik prasidėjus komplikacijoms: *intima-media* komplekso sustorėjimas, spindžio susiaurėjimas ar trombozė ir (arba) elastingumo sumažėjimas ^[11]. Aterosklerozė sukelia periferinių arterijų ligas, insultą, širdies priepuolius, ir visa tai vadinama ŠKL, o miokardo infarktas ir insultas apibūdinami kaip paskutinė aterosklerozės stadija ^[12].

Arterijos standumas yra nepriklausomas širdies ir kraujagyslių ligų požymis analizuojamas siekiant įvertinti ŠKL riziką ^[13,14,15]. Klinikinėje praktikoje dažniausiai naudojami rizikos žymenys arterijos standumo vertinimui yra *intima-media* komplekso storis, pulso bangos greitis ir skersinis išsitempimas (*angl.* cross-sectional distensibility) ^[16,17,18,19]. Deja, bet šių tradicinių rizikos žymenų, kaip atrankos testo, klinikinis potencialas tebėra ribotas ^[20]. Sunku įvertinti ŠKL riziką pacientams iki 50 metų, ypač jei nėra specifinių, individualių ŠKL rizikos veiksnių ar anamnezės. Todėl yra sudėtinga įvertinti ligos išsivystymo tikimybę ir prireikus pradėti gydymą vaistais ^[13].

Nepaisant to yra įrodyta, kad mechaniniai pokyčiai, t.y. išilginis ir skersinis arterijos sienelės judėjimas, atsiranda daug anksčiau nei reikšmingi arterijos sienelės anatomiciniai pokyčiai, t.y. *intima-media* komplekso sustorėjimas ^[12]. Skersinis judėjimas yra parametras apibūdinantis arterijų sienelių mechanines savybes ir pastaraisiais metais buvo plačiai ištirtas. Tampantis informatyviu, neinvaziniu parametru, skersinis judesys padeda ištirti ŠKL bei nustatyti arterijų sienelių elastingumą. Išilginis judesys tokio pripažinimo nesulaukė, priešingai nei skersinis arterijos sienelės judėjimas. Lyginant su skersiniu judesiu buvo manoma, kad išilginis judesys širdies ciklo metu yra nežymus. Tačiau naudojant šiuolaikinius ultragarsinius skenerius buvo pastebėta, kad širdies ciklo metu *intima-media* kompleksas juda ne tik skersine, bet ir išilgine kryptimi ^[21,22]. Taip pat buvo pastebėta, kad skersinio ir išilginio arterijos sienelės judesio amplitudės yra vienodos ir siekia maždaug vieną

milimetrą ^[23]. Be to, klinikiniai tyrimai susiejo bendrosios miego arterijos išilginį judesį su rizikos veiksniais ir ŠKL ^[24,25]. Ankstesni tyrimai parodė ryšį tarp arterijos standumo, ŠKL ir išilginio judesio sumažėjimo ^[12]. Nors ir išilginio judesio amplitudė yra susijusi su ŠKL, veiksniai lemiantys išilginio judesio fazes lieka nežinomi ^[16].

ŠKL rizikos vertinimo kontekste, arterijos audinio judėjimas širdies ciklo metu yra svarbus, nes mechaninė deformacija atspindi kraujagyslių elastingumą ir yra atvirkščiai susijusi su arterijos standumu, kaip nepriklausomu sergamumo ir mirtingumo rodikliu ^[26]. Arterijos audinio judėjimas širdies ciklo metu susideda iš skersinio (arterijos sienelės judėjimo statmeno kraujotakai), išilginio (*intima-media* komplekso judesio lygiagrečiai kraujo tėkmei) judesių ir žiedinio įtempio. Taikant keletą judesio sekimo metodų, arterinio audinio judėjimas iš ultragarsinių radiodažninių signalų ar vaizdų sekų buvo išanalizuotas ir apibendrintas Rizi ir kt. ^[27].

Šiuo metu esami ultragarsinės elastografijos metodai galimi suskirstyti į dvi pagrindines grupes pagal išmatuojamą fizinį dydį: 1) įtempių vizualizavimas, 2) šlyties bangos vizualizavimas ^[28]. Abi šios metodų grupės naudoja išorinį spaudimo šaltinį. Nepaisant to, vidinis deformacijų šaltinis arba taip vadinamas endogeninis judesys, kurį sukelia širdies plakimas ir kraujagyslių veikla, gali būti naudojamas elastingumui matuoti ^[29,30,31].

Metodai, pagrįsti endogeniniu judesio detektavimu, klinikinėje praktikoje šiuo metu nėra taikomi. Pirmą, šie metodai turėtų būti kruopščiai išstudijuoti ir ištirti. Dėl to būtų galima naudoti kompiuterinį ultragarsinį vizualizavimą ultragarsinių radiodažninių signalų ar B režimo vaizdų simuliacijai naudojant tam skirtus algoritmus. Populiariausi simuliacijos programinės įrangos paketai ^[32,33,34] yra CREANUIS ^[35] (paremtas Chochlovo-Zabolotskajos-Kuznecovo lygtimi), skirtas netiesiniam sklidimui ir harmoninio vizualizavimo simuliacijai ir Field II ^[36] (pagrįstas Huygenso principu ir hibridiniu skaitmeniniu-analitiniu metodu) kuris įgijo platų pritaikomumą nuo modelio paskelbimo 1991 metais ^[37] ir programinės įrangos paketo 1996 metais ^[38]. Field II populiarumas slypi dideliame lankstume pritaikyti šią simuliacijai skirtą programą plačiam spektrui keitiklių, spindulio formavimo pasirinkimo ir vaizdavimo pasirinkimo galimybių. Tai vis dar galingas ir besivystantis įrankis skirtas simuliuoti įvairiems skenavimo ir fokusavimo būdams, taip pat kaip ir visam echoskopijos mechanizmui, įskaitant sklaidą audiniuose ir organuose ^[39]. Nors yra daug Field II pritaikymų, aprašytų begalėje straipsnių, tačiau tik keliose publikacijose kalbama apie kiekybinį simuliacijos ir eksperimento palyginimą įvertinant neapibrėžtis ^[40,41].

Miego arterijos sienelės judesys buvo modeliuojamas daugelio autorių. Gemignani ir kt. ^[42] simulavo skersinį judesį kaip pjūklo funkciją, o Solomon ir kt. ^[43] kaip trikampio funkciją. Kaip skelbia Deng ir kt. ^[44], jie pasiūlė bendros miego arterijos geometrinį modelį, kur dinaminis atspindėtuvų modelis yra sukonstruojamas keičiant atspindėtuvų padėtį pagal sintezuotą pulso bangą. Pastaroji apskaičiuojama pagal kraujagyslės sienelės *in vivo* radiodažninius signalus naudojant 1D normalizuotos kryžminės koreliacijos algoritimą paremtą aido sekimu. Judėjimui skersine kryptimi, Hu ir kt. ^[45] pasiūlė izotropinį pulso modelį, kurio elastingumas

apibūdinamas ryšiu tarp skersinio poslinkio ir kraujo spaudimo. Tačiau nei viename iš ankstesnių tyrimų nenagrinėjamas išilginis arterijos judėjimas kartu su skersinio ir išilginio judesių slopimu gilyn į audinius. Tai padarė Stoitsis ir kt. ^[46] simuliuojant skersinį judėjimą kaip impulso funkciją, kurios parametrų vertės buvo nustatytos remiantis eksperimentais su *in vivo* duomenimis. Išilginis judesys buvo modeliuojamas kaip sinuso funkcija, nes nėra galutinės informacijos apie šio judesio matematinį modeliavimą. Remiantis panašiu *in vivo* tyrimu, taip pat buvo įtraukta skersinio ir išilginio judesių amplitudės erdvinė priklausomybė, kuri yra nepriklausoma nuo ašinės padėties.

Išilginis judesys, naujas, neinvazinis elastingumo matavimo parametras, vis dar nėra iki galo išnaudotas vertinant širdies ir kraujagyslių riziką, todėl jis turi daug potencialo. Be to, kompiuteriniam ultragarsiniam vizualizavimui turi būti atliekamas kiekybinis simuliacinio ir eksperimento palyginimas įvertinant neapibrėžtis prieš simuliuojant ultragarsinius radiodažnius signalus ar B skenavimo vaizdus, siekiant sukurti endogeninio judesio detektavimo metodus. Visi šie faktai kelia mokslinę-technologinę problemą ir darbo hipotezę.

Mokslinė-technologinė problema ir hipotezė

Metodai, paremti endogeniniu judesio detektavimu, šiuo metu nėra taikomi klinikinėje praktikoje. Pirmiausia, prieš pradedant šiuos metodus plačiai naudoti, jie turi praeiti tris „žingsnius“: 1) metodo testavimas *in silico*, siekiant suprasti, sukurti ir patikrinti metodą, 2) bandymai *in vitro*, siekiant optimizuoti, dar kartą patikrinti ir patvirtinti bandymų rezultatus, ir galiausiai 3) atestacija *in vivo*, siekiant patikslinti ir patvirtinti siūlomo metodo patikimumą. Dėl to, prieš *in vitro* ir *in vivo*, būtų galima naudoti kompiuterinį ultragarsinį vizualizavimą ultragarsinių radiodažnių signalų ar B režimo vaizdų simuliacijai naudojant tam skirtus algoritmus. Nėra pasiūlytas 3D arterijos modelis, gebantis visapusiškai atkurti žmogaus bendrosios miego arterijos biomechaninę elgseną ir būti tinkamas ultragarsinių radiodažnių signalų ir B režimo vaizdų sekų simuliacijai naudojant Field II programą.

Šios disertacijos darbinė hipotezė: audinių endogeniniai mikroposlinkiai, kuriuos daugiausia sukelia kraujo pulsacija kraujagyslėse, gali būti naudojami audinių elastingumo (ar standumo) įvertinimui ir ankstyvam aterosklerozės nustatymui.

Tyrimo objektas

Tyrimas pagrįstas bendrosios miego arterijos sienelės judesio simuliacinio algoritmo, skirtų ankstyvai aterosklerozės diagnostikai, kūrimu ir tyrimu.

Darbo tikslas

Šios daktaro disertacijos darbo tikslas yra sukurti ir ištirti ultragarsiniais radiodažniniais signalais paremtus algoritmus bendrosios miego arterijos sienelės judesių simuliacijai susijusiai su ankstyva aterosklerozės diagnostika.

Tikslui pasiekti iškelti darbo uždaviniai

1. Sukurti ir ištirti virtualų skenavimo simulavimą, atitinkantį fizinį ultragarsinį skenavimą.
2. Sukurti 3D arterijos modelį, gebantį atkurti žmogaus bendrosios miego arterijos biomechaninę elgseną ir tinkamą ultragarsinių radiodažninių signalų simuliacijai.
3. Ištirti ir įvertinti siūlomų judesio detektavimo algoritmų tikslumą naudojant simuliuotus bendrosios miego arterijos ultragarsinius radiodažninius signalus.
4. Ištirti galimybę diferencijuoti arterijas pagal judesio slopimo profilius.
5. Surinkti ultragarsinius radiodažninius duomenis iš sveikų savanorių ir pacientų, kuriems yra padidėjusi rizika susirgti širdies ir kraujagyslių ligomis, ištirti ir palyginti judesio parametrus tarp dviejų skirtingų grupių.

Mokslinis naujumas

Šioje daktaro disertacijoje buvo atliktas kiekybinis skiriamumo neapibrėžčių, kylančių skaitmeniniame linijinio skenavimo simuliacijoje naudojant Field II, vertinimas ir jų palyginimas su fiziniu fantomo skenavimo rezultatais. Tai leidžia daryti išvadą apie kiekybines taško sklaidos funkcijos ir skiriamumo elevacijos plokštumoje neapibrėžtis naudojant standartinius fantomus.

Buvo sukurtas dinaminis 3D arterijos modelis, gebantis atkurti realistiškus ir dinaminis pulsuojančios žmogaus arterijos, apsuptos viskoelastinio audinio, radiodažninius signalus.

Praktinė darbo vertė

Kiekybinis ultragarsinis vizualizavimas leidžia simuliuoti neapdorotus radiodažninius signalus, atitinkančius tuos, kurie gaunami realaus ultragarsinio skenavimo metu.

Pasiūlytas dinaminis 3D arterijos modelis leidžia simuliuoti 3D deformacijos elastografiją, kurti ir verifikuoti elastografijos algoritmus, 3D elastografijos eksperimentus ir galimybių studijas.

Šioje disertacijoje pateikti metodai buvo sukurti ir taikyti gavus šio projekto paramą: Lietuvos mokslo tarybos finansuojamas mokslininkų grupių projektas *Ultragarsinės radiodažninės deformacinės elastografijos algoritmų tyrimas (ELASTUS)* – Nr. S-MIP-19-8, 2019-2022 m.

Ginti teikiami teiginiai

1. Sukurtas virtualus skenavimo simuliacijai, atitinkantis fizinį ultragarsinį skenavimą. Skaitmeninis skenavimas rodo gerą sutapimą su fiziniu: neatitikimas tarp taško sklaidos funkcijų plokščių pusės lygyje ašine ir šonine kryptimis yra atitinkamai mažesnis nei 12 % ir 16 %.
2. Buvo sukurtas 3D arterijos modelis, gebantis atkurti žmogaus bendrosios miego arterijos biomechaninę elgseną ir tinkamą ultragarsinių radiodažninių signalų simuliacijai. Echoskopijos simuliacijai rodo, kad

arterijos modelis atvaizduoja A, B ir M režimo vaizduose arterijos struktūrą, tokią kaip ir *in vivo* arterijos sienelė. Įvertinti vienalaikiai, virtualiai nuskenuotos 3D struktūros skersinis ir išilginis judesiai vizualiai beveik nesiskiria nuo sugeneruoto judesio šablono.

3. Ištirtas siūlomų judesio detektavimo algoritmų tikslumas naudojant simuliuotus bendrosios miego arterijos ultragarsinius radiodažninius signalus. Rezultatai rodo, kad skersinių ir išilginių judesių detektavimo tikslumo vertinimui skirtų parametrų įvairovė gali įvertinti ne tik klaidą, bet skirtumus tarp apskaičiuotų ir teorinių judesio signalų.
4. Ištirta galimybė diferencijuoti arterijas pagal judesio slopimo profilius. Rezultatai rodo, kad skersinių ir išilginių judesių slopimo profilių įvairovė, apibrėžianti skirtingo elastingumo audinius, gali būti naudojama sveikų tiriamųjų ir rizikos grupei priklausančių pacientų diferencijavimui.
5. Surinkti sveikų savanorių ir pacientų, kuriems yra padidėjusi rizika susirgti širdies ir kraujagyslių ligomis, ultragarsiniai radiodažniniai duomenys, apskaičiuoti dviejų skirtingų populiacijų judesio parametrai ir įvertinta šių parametrų diagnostinė geba diagnozuoti pacientus, sergančius ateroskleroze ir ne. Didžiausiu jautrumu iš pasiūlytų laiko ir dažnio srities parametrų pasižymėjo poslinkis, t.y. 0,77 ir spektrinė sklaida, t.y. 0,86. Greitis ir spektrinis centroidas, priskirti kaip parametrai pasižymintys didžiausiu specifiškumu ir atitinkamai lygūs 0,88 ir 0,71.

Rezultatų aprobavimas

Disertacijoje pateikti rezultatai buvo publikuoti devyniuose mokslo darbuose, iš kurių penki straipsniai buvo paskelbti užsienio leidyklų leidžiamuose Mokslinės informacijos instituto pagrindinio sąrašo leidiniuose, turinčiuose citavimo indeksą. Rezultatai buvo pristatyti dvejose tarptautinėse ir vienoje nacionalinėje mokslinėje konferencijoje: World Congress on Medical Physics and Biomedical Engineering (IUPESM 2018), 2019 IEEE International Ultrasonics Symposium (IUS), ir Bioateitis: gamtos ir gyvybės mokslų perspektyvos 2019. 2020 m. gauta Lietuvos mokslo tarybos skirta stipendija. 2019 ir 2020 metais buvo gautos KTU skirtos doktorantų skatinamosios stipendijos už pasiekimus.

Disertacijos struktūra

Disertaciją sudaro įvadas, trys skyriai, baigiamosios išvados, santrauka, literatūros sąrašas, autoriaus publikacijų ir konferencijų sąrašas bei du priedai. Darbą sudaro 149 puslapiai, 54 paveikslai, 4 lentelės, 21 formulė ir 175 literatūros šaltiniai. Darbo turinys yra išdėstytas taip: pirmame skyriuje aprašoma bendrosios miego arterijos anatomija ir histologija, išilginis arterijos sienos judėjimas, pasiūlyti skaitmeniniai arterijų modeliai, atitinkamas realios ultragarsinės echoskopijos simuliacija ir arterijos sienelės judesio sekimo algoritmai. Antrame skyriuje pateikiamas ultragarsinis bendrosios miego arterijos tyrimas, išvystytas fizinio ultragarsinio skenavimo skaitmeninis simuliacija ir verifikavimas, sukurtas skaitmeninis arterijos modelis ir išplėtoti ultragarsinių radiodažninių signalų

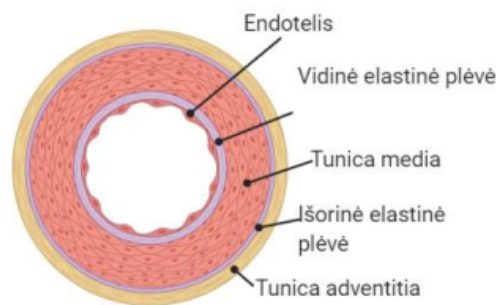
apdorojimo algoritmai. Trečiame skyriuje pateikiami eksperimentiniai modeliavimo, judesio detektavimo tikslumo ir skersinio *in vivo* judesio parametrizavimo rezultatai. Ketvirtas skyrius skirtas baigiamosioms išvadoms.

1. BENDROSIO MIEGO ARTERIJOS JUDESIŲ IR METODŲ JUDESIO SEKIMUI APŽVALGA

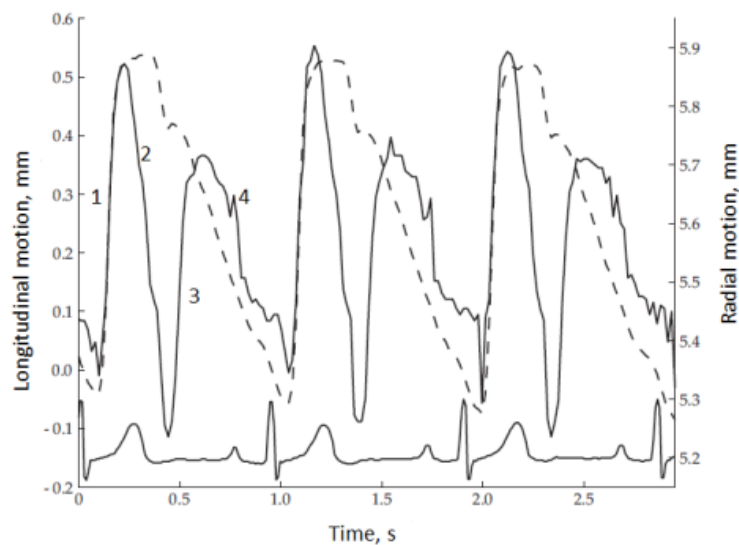
Bendroji miego arterija yra kaklo srityje ir patenka į miego arterijos trikampį, kurį riboja priekinis galvos sukamojo raumens kraštas, užpakalinis dvipilvio raumens pilvelis ir viršutinis mentinio poliežuvių raumens pilvelis^[47].

Bendrosios miego arterijos sienelė sudaryta iš trijų sluoksnių (žr. 1.1 pav.)^[17,50]:

1. vidinio sluoksnio vadinamo *tunica intima*.
2. vidurinio sluoksnio vadinamo *tunica media*.
3. išorinio sluoksnio vadinamo *tunica adventitia*.



1.1 pav. Bendrosios miego arterijos struktūra



1.2 pav. Išilginio judesio (—), diametro kitimo (---) sąsaja su elektrokardiograma.

Išilginio judesio būseną širdies ciklo metu pažymėta skaičiais (1,2,3,4). Išilginio judesio ir diametro pokyčio amplitudės yra tokios pačios. Tačiau, vis dar esant sistolei, išilginis judesys pasižymi aiškiu judesiu atgal (2) ir diastolės metu judesiu į priekį (3). Adaptuota iš^[21]

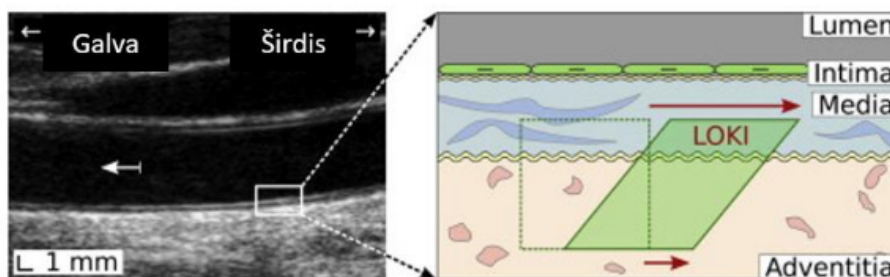
Sistolės metu iš skilvelių išstumiamas kraujas ištempia kraujagyslių sieneles, kai diastolės metu tamprios kraujagyslių sienelės pastumia kraują į periferiją ir

sugrįžta į pradinę būseną. Nors, skersinis arterijų išsiplėtimas sukelia pulsuojantį kraujo srautą, dauguma arterijų (pakinklinė arterijos, žastinė, miego) turi išilginį judėjimą lygiagrečiai kraujo srautui, kuris apibūdina kraujagyslių elastingumą.

Dvikryptis *intima-media* komplekso išilginis judėjimas stebimas širdies ciklo metu (žr. 1.2 pav.). Sistolės pradžioje *intima-media* kompleksas juda kraujo srauto kryptimi (1). Vėliau, vis dar esant sistolei, šio komplekso judėjimas vyksta prieš kraujo srauto kryptį (2). *Intima-media* kompleksas dar kartą juda į priekį diastolės metu (3) ir galiausiai grįžta į pradinę padėtį (4).

Cinthio ir kt. ^[21] kartu su Nillson ir kt. ^[51] paskelbė, kad arterijos sienelės *adventitia* sluoksnis turi tą patį išilginio judesio šabloną, tačiau judesio dydis yra mažesnis nei *intima-media* komplekso, kas parodė anksčiau nežinomą, žymų šlyties įtempį, tuo būdu šlyties deformaciją, vykstančią pačioje arterijos sienelėje.

Vėliau šis fenomenas Zahnd ir kt. ^[52] buvo pavadintas išilgine kinetika (LOKI), kuomet širdies ciklo metu *intima-media* kompleksas juda *adventitia* sluoksnio atžvilgiu lygiagrečiai kraujo srautui kas sukelia arterijų sienelių šlyties deformaciją, (žr. 1.3 pav.). Dėl to stebimas šlyties įtempis ir šlyties deformacija tarp *intima-media* komplekso ir *adventitia* sluoksnio. Tyrimai parodė, kad arterijų standumą ir širdies bei kraujagyslių rizikos veiksnių buvimą atspindi išilginės kinetikos parametras ^[21,52].



1.3 pav. Išilginis *in vivo* sveikos bendrosios miego arterijos ultragarsinis B-rėžimo vaizdas (*kairėje*). Balta rodyklė vaizduoja kraujo tėkmės kryptį. Išilginė kinetika įvykstanti arterijos sienelėje širdies ciklo metu (*dešinėje*). Atkreipkite dėmesį, kad audinio judėjimo šablonas širdies ciklo metu yra daugiafazis ir dvikryptis. Šaltinis: Zahnd ir kt. ^[52]

Miego arterijos sienelės judesys buvo modeliuojamas daugelio autorių. ^{[42][43][44][45]} Tačiau nei viename iš ankstesnių tyrimų nenagrinėjamas išilginis arterijos judėjimas kartu su skersinio ir išilginio judesių slopimu gylyn į audinius. Tai padarė Stoitsis ir kt. ^[46] simuliuojant skersinį judėjimą kaip impulso funkciją, kurios parametrai vertės buvo nustatytos remiantis eksperimentais su *in vivo* duomenimis. Išilginis judesys buvo modeliuojamas kaip sinuso funkcija, nes nėra galutinės informacijos apie šio judesio matematinį modeliavimą. Remiantis panašiu *in vivo* tyrimu, taip pat buvo įtraukta erdvinė skersinio ir išilginio judesių amplitudės priklausomybė, kuri yra nepriklausoma nuo ašinės padėties.

Kadangi skaitmeninė simuliacija tampa vis svarbesnė ultragarsinio vizualizavimo ir elastografijos raidai, vis tik problema yra kiekybinis neapibrėžtumų, susijusių su simuliacijos proceso komponentais, įvertinimas. Be to, kiekybinis

simuliavimo palyginimas su eksperimentiniu skenavimu, įskaitant skiriamosios gebos analizę ašine, šonine ir elevacijos kryptimis, tebėra ribotas.

Skersiniam ir išilginiam judesiui detektuoti siūlomi blokų tapatinimo, optinės tėkmės, požymių atitikimo algoritmai. Kai kurie iš jų yra laisvai (CAROLAB^[133]) ar komerciškai (MyLab^[133]) prieinami išilginiam judesiui tirti. Bet šiuo metu nei vienas iš jų netaikomas klinikinėje praktikoje. Pirmiausia šie metodai turėtų būti detaliai ištirti prieš juos pradėdant plačiai naudoti.

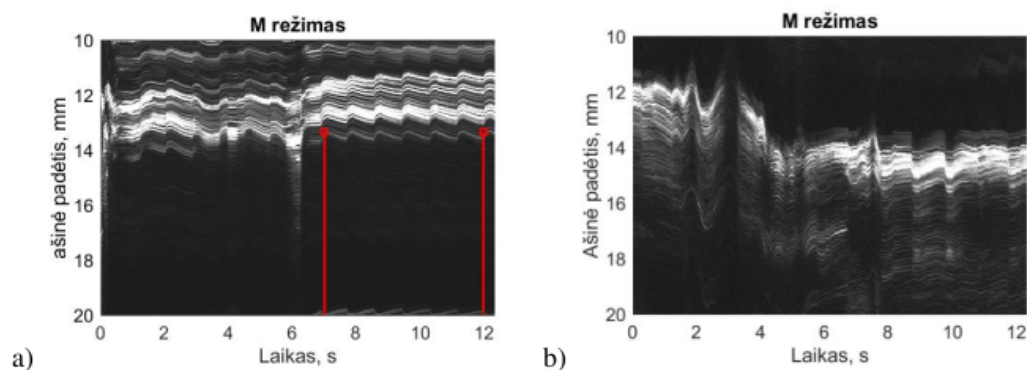
2. PLĖTOJAMI METODAI ARTERIJOS IR APLINKINIŲ AUDINIŲ PULSAVIMO SIMULIAVIMUI BEI JUDESIO DETEKTAVIMO TIKSLUMO VERTINIMAS

2.1. Bendrosios miego arterijos ultrgarsinis tyrimas

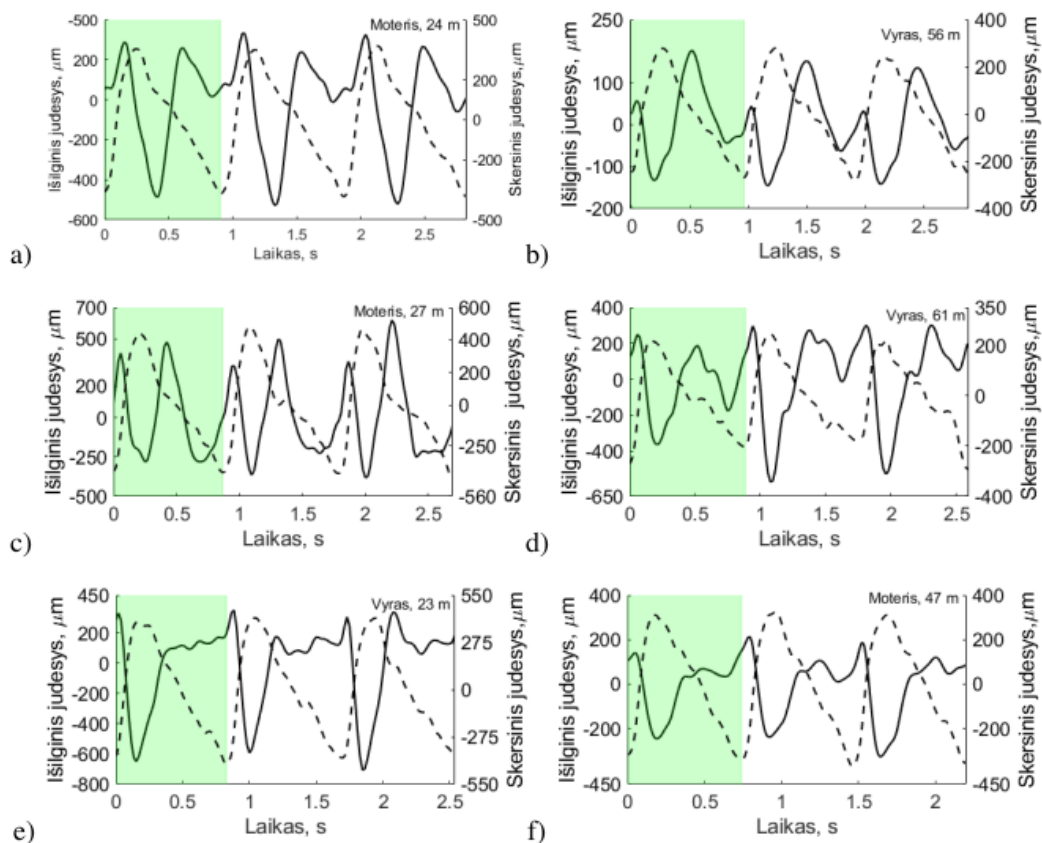
Bendrosios miego arterijos skenavimas buvo atliekamas Ultrasonix SonixTouch echoskopu (Analogic Ultrasound, Kanada) naudojant linijinę gardelę. Pagrindiniai ultrgarsinio keitiklio ir duomenų surinkimo parametrai buvo tokie: bangų dažnis 13,3 MHz, fokusavimo atstumas 1,5 cm, skenavimo gylis 2,5 cm, kadrų dažnis 52 Hz, kadrų skaičius 629, vaizdą sudarančių echoskopinių linijų skaičius 640, skenavimo sektorius 50 %, radiodažninio signalo diskretizavimas 40 MHz, ultragarso bangų greitis – 1540 m/s.

Trisdešimt jaunų sveikų savanorių (dvidešimt viena moteris, devyni vyrai) ir dvidešimt aštuoni vyresni, rizikos grupei sirgti širdies ir kraujagyslių ligomis priklausantys pacientai (dešimt moterų, aštuoniolika vyrų) buvo įtraukti į tyrimą. Ultrgarsinių radiodažninių signalų ir B režimo vaizdų sekos buvo surinktos Lietuvos sveikatos mokslų universiteto ligoninėje Kauno klinikose, Kardiologijos skyriuje, 2018 metų gegužės – spalio mėnesiais. Tyrimai atlikti gavus Kauno regioninio biomedicininio tyrimų etikos komiteto bioetikos leidimą (2018-08-02, No. BE-2-51, Kaunas, Lietuva).

Du kardiologai atliko bendrosios miego arterijos skersinio ir išilginio judesių ultrgarsinių radiodažninių signalų ir B režimo vaizdo sekų registravimą. Išilginių ir skersinių judesių bent per du pilnus širdies ciklus registravimas buvo atliekamas 2–3 cm nuo bifurkacijos. Siekiant išvengti judesio artefaktų, ultrgarsinis keitiklis buvo įtvirtintas į stacionarų laikiklį, o duomenų registravimo metu pacientų buvo prašoma sulaikyti kvėpavimą apie 10 – 15 sekundžių^[16,19,21,25]. Galiausiai visos sekos buvo saugomos skaitmeniniu būdu ir perkeltos į kompiuterį tolesnei analizei su MATLAB R2018b (The MathWorks, Inc., Natick, JAV). Duomenų kokybiškumo įvertinimas buvo atliktas remiantis vienos ultrgarsinės echoskopinės eilutės atvaizdavimu M-režime (žr. 2.1 pav.), kuomet aiškiai matosi, kuris laiko intervalas yra sugadintas judesio artefaktais, kuris intervalas yra kokybiškas ir kiek pastarajame intervale yra pilnų pasikartojančių širdies ciklų.



2.1 pav. Bendrosios miego arterijos aukštos kokybės duomenų (a) palyginimas su žemos kokybės duomenimis (b). Raudonais žymekliais (a) pažymėtas laiko intervalas, kuris buvo naudojamas tolimesnei analizei



2.2 pav. *In vivo* skersinis (*punktyrinė linija*) ir išilginis (*ištisinė linija*) bendrosios miego arterijos judesiai skirtingo amžiaus tiriamųjų parodant skirtingus išilginio judesio šablonus: a), c), e) jaunas tiriamasis, b), d), f) rizikos grupės pacientas. Žaliai pažymėti periodai buvo naudojami modeliuojant arterijos ir audinių puslacią

Po vizualinės užregistruotų duomenų patikros aštuoni sveiki savanoriai ir keturi rizikos grupės pacientai nebuvo įtraukti į tyrimą, o kiekvieno tiriamojo kokybiniai laiko intervalai rankiniu būdu buvo atrikti tolesnei analizei.

Surinkti *in vivo* duomenys buvo apdoroti CAROLAB programa, kuri įvertino išilginį bei skersinį arterijos judesius. Įvertintuose judesio signaluose rankiniu būdu buvo pažymėti trys vienas po kito sekantys širdies ciklai (žr. 2.2 pav.). Tačiau tik vienas širdies ciklas buvo naudojamas judesio modeliavime, ypač kai kiti periodai yra kvaziperiodiniai su širdies ciklu.

2.2. Fizinio ultragarsinio skenavimo skaitmeninio simuliacijos modeliavimas ir verifikavimas

Skaitmeninis keitiklis buvo modeliuojamas su Field II programa ^[36,142] Siekiant gauti adekvatumą tarp eksperimento ir simuliacijos rezultatų, buvo identifikuojami fizinio ultragarsinio skenerio ir keitiklio parametrai ir suvedami į Field II programą (žr. 2.1 lentelę).

2.1 lentelė Virtualaus skenavimo su Field II parametrai

Parametrai	Vertės
Gardelės tipas	Linijinė
Keitiklio centrinis dažnis	5 MHz
Elementų skaičius	128
Elementų žadinimas	Dviejų periodų sinusinis signalas modeliuotas Hanning-o funkcija
Elemento aukštis	4 mm
Elemento plotis	0.279 mm
Tarpas tarp elementų	0.025 mm
Atstumas tar elementų centrų	0.304 mm
Elemento sub-dalinimas x-kryptimi	1
Elemento sub-dalinimas y-kryptimi	9
Elevacijos lizės fokusas	16 mm
Fokusas	15.5 mm
F-skaičius išsiuntime	3
F-skaičius priėmimo	1.7
Apodizavimas	Hanningo funkcija
Diskretizavimo dažnis	40 MHz
Bangų greitis	1540 m/s
Nuo dažnio priklausantis slopinimas	0.5 dB/cm/MHz@ 3.5MHz

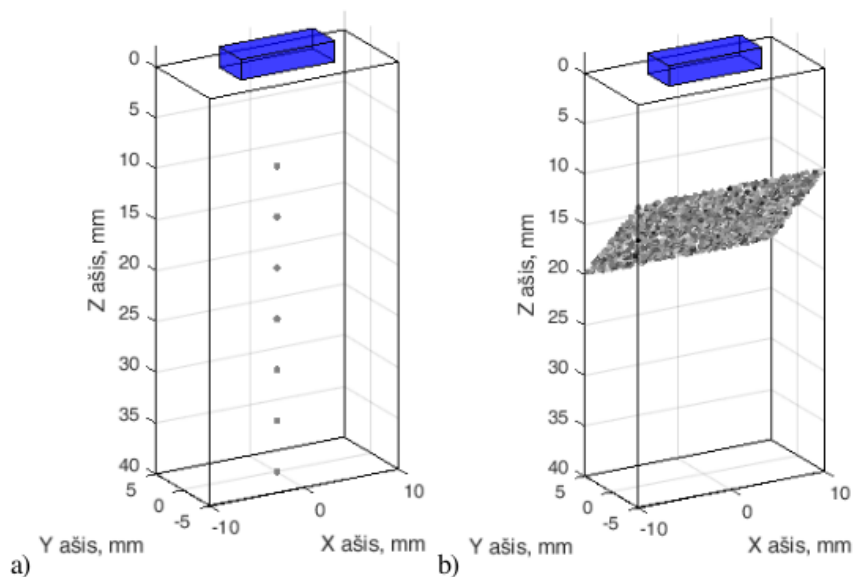
Norint tinkamai atlikti ultragarsinės skaitmeninės echoskopijos simuliaciją, reikia kiekybiškai įvertinti ir palyginti ją su fizine echoskopija. Ultragarsinio spindulio skiriamoji geba buvo vertinta pagal tris matmenis: ašine, skersine kryptimis ir

ultragarsinio spindulio plotis. Taško sklaidos funkcijos plotis pusės lygyje buvo naudojamas vertinant skirtumą tarp fizinio ir skaitmeninio skenavimų.

Siekiant turėti vienodą B režimo vaizdo formavimą tiek fizinio, tiek skaitmeninio skenavimų metu, buvo pasirinkta vaizdo formavimą sudaryti iš radiodažninių signalų gaubtinės radimo ir log-suspaudimo nuo 0 iki -70 dB.

Eksperimento metu buvo naudojami du ATS Laboratories Inc. fiziniai fantomai: 1. Model 549 General & Small Parts fantomas^[144] ašinei ir šoninei skiriamajai gebai, bei 2. Model 538NH Beam Profile & Slice Thickness fantomas^[145] spindulio pločiui elevacijos kryptimi įvertinti.

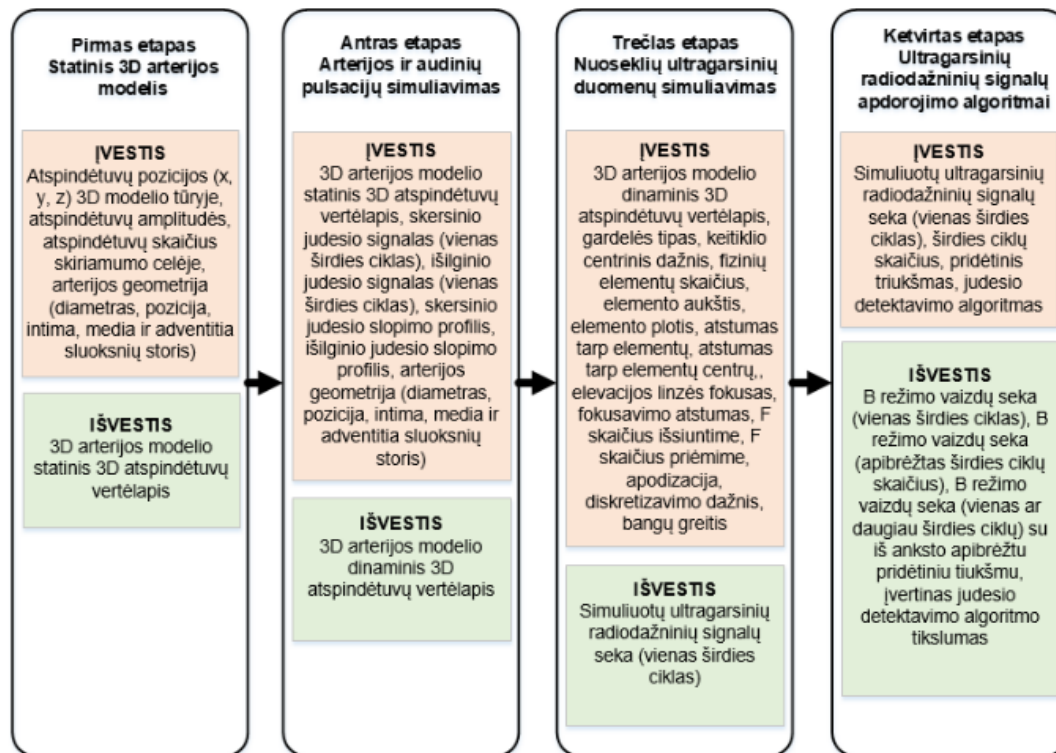
Modeliuojant skaitmeninius fantomus 3D koordinatinių sistemoje buvo nurodomos atspindėtuvų koordinatės, atspindėjimo amplitudės ir visą fantomą sudarančių atspindėtuvų skaičius. Atspindėtuvų skaičius skaitmeninių fantomų tūryje buvo nustatytas proporcingai išmatuotai fizinio ultragarsinio keitiklio skiriamumo celei^[41] ir skaitmeninio fantomo tūriui. Atspindėtuvai buvo atsitiktinai paskirstę fantomo tūryje, amplitudės buvo pasiskirsčiusios pagal Gauso funkciją. Siekiant sumodeliuoti pilnai nusistovėjusį interferencijos rezultatą, atspindėtuvų skaičius skiriamumo celėje buvo lygus 10^[41,148,149]. Norint turėti adekvačias atspindžio signalo amplitudes simuliuojamame vaizde, modeliuojamų objektų (vieučių, plokštumos) amplitudės buvo normuojamos atitinkamai pagal realaus B režimo vaizdo fono atspindėtuvų amplitudes.



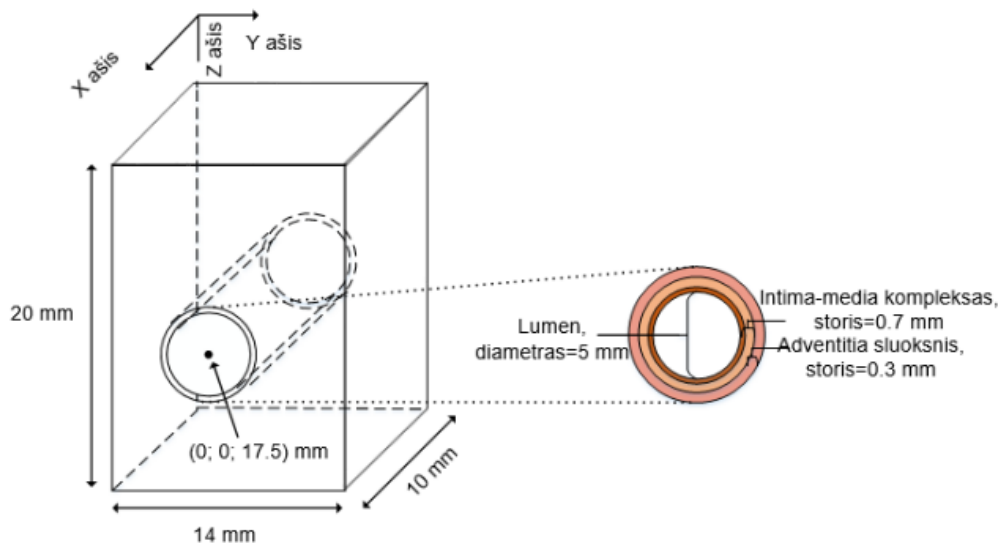
2.3 pav. Skaitmeninių fantomų konfigūracija: a) vieučių, b) spindulio pločio. fantomų viršuje pažymėti stačiakampiai gretasieniai žymi skaitmeninio ultragarsinio keitiklio poziciją

2.3. Skaitmeninis arterijos modelis

Apibendrinta simuliacijos algoritmo eiga pavaizduota 2.4 paveiksle parodo įvesties ir išvesties parametrus ir išryškina algoritmo gebėjimą modifikuoti įvesties parametrus, siekiant jį pritaikyti konkrečiai simuliacijos užduočiai.



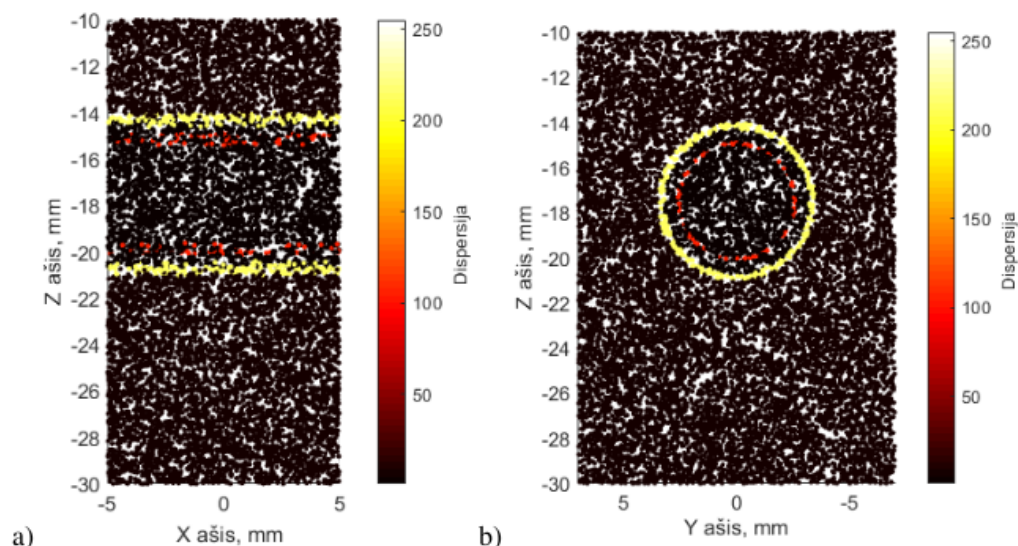
2.4 pav. Apibendrinta simuliacijos algoritmo eiga



2.5 pav. Apibendrinta arterijos modelio geometrija

Pirmame etape arterija modeliuojama statiniu atspindėtuvų pasiskirstymu pagal *in vivo* arterijos geometriją, matmenis ir padėtį. Skaitmeninė arterija modeliuojama kaip trys koncentriniai vamzdžiai, kurie atitinka tris arterijos sienelės sluoksnius (žr. 2.5 pav.).

Modeliuojant skaitmeninę arteriją 3D koordinatinių sistemoje nurodomos atspindėtuvų koordinatės, atspindėjimo amplitudės ir visą modelį sudarančių atspindėtuvų skaičius. Atspindėtuvų koordinatės ir skaičius parinkti pagal metodiką aprašytą 2.2 poskyryje, o atspindėtuvų amplitudės apskaičiuotos pagal realų bendrosios miego arterijos B-režimo ultragarsinį vaizdą. 3D arterijos modelio 3D atspindėjimo vertėlapis pateiktas 2.6 paveiksle.



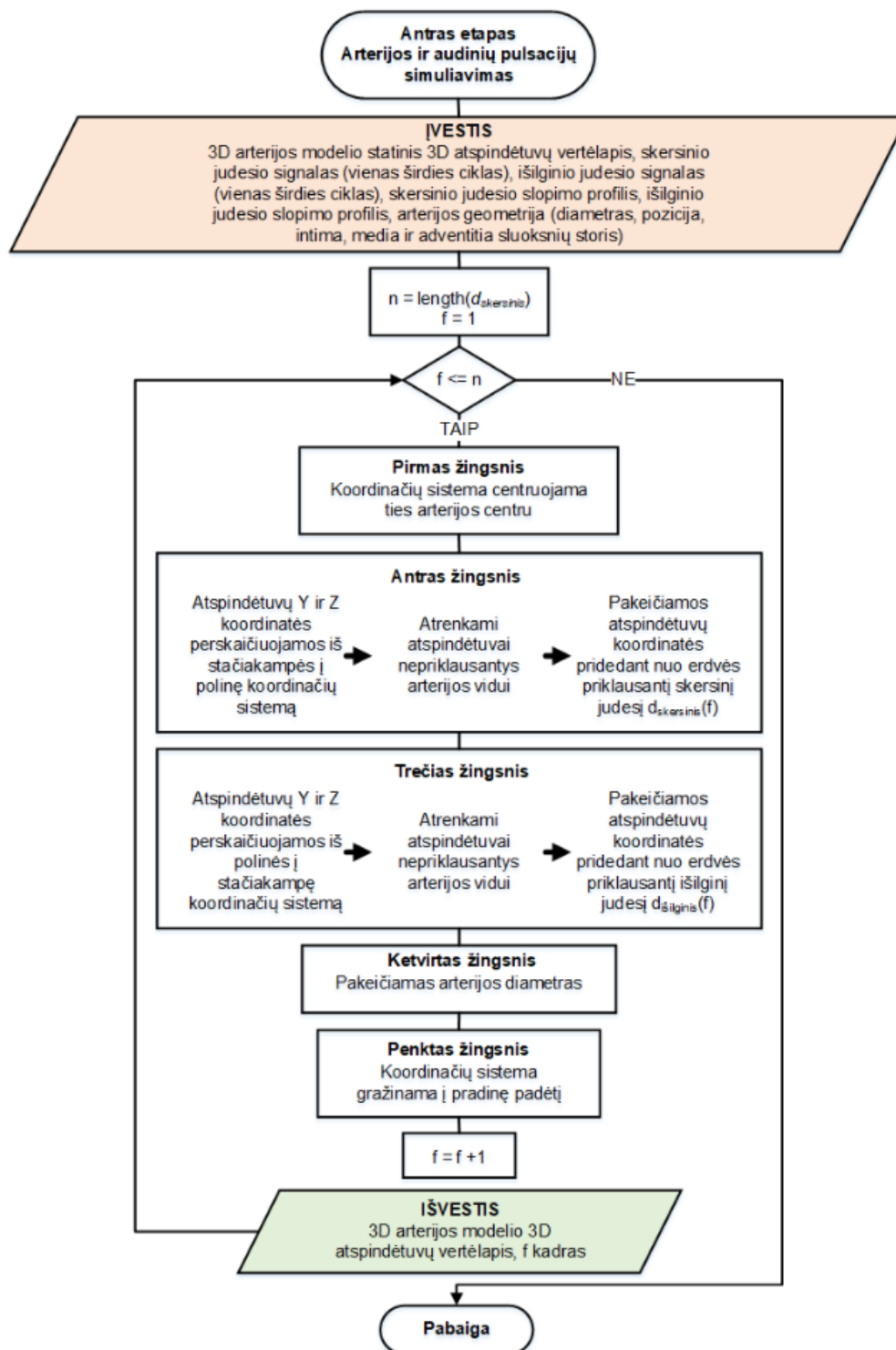
2.6 pav. 3D atspindėtuvų vertėlapis atvaizduojantis arterijos modelį iš skirtingų projekcijų: a) išilginė, b) ašinė

Antrame etape statinis arterijos modelis modifikuojamas į dinaminį naudojant *in vivo* skersinius ir išilginius judesius (žr. 2.1 poskyris) 3D pasiskirsčiusiems arterijos atspindėtuvams. Simuliavimui pasirinktų parametų vertės pateiktos 2.2 lentelėje.

2.2 lentelė Arterijos modelio judesio modeliavimo parametrai

	Sveiki savanoriai	Rizikos grupės pacientai
Judesio signalo forma	žr. 2.2 pav. a), c), e)	žr. 2.2 pav. b), d), f)
Skersinių ir išilginių judesių amplitudės, μm	1000; 750; 500	750; 500; 250
Skersinio judesio slopimas b_1	0,17	0,26
Išilginio judesio slopimas b_2	1,08	1,62
Viso:	9 atvejai	9 atvejai

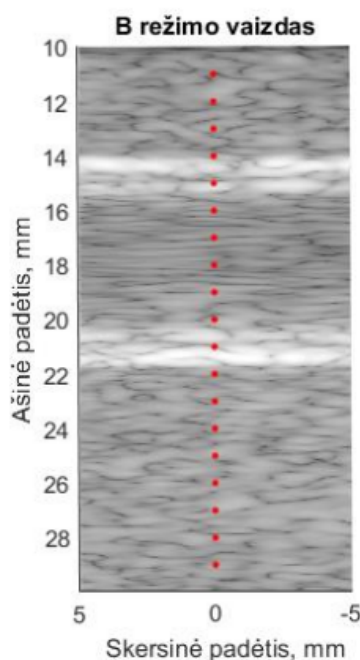
Kiekvienas arterijos ir jį supančių audinių pulsavimo simuliacijos žingsnis pateiktas funkcinėje schemoje 2.7 paveiksle.



2.7 pav. Funkcinė antro etapo schema, simuliuoti kompleksinę arterijos ir audinių pulsaciją. Čia f atitinka šiuo metu analizuojamą kadro skaičių judesio signalė ir n - bendrą tokių kadro skaičių

Judantys atspindėtuvai buvo naudojami simuliuoti vieno širdies ciklo ultragarsinių radiodažninių signalų seką (trečias etapas).

Ketvirtame etape buvo atliekamas simuliuotų ultragarsinių radiodažninių signalų apdorojimas, judesio įvertinimas, judesio detektavimo rezultatų palyginimas su arterijos ir aplinkinių audinių pulsacijos atraminiais duomenimis nustatytais antrame etape, ir santykinės judesio detektavimo klaidos įvertinimas. Judesio detektavimui pasirinkta naudoti du algoritmus: 1. 1D kros-koreliacijos ir parabolinės interpoliacijos, 2. atviros prieigos OpenOptikalFlow programą. Paklaidai tarp apskaičiuoto ir atraminio judesio įvertinti pasirinktas vidutinės absoliutinės paklaidos įvertis. Judesio detektavimo tikslumas buvo vertinamas vidurinėje echoskopavimo linijoje esant įvairioms ašinėms padėtims (žr. 2.8 pav.), t.y. pradedant nuo 11 mm kas 1 mm iki 29 mm.



2.8 pav. Simuliuotas arterijos modelio B režimo vaizdas su pažymėtais raudonais taškais, kuriuose vertintas judesio aptikimo algoritmų tikslumas

Slopimo profilių vertinimas buvo atliktas su visais modeliuojamų duomenų atvejais. Vidutinės slopimo profilių vertės ir standartiniai nuokrypiai buvo apskaičiuoti kiekvienai iš anksto pasirinktai ašinei padėčiai (žr. 2.8 pav.).

2.4. Ultragarsinių radiodažninių signalų aprorojimo algoritmai

Atsikartojantys poslinkių signalo periodai buvo nustatomi skaičiuojant antrąją judesio signalo išvestinę (pagreičio signalą) ir ieškant pikų nutolusių ne mažesniu nei 1 sekundės laiko atskaitos intervalu, kurių minimalus piko aukštis būtų 1/3 maksimalios pagreičio signale esančios vertės. Judesio signalas, nuo pirmojo iki paskutiniojo pagreičio signale rasto piko, buvo sudalintas į periodus, kurie sulygiuoti pagal diastolės momentus. Visų periodų ilgis buvo lygus trumpiausiam judesio signale

esančiam periodo ilgiui. Koreliuojantys periodai rasti skaičiuojant koreliacijos koeficientą tarp periodų ir taikant 0,95 slenkstį. Rasti koreliuojantys periodai vidurkinami laike ir gaunamas vidutinis judesio signalo periodas. Taikant Yule-Walker metodą randamas judesio periodo spektras. Vidutiniam judesio periodui ir jo spektrui parametrizuoti buvo pasirinkti laiko ir dažnio srities parametrai, kurie pateikti 2.3 lentelėje.

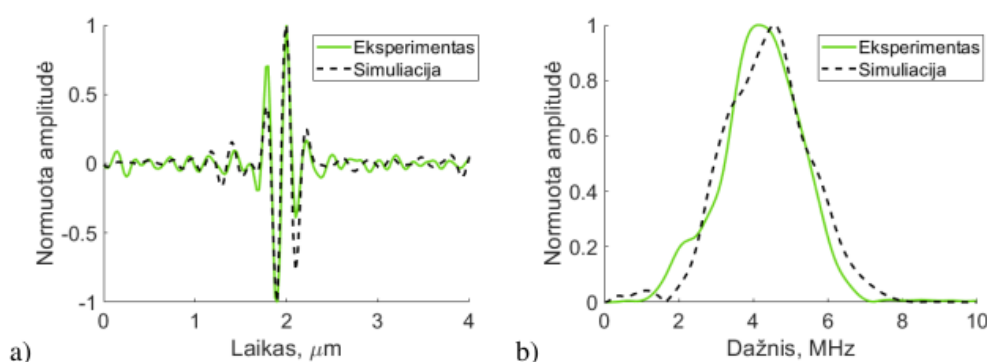
2.3 lentelė Laiko ir dažnio srities parametrai vidutinio judesio periodo signalui ir jo spektrui parametrizuoti

Laiko srities parametrai	Dažnio srities parametrai (ribose nuo 0 Hz iki 10 Hz)
<ul style="list-style-type: none"> • Širdies ritmas • Judesio amplitudė • Greičio amplitudė • Pagreičio amplitudė 	<ul style="list-style-type: none"> • Spektrinis centroidas • Spektrinis sklaida • Spektrinis asimetrija • Spektrinis ekscesas

3. REZULTATAI

3.1. Skenavimo modelio pritaikymas fizinei taško sklaidos funkcijai

Modeliavimo adekvatumas priklauso nuo simuliuojamo ultragarso impulso formos atitikties su eksperimentiškai išmatuotu impulsu. Tarpusavyje lyginant eksperimentinio ir simuliuojamo aido impulsų formą ir spektrus esant ultragarso bangos atspindžiui nuo vielutės, esančios 15 mm atstumu nuo keitiklio turime santykinai gerą sutapimą (koreliacijos koeficientas tarp eksperimento ir simuliacijos aido impulsų yra 0.91, kai tarp spektrų – 0.98), juolab, kad rezultatui įtakos turi ultragarso bangos difrakcija ir kiti sklaidimo efektai.



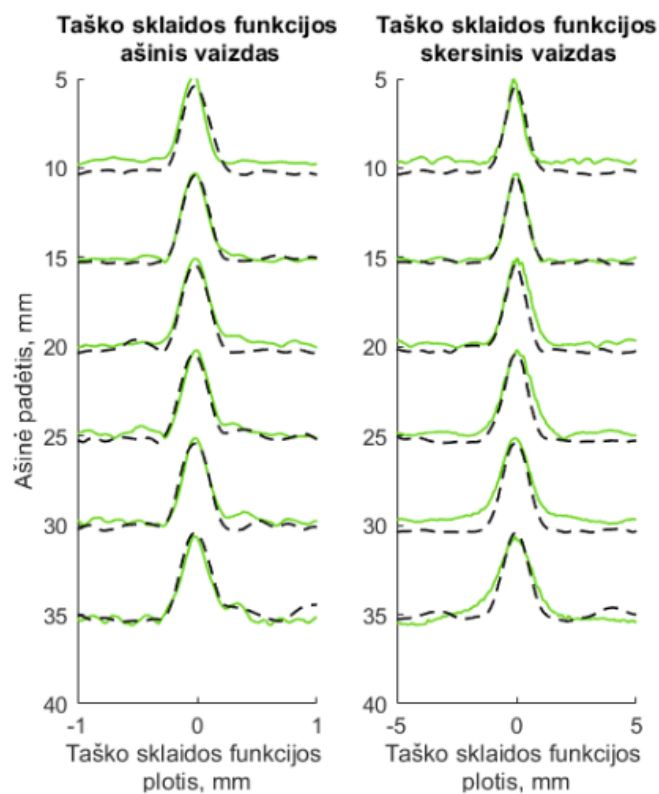
3.1 pav. Eksperimento ir simuliacijos palyginimas: a) aido impulso signalai atsispindėję nuo 15 mm gylyje esančios vielutės (ašinis vaizdas), b) aido impulso signalų spektrai

Kiekybiškai vertinant taško sklaidos funkcijos plotį gauta, kad vidutinė santykinė paklaida tarp eksperimento ir simuliacijos pagal ašinę ir skersinę skiriamąją gebą atitinkamai yra 11,6 % ir 15,2 % (žr. 3.1 lentelę).

3.1 lentelė Eksperimento ir simuliacijos palyginimas

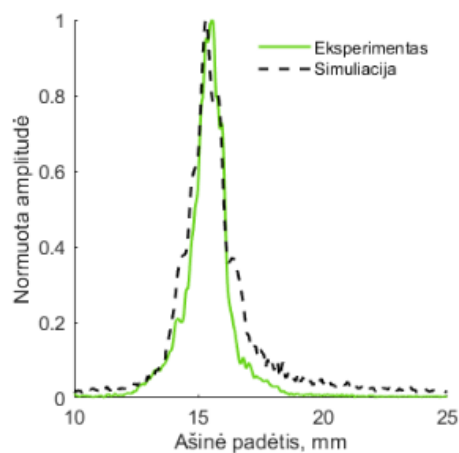
Eksperimentas				Simuliacija				Ašinės skyros santykinė paklaida, %	Skersinės skyros santykinė paklaida, %
Ašinė padėtis, mm	Skersinė padėtis, mm	Ašinė skyra, mm	Skersinė skyra, mm	Ašinė padėtis, mm	Skersinė padėtis, mm	Ašinė skyra, mm	Skersinė skyra, mm		
9,8	-0,13	0,23	0,80	10,3	0,00	0,26	1,01	13,0	26,3
15,3	0,06	0,24	1,02	15,4	0,00	0,27	1,05	12,5	2,9
20,1	0,06	0,25	1,18	20,4	0,00	0,27	1,03	8,0	12,7
25,2	0,00	0,26	1,37	25,4	0,00	0,27	1,16	3,8	15,3
30,1	-0,06	0,24	1,46	30,4	0,00	0,29	1,29	20,8	11,6
35,6	-0,06	0,26	1,69	35,3	0,00	0,29	1,31	11,5	22,5
Vidurkis, %								11,6	15,2

3.2 paveiksle parodyta, kad normuotos taško sklaidos funkcijos ašinis vaizdas geriau sutampa su eksperimentu nei šoninio vaizdo atveju. Tam įtakos turi sunkiai įvertinami apodizacijos, fokusavimo ir kiti ultragarso difrakcijos efektai.



3.2 pav. Taško sklaidos funkcijos pločio ašine ir skersine kryptimis palyginimas: ištisinė linija – eksperimentas, punktyrinė linija – simuliacija. Taško sklaidos funkcijos amplitudės normuotos nuo 0 iki 5

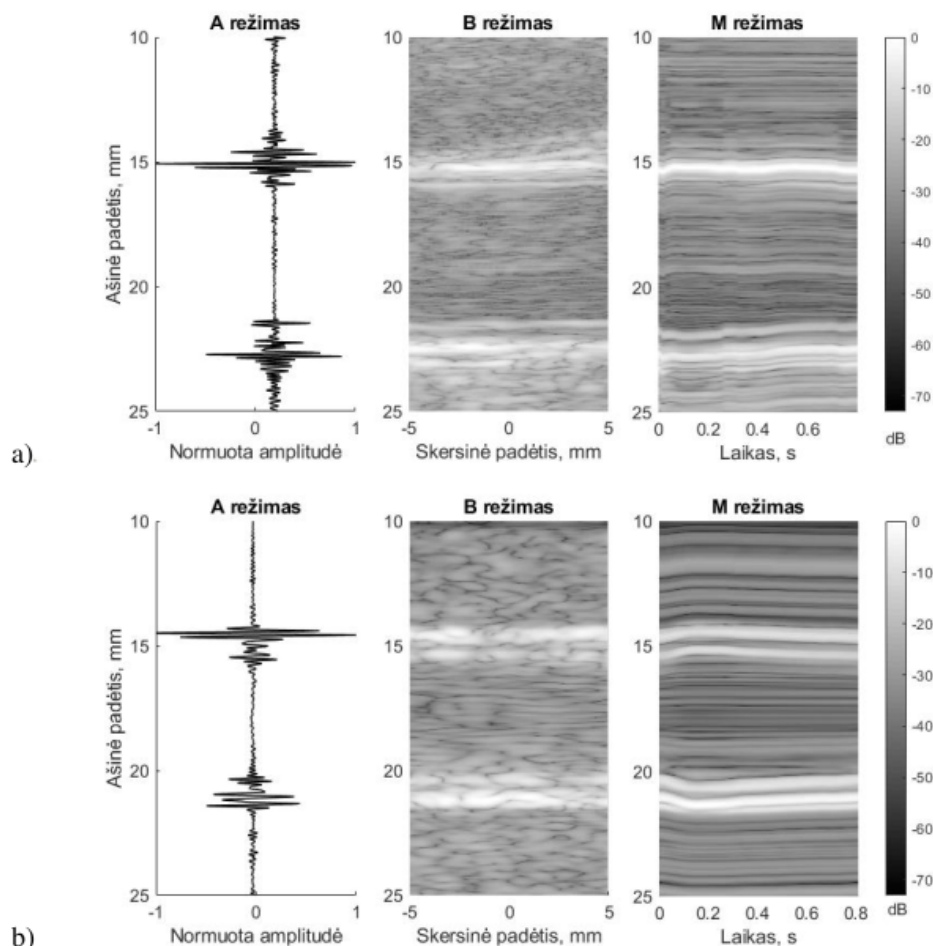
Ultragarinio spindulio plotis pusės lygyje elevacijos plokštumoje (žr. 3.3 pav.) echoskopijos atveju buvo 1,21 mm, o simuliacimo atveju 1,38 mm.



3.3 pav. Echoskopija ir simuliacimo elevacijos skiriamosios gebos palyginimas pagal iš šono vidurkintas skenavimo linijas

3.2. Arterijos modelio simuliuotų ultragarsinių radiodažnių signalų ir vaizdų rezultatai

Tarpusavyje lyginant eksperimentinius ir simuliuotus duomenis (žr. 3.4 pav.) gauta, kad A režime abiem atvejais aiškiai matyti aidų impulsai nuo *lumen-intima* ir *media-adventitia* ribų, o B režimo atvejais arterijos sienelės matosi kaip dviguba linija. Apibendrinant, arterijos modelis pasižymi *in-vivo* arterijos sieniei būdinga struktūra.

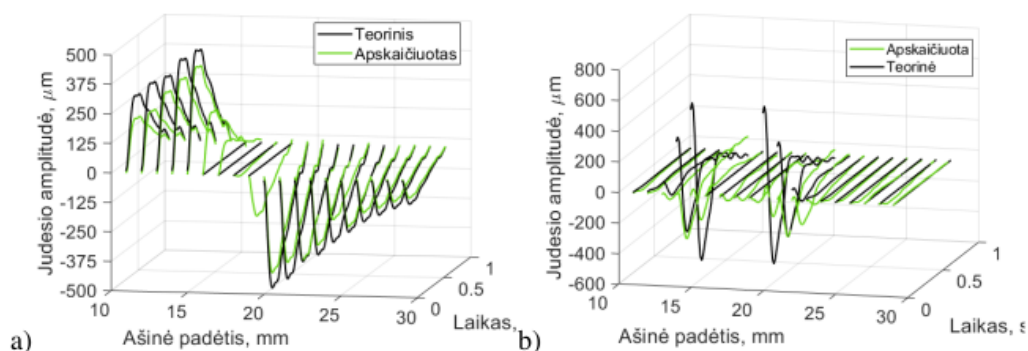


3.4 pav. Radiodažnių signalų formos palyginimas (A režimas, f_1 kadras, skersinė padėtis 0 mm), B režimo vaizdas (f_1 kadras), judesys laike (M režimas): a) *in vivo* atvejis (23 metų moteris, judesio amplitudė nenormuota), b) simuliuotas atvejis (23 metų moteris, judesio amplitudė normuota į 1 mm)

M režime stebime arterijos modelio judėjimą pagal užduotą skersinio judesio signalą. Gauta, kad tiek apatinė, tiek viršutinė arterijos modelio sienelės juda pagal tą pačią judesio formą, tik priešingu ženklu. *In-vivo* atveju tokio vienodo abiejų sienelių judėjimo nematyti. Greičiausiai ultragarsinis keitiklis registravimo metu nebuvo visiškai teisingai laikytas ties arterijos centru ir 90 laipsnių kampu į arteriją. Taip pat

neatmetama galimybė, kad registravimo metu ultragarsinis keitiklis buvo spaudžiamas į kaklą, kas neleido viršutinei arterijos sieniei judėti tokiu pat dėsniu kaip apatinei.

Dinaminis 3D arterijos modelis turi panašius skersinių ir išilginių judesių šablonus, amplitudę ir slopimą gilyn į audinius lyginant su teoriniais judesiais (žr. 3.5 pav.), nors apskaičiuota judesių amplitudė yra nežymiai mažesnė nei teorinė.

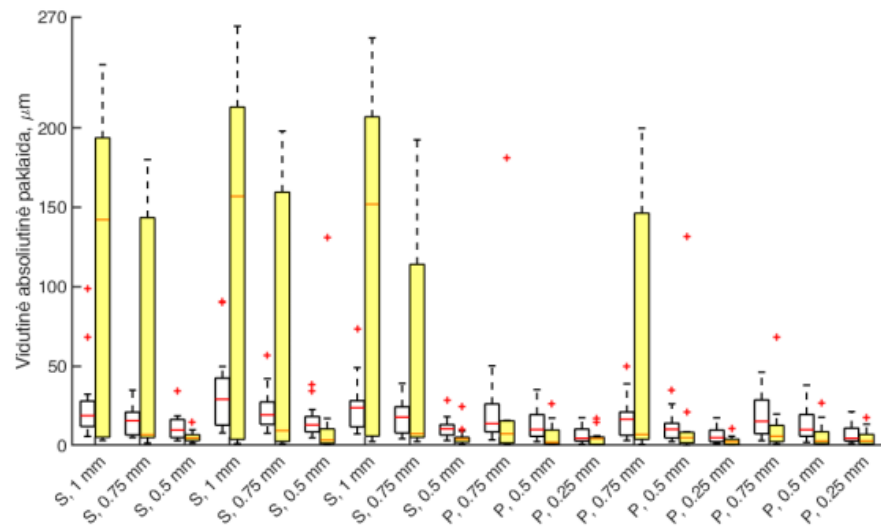


3.5 pav. Viršutinės ir apatinės arterijos sienelių ir aplinkinių audinių judesiai detektuoti su OpenOpticalFlow algoritmu, 23 metų moteris: a) 1 mm amplitudės teorinis ir apskaičiuotas skersinis judesys, b) 1 mm amplitudės teorinis ir apskaičiuotas išilginis judesys

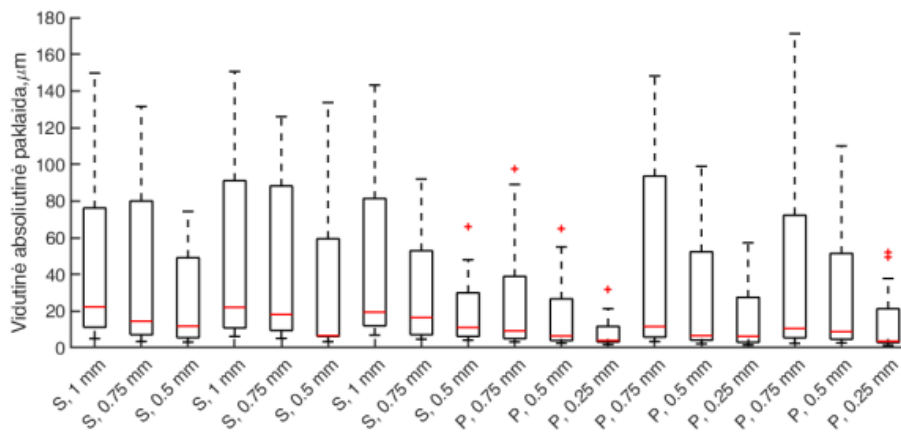
3.3. Skersinio ir išilginio judesių detektavimo metodų tikslumo tyrimo rezultatai

Vidutinės absoliutinės paklaidos analizė parodė, kad didelių klaidų pasitaiko, kai skersiniam judesiui aptikti buvo naudojamas 1D kros- koreliacijos metodas, o judesio amplitudė buvo didesnė nei 0,75 mm (žr. 3.6 pav. a). Žymias paklaidas lemė tai, kad tarpkadrinis judėjimas buvo didesnis nei ketvirtadalis bangos ilgio dėl ko egzistuoja tikimybė nustatyti klaidingą koreliacijos piką, kas įtakoja dideles dvireikšmiškumo klaidas. Nepaisant to nustatyta, kad esant didelėms skersinio judesio amplitudėms medianinės vidutinės absoliutinės paklaidos vertės buvo mažesnės nei 25 μm tiriant OpenOpticalFlow metodą.

Tiriant OpenOpticalFlow metodo galimybę detektuoti išilginį judesį gauta, kad medianinės vidutinės absoliutinės paklaidos vertės yra mažesnės nei 25 μm (žr. 3.6 pav. b). Vertinant vidutinės absoliutinės paklaidos vidurkio vertes gauta, kad jos yra apie 50 μm ir turi tendenciją mažėti, kai detektuojama judesio amplitudė mažėja.



a)



b)

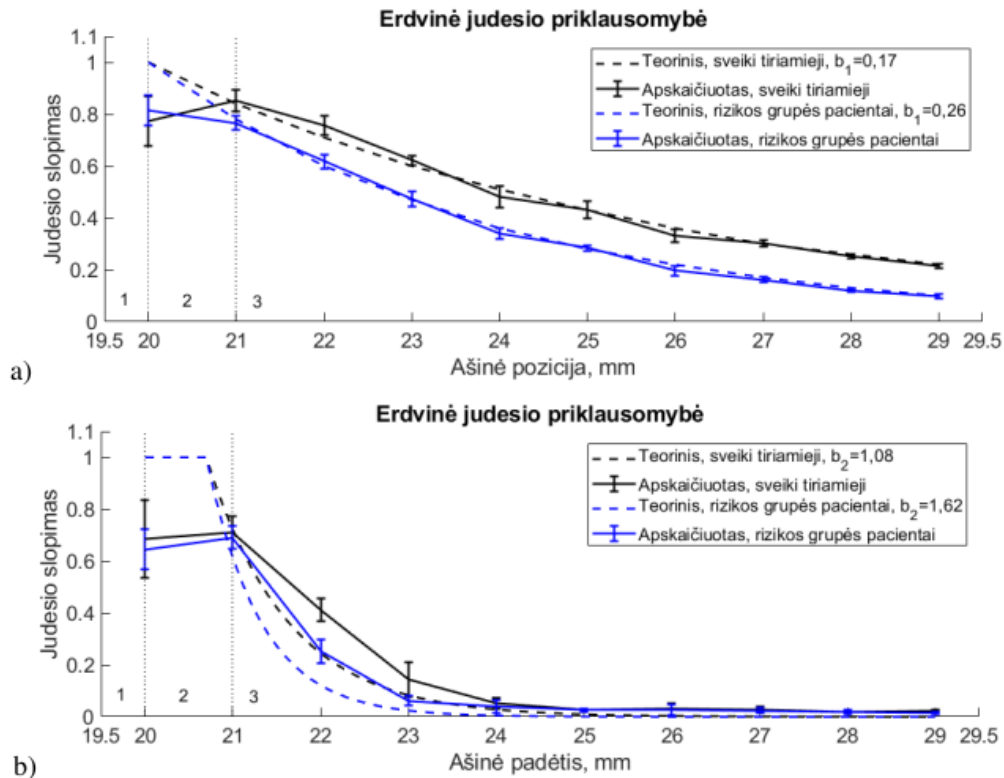
3.6 pav. Stačiakampės vidutinės absoliutinės paklaidos diagramos vaizduojančios paklaidas įvertintas vidurinėje skenavimo linijoje pradedant nuo 11 mm kas 1 mm iki 29 mm) (n=19):

a) skersinio judesio detektavimas, b) išilginio judesio detektavimas. Baltos ir geltonos stačiakampės diagramos atitinkamai yra 1D kros-koreliacijos ir OpenOpticalFlow algoritmai. Medianinės vertės vaizduojamos horizontaliomis raudonomis linijomis, riktai – raudonais +.

S – sveikas savanoris, P – rizikos grupės pacientas

3.4. Skersinių ir išilginių judesių teorinių ir apskaičiuotų slopimo profilių palyginimas

Atliekant arterijos apatinės sienelės ir aplinkinių audinių skersinių ir išilginių judesių amplitudėserdvinės priklausomybės palyginimą tarp teorinių ir apskaičiuotų verčių gauta, kad teorinis ir apskaičiuotas skersinio judesio slopimo profiliai aplinkiniuose audiniuose gerai sutampa (žr. 3.7 pav. a). Tačiau tokio gero sutapimo arterijos sienelėje nematyti. Tai galėjo nutikti dėl nepakankamo iš anksto pasirinktų taškų skaičiaus arterijos sienelėje, kuriuose buvo vertinamas slopimo profilis.



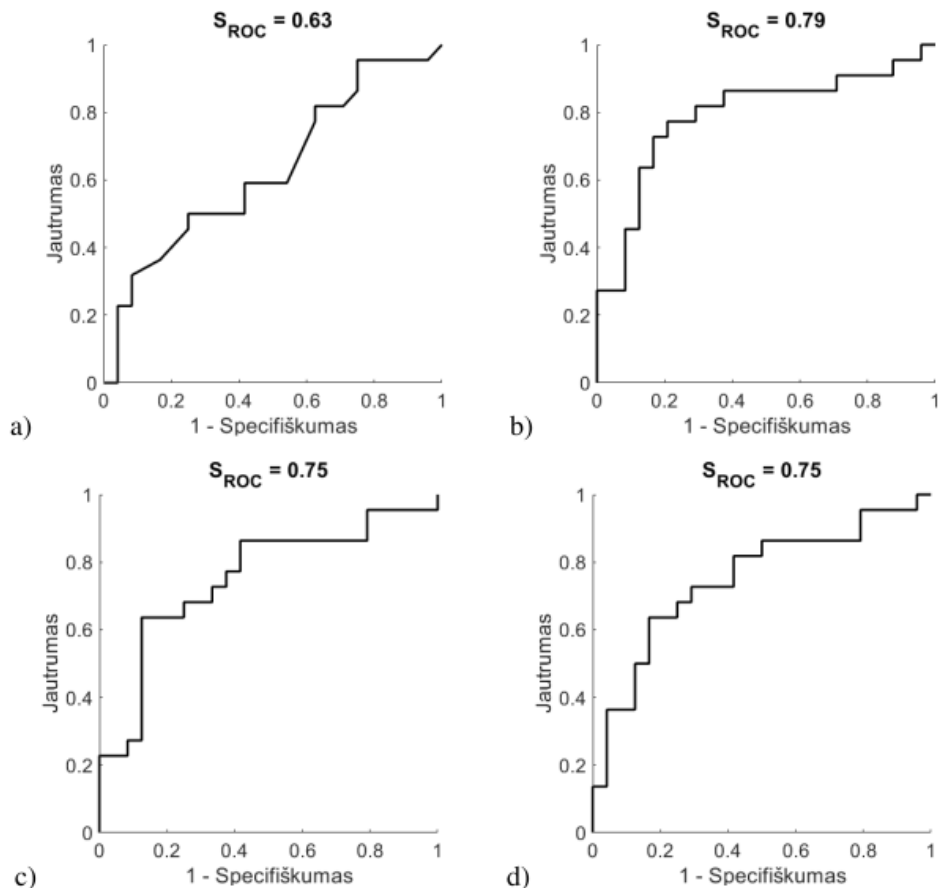
3.7 pav. Teorinių ir apskaičiuotų (OpenOpticalFlow algoritmas) skersinių ir išilginių judesių priklausomybės nuo ašinės padėties palyginimas: a) skersinių judesių slopimas arterijos sienelėje ir aplinkiniuose audiniuose, b) išilginių judesių slopimas arterijos sienelėje ir aplinkiniuose audiniuose. Vidurkiai ($n=9$) ir standartiniai nuokrypiai ($n=9$) vaizduoja apskaičiuotas slopimo profilių vertes kiekvienai pasirinktai ašinei pozicijai. Skaičiai 1, 2, 3 atitinkamai nurodo arterijos vidų, arterijos sienelę ir aplinkinius audinius.

Toks pats iš anksto parinktų taškų skaičius buvo naudojamas išilginio judesio slopimo profilio įvertinime arterijos sienelėje. Čia matomas dar didesnis teorinių ir apskaičiuotų slopimo profilių neatitikimas (žr. 3.7 pav. a). Be to, apskaičiuoti išilginio judesio profiliai yra prasislinkę lyginant su teoriniais aplinkinių audinių slopimo profiliais. Nepaisant teorinių ir apskaičiuotų judesio slopimo profilių neatitikimo, ypač išilginio judesio atveju, sveiki tiriamieji ir rizikos grupės pacientai gali būti diferencijuojami pagal skersinių ir išilginių judesių slopimo profilius.

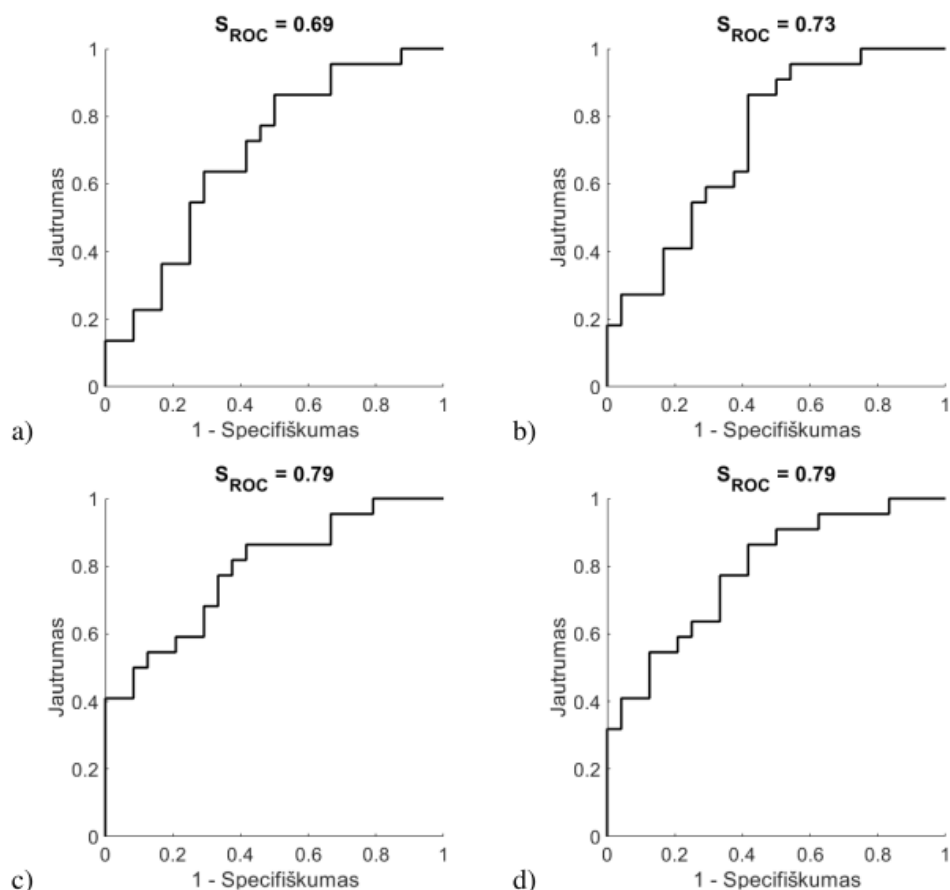
3.5. In vivo skersinio judesio signalų parametrų nustatymo rezultatai

Lyginant laiko srities parametrus ir remiantis plotu po ROC kreive (S_{ROC}), kuris yra apie 0,8 (žr. 3.8 pav. b, c ir d) nustatyta, kad poslinkio, greičio ir pagreičio parametrai geba diferencijuoti sveikus savanorius ir rizikos grupės pacientus.

Dažnio srities parametrų (žr. 3.9 pav.) analizė parodė, kad diferencijuoti dviejų tiriamųjų grupes galima pagal spektrinį centroidą, spektrinę sklaidą, spektrinę sklaidą ir spektrinį ekscesą nes S_{ROC} atitinkamai yra 0,69; 0,73; 0,79 ir 0,79.



3.8 pav. ROC kreivės a) širdies ritmo, b) poslinkio, c) greičio, d) pagreičio parametrų vertinant jų diagnostinę vertę nustatant aterosklerozę



3.9 pav. ROC kreivės a) spektrinio centro, b) spektrinės sklaidos, c) spektrinės asimetrijos, d) spektrinio eksceso parametrų vertinant jų diagnostinę vertę nustatant aterosklerozę

Didžiausiu jautrumu pasižymėjo poslinkis (jautrumas=0,77) ir spektrinė sklaida (jautrumas=0,86). Greitis ir spektrinis centroidas, priskirti kaip parametrai, turintys didžiausią specifiškumą, vertės atitinkamai yra 0,88 ir 0,71 (žr. 3.2 lentelę).

3.1 lentelė. Laiko ir dažnio srities parametrų diagnostinė vertė diferencijuojant sveikus savanorius nuo rizikos grupės pacientų

		Jautrumas	Specifiškumas
Laiko srities parametrai	Širdies ritmas, DPM	0,50	0.63
	Poslinkis, μm	0.77	0.79
	Greitis, $\mu\text{m/s}$	0.64	0.88
	Pagreitis, $\mu\text{m/s}^2$	0.73	0.71
Dažnio srities parametrai	Spektrinis centroidas, Hz	0.64	0.71
	Spektrinė sklaida	0.86	0.58
	Spektrinė asimetrija	0.77	0.67
	Spektrinis ekscesas	0.77	0.67

Baigiamosios išvados

1. Literatūros analizė parodė, kad aterosklerozė yra lėtinė arterijos sienelių liga, kuri nėra pastebima tol, kol nesusiformuoja aterosklerozinės plokštelės. Tačiau įrodyta, kad reikšmingi arterijos sienelių mechaninių savybių pokyčiai, t.y. išilginis ir skersinis arterijos sienelių judėjimas, įvyksta daug anksčiau, nei atsiranda anatomiciniai pokyčiai, t.y. *intima-media* komplekso sutorejimas. Klinikiniai tyrimai bendrosios miego arterijos išilginį judesį susiejo su rizikos veiksniais ir ŠKL, bei parodė ryšį tarp arterijos standumo, ŠKL ir išilginio judesio sumažėjimo. Skersiniam ir išilginiam judesiui detektuoti yra pasiūlyta keletas judesio sekimo algoritmų. Kai kurie iš jų yra laisvai ar komerciškai prieinami išilginiam judesiui tirti. Bet šiuo metu nei vienas iš jų nėra taikomi klinikinėje praktikoje. Pirmiausia šie metodai turi būti kruopščiai ištirti prieš juos pradedant plačiai naudoti.
2. Sukurtas virtualaus skenavimo simuliacija, atitinkanti fizinį ultragarsinį skenavimą. Skaitmeninis skenavimas rodo gerą sutapimą su fiziniu: neatitikimas tarp taško sklaidos funkcijų plokštumos lygyje ašine ir šonine kryptimis yra atitinkamai mažesnis nei 12 % ir 16 %. Elevacijos plokštumoje spindulio plotis pusės lygyje fizinės echoskopijos metu buvo 1,21 mm, o skaitmeninio skenavimo - 1,38 mm.
3. Sukurtas 3D arterijos modelis, gebantis atkurti žmogaus bendrosios miego arterijos biomechaninę elgseną ir tinkamas ultragarsinių radiodažninių signalų simuliacijai. Echoskopijos simuliacija rodo, kad arterijos modelis atvaizduoja A, B ir M režimo vaizduose arterijos struktūrą, tokią kaip ir *in vivo* arterijos sienelė. Įvertinti vienalaikiai, virtualiai nuskenuotos 3D struktūros skersinis ir išilginis judesiai vizualiai beveik nesiskiria nuo sugeneruoto judesio šablono.
4. Ištirtas siūlomų judesio detektavimo algoritmų tikslumas naudojant simuliuotus bendrosios miego arterijos ultragarsinius radiodažninius signalus. Rezultatai rodo, kad skersinių ir išilginių judesių detektavimo tikslumo vertinimui skirtų parametrų įvairovė gali įvertinti ne tik klaidą, bet skirtingumą tarp apskaičiuotų ir teorinių judesio signalų. Nustatyta, kad tiriant OpenOpticalFlow metodą skersiniam ir išilginiam judesiui detektuoti, vidutinės absoliutinės paklaidos medianinės vertės buvo mažesnės nei 25 μ m.
5. Ištirta galimybė diferencijuoti arterijas pagal judesio slopimo profilius. Teorinis ir apskaičiuotas skersinio judesio slopimo profiliai aplinkiniuose audiniuose gerai sutampa, tačiau išilginio judesio profiliai aplinkiniuose audiniuose yra prasislinkę lyginant su teoriniais profiliais aplinkiniuose

audiniuose. Rezultatai rodo, kad skersinių ir išilginių judesių slopimo profilių įvairovė, apibrėžianti skirtingo elastingumo audinius, gali būti naudojama sveikų tiriamųjų ir rizikos grupei priklausančių pacientų diferencijavimui.

6. Surinkti sveikų savanorių ir pacientų, kuriems yra padidėjusi rizika susirgti širdies ir kraujagyslių ligomis, ultragarsiniai radiodažniniai duomenys, apskaičiuoti dviejų skirtingų populiacijų judesio parametrai ir įvertinta šių parametru diagnostinė geba diagnozuoti pacientus, sergančius ateroskleroze ir ne. Didžiausiu jautrumu iš pasiūlytų laiko ir dažnio srities parametru pasižymėjo poslinkis, t.y. 0,77 ir spektrinė sklaida, t.y. 0,86. Greitis ir spektrinis centroidas, priskirti kaip parametrai pasižymintys didžiausiu specifiškumu ir atitinkamai lygūs 0,88 ir 0,71.

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APPENDIX A1

Table A1.1. Wall motion extraction techniques based on B-mode ultrasound imaging (chronologic order). Adapted from ^[27]

Study	Technique	Data	Accuracy evaluation	
			Criteria	Score
Golemati <i>et al.</i> (2003) ^[88]	BM	11 symptomatic patients 9 asymptomatic patients	No quantitative evaluation of accuracy	-
Persson <i>et al.</i> (2003) ^[22]	Echo tracking	1 healthy volunteer	No quantitative evaluation of accuracy	-
Cinthio <i>et al.</i> (2005) ^[23]	Echo tracking	1 healthy volunteer 1 agar phantom	Mean differences compared with two high-resolution triangulation lasers	Longitudinal: $5.9 \pm 40.5 \mu\text{m}$ Radial: $28.5 \pm 19.5 \mu\text{m}$
Stoitsis <i>et al.</i> (2006) ^[106]	BM and OF	10 healthy volunteers	Cross-correlation coefficient between BM and OF	Longitudinal: $0.32 \pm 0.39 \text{ mm}$ Radial: $0.72 \pm 0.22 \text{ mm}$
Gastouniotti <i>et al.</i> (2011) ^[91]	BM + Kalman filtering as an adaptive strategy with (a) updating of the reference block and (b) updating of the displacements	5 young healthy volunteers (ages: 25–32 y) 4 elderly healthy volunteers (ages: 44–73 y)	Tracking accuracy compared with conventional BM	Adaptive BM minimized the warping index and yielded average displacement error reductions of 24% with respect to BM Estimation bias reduction of 30% with respect to BM Jitter over varying center frequencies reduction of 64% with respect to BM
Zahnd <i>et al.</i> (2011) ^[25]	Multi-BM ruled by a	26 young healthy volunteers	Qualitative evaluation	-

	deformable skeleton model	26 elderly diabetic patients	only (visual control by two experts)	
Golemati <i>et al.</i> (2012) ^[61]	Comparison of several existing methods: OF, WLSOF, BM, ABMM	Real image template and Field II	Average warping indices between OF, WLOF, BM and ABMM	WLSOF: 105 μm ABMM: 120 μm BM: 405 μm OF: 694 μm
Salles <i>et al.</i> (2012) ^[105]	Phase-based OF	1 healthy volunteer	Qualitative evaluation only	-
Zahnd <i>et al.</i> (2012) ^[97]	Multi-BM guided by contour segmentation	126 indigenous Australians with periodontal disease 27 healthy age- and sex-matched Caucasian controls	Qualitative evaluation only (visual control by two experts)	-
Zahnd <i>et al.</i> (2013) ^[19]	Kalman-based BM	57 young healthy volunteers 25 diabetic patients	Average absolute error (\pm SD) from manual reference tracings	Longitudinal = $20 \pm 19 \mu\text{m}$ Radial = $84 \pm 107 \mu\text{m}$
Gastouniotti <i>et al.</i> (2013) ^[90]	Adaptive BM	40 patients 1 <i>in silico</i> phantom	Tracking accuracy compared with conventional BM	Adaptive BM algorithm, yielding a 47% increase in accuracy with respect to the conventional BM
Yli-Ollila <i>et al.</i> (2013) ^[63]	BM + luminance optimization	19 healthy volunteers	Reproducibility	Cronbach's α coefficient: 0.59–0.97
Albinsson <i>et al.</i> (2014) ^[92]	Lagrangian BM	20 healthy volunteers 1 simulated (Field II [Jensen 1996]) 1 <i>in silico</i> phantom	Absolute tracking error compared with Cinthio <i>et al.</i> (2005)	<i>In silico</i> : Improvement of tracking accuracy (mean = 48%, $p < 0.005$) Phantom: Improvement of tracking accuracy

				(mean = 43%, $p < 0.01$) <i>In vivo</i> : Reduction of block size with similar tracking performance (mean = 19%, $p < 0.01$)
Gao <i>et al.</i> (2015) ^[170]	BM + H_∞ filter	50 patients	Mean absolute tracking difference compared with manual annotations	Mean absolute estimation error: longitudinal: 96 μm , radial: 46 μm
Salles <i>et al.</i> (2012) ^[105]	Phase-based BM	1 simulated RF clip (Field II) 10 healthy volunteers	Mean absolute amplitude difference, evaluated on a numerical phantom	Longitudinal: $9.9 \pm 7.9 \mu\text{m}$ Radial: $4.2 \pm 3.4 \mu\text{m}$
Yli-Ollila <i>et al.</i> (2016) ^[171]	Transfer function analysis	19 healthy volunteers	Reproducibility	Longitudinal: Cronbach's α coefficient, 0.59–0.97 Radial: Cronbach's α coefficient, 0.68–0.93
Tat <i>et al.</i> (2016) ^[172]	Multi-BM	23 healthy volunteers 12 patients	Not specified	-
Gao <i>et al.</i> (2017) ^[95]	Elasticity-based state-space approach	37 healthy volunteers 103 patients	Correlation coefficient (r) and RMSE against manual tracings	Radial: $r = 0.9897$ RMSE = 25.98 μm Longitudinal: $r = 0.9536$ RMSE = 142.82 μm
Scaramuzzino <i>et al.</i> (2017) ^[107]	Automatic detection and matching of multiple salient points + scale-invariant feature transform	1 <i>in silico</i> phantom 18 healthy volunteers 16 patients	Accuracy Average absolute error ($\pm\text{SD}$), Maximum variation Coefficient Correlation coefficient	<i>In silico</i> <i>Intima-media</i> complex: $23 \pm 15 \mu\text{m}$ <i>Adventitia</i> : $19 \pm 18 \mu\text{m}$ <i>In vivo</i> <i>Intima-media</i> complex: 9.5 (variation coefficient, over 5 repeated measures) <i>Adventitia</i> : 13.8% (variation coefficient,

				over 5 repeated measures) Compared with visual assessment performed by 2 physicians, $r = 0.7$
Gao <i>et al.</i> (2017) ^[94]	Non-linear state space with a time-variant control signal based on a mathematical model of the carotid dynamics	30 simulated sequences 22 healthy volunteers 81 patients	Intraclass correlation	<i>In silico</i> Accuracy 0.1161–0.1260 mm <i>In vivo</i> <i>Longitudinal</i> Intraclass correlation ≥ 0.9948 95% CI = 0.8871 mm <i>Radial</i> Intraclass correlation ≥ 0.9966 95% CI = 0.4159 mm
Zahnd <i>et al.</i> (2018) ^[101]	Dynamic BM	62 elderly patients at high cardiovascular risk	Average absolute error (\pm SD) from manual reference tracings	$150 \pm 163 \mu\text{m}$
Albinsson <i>et al.</i> (2018) ^[98]	Parabolic sub-sample and grid slope sub-sample interpolation for 2-D BM	1 healthy volunteer 1 phantom 1 <i>in silico</i> simulation (Field II)	Absolute sub-sample estimation errors	Reduced by 24% on phantom data Reduced by 15% on <i>in silico</i> data

BM = block matching; OF = optical flow; WLSOF = weighted least-squares optical flow; ABMM = affine block motion model; RMSE = root mean square error; SD = standard deviation; CI = confidence interval.

Table A1.2. Wall motion extraction techniques based on RF ultrasound signals (chronologic order). Adapted from ^[27]

Study	Technique	Hardware, format of RF data	Data	Performance
Ribbers <i>et al.</i> (2007) ^[173]	Cross-correlation	$f_r = 25 \text{ Hz}$, $f_s = 39 \text{ MHz}$ $f_c = 11 \text{ MHz}$ 15-6 L linear array Philips Sonos 7500 real-	1 physical phantom 12 patients	No quantitative analysis of the <i>in vivo</i> results was performed

time 3-D echo scanner B				
Zahnd <i>et al.</i> (2015) ^[20]	Local phase-based OF (Basarab <i>et al.</i> 2009 ^[129])	$f_r = 91$ Hz $f_s = 50$ MHz $f_c = 4$ MHz, fs50 MHz, ULA-OP research scanner	20 young healthy volunteers 6 elderly patients	Longitudinal: 98 ± 84 μ m Radial: 55 ± 44 μ m
Salles <i>et al.</i> (2015) ^[117]	Transverse oscillations (Liebgott <i>et al.</i> 2010 ^[174])	$f_r = 10$ kHz $f_c = 5$ MHz $f_s = 40$ MHz L14-5 W/60 array Ultrasonix SonixTouch US system (Richmond, BC, Canada)	3 artery numerical phantoms	Mean axial error: 4.2 ± 3.4 μ m Mean lateral errors: 9.9 ± 7.9 μ m Stiffness of the 3 vessel phantom walls investigated was estimated with an average relative error of 2.2%
Hasegawa (2016) ^[175]	Phase tracking with frequency spectra	$f_r = 1302$ Hz $f_s = 31.25$ MHz $f_c = 7.5$ MHz Linear array PU-0558 Ueda Japan Radio (scanner RSYS0002, Microsonic, Tokyo, Japan)	1 phantom	Bias error 1-D: $R_a = 11.5\%$, $L_o = 2.0\%$ Bias error 2-D: $R_a = 3.0\%$, $L_o = 2.0\%$
Zambacevičienė and Jurkonis (2019) ^[122]	Phase correlation and sub-sample algorithm	$f_r = 52$ Hz $f_s = 40$ MHz $f_c = 14$ –5 MHz Linear array Scanner Ultrasonix SonixTouch	1 phantom	NRMSE of detected motion amplitude: 0.21 – 0.41 μ m Coefficient of correlation = 0.95 – 0.98 in case of any determined longitudinal motion function when the phase correlation, sub-pixel algorithm and additional filtering were used
Miyajo and Hasegawa (2018) ^[127]	Matching performed in 2-D Fourier domain	Scanner α -10, Aloka $f_r = 3472$ Hz	1 phantom 1 healthy volunteer	Bias error and SD in lateral velocity estimates: 0.048 and 0.282 mm/s

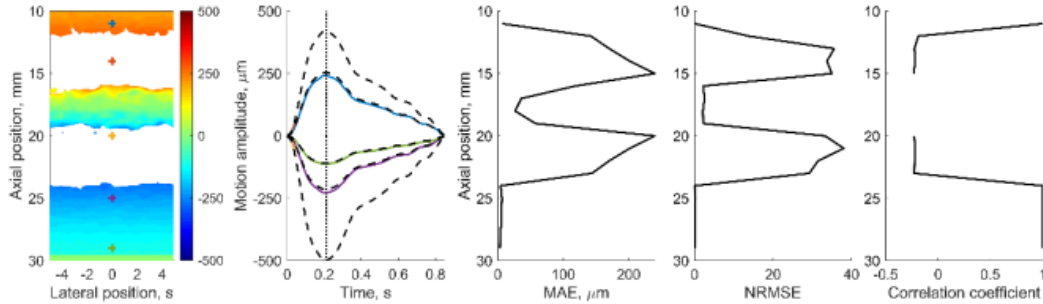
			$f_s = 40 \text{ MHz}$ $f_c = 10 \text{ MHz}$	
			$f_r = 2500 \text{ Hz}$ $f_s = 25 \text{ MHz}$ $f_c = 5 \text{ MHz}$	
Perrot <i>et al.</i> (2018) ^[130]	Video magnification	Linear array L7-4 (Scanner Verasonics Inc., Redmond, WA, USA) Reconstruction technique: Stolts	8 healthy volunteers	Motion magnification by a factor of 1000

RF = radiofrequency; OF = optical flow; NRMSE = normalized root mean square error; fr= frame rate; fs= sample frequency; fc= center frequency.

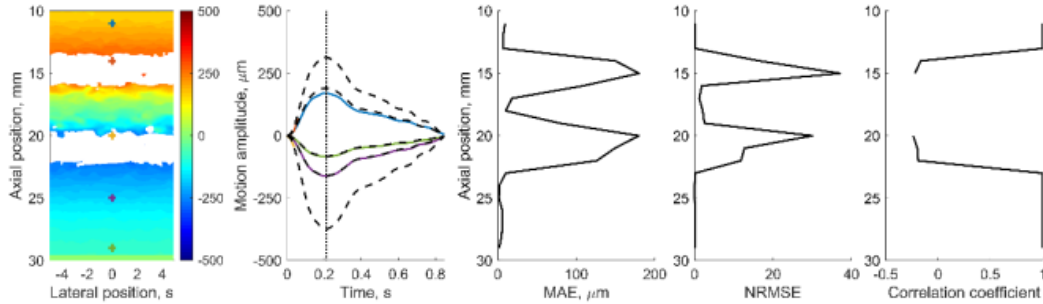
APPENDIX A2

Radial motion estimated by 1D cross-correlation and evaluation of mean absolute error (MAE), normalized root-mean-square error (NRMSE), and Pearson correlation coefficient between estimated and theoretical radial motion. Radial motion map in scanning plane with preselected five points from where the estimated motion is taken and depicted together with theoretical radial motion. Here, the vertical dashed line corresponds to the time the moment of maximal theoretical displacement. At this time moment, a radial motion map is depicted. Finally, MAE, NRMSE, and Pearson correlation coefficient are evaluated in the midline of the motion map at the different axial positions, i.e. starting from 11 mm every 1mm to 29 mm. Inter-frame radial displacements are accumulated relative to the first frame resulting in radial motion. White areas in the motion map correspond to the regions where inter-frame motion is higher than a quarter of the wavelength and exist probability to identify false correlation peak resulting in large tracking errors that are known as “peak hopping” errors.

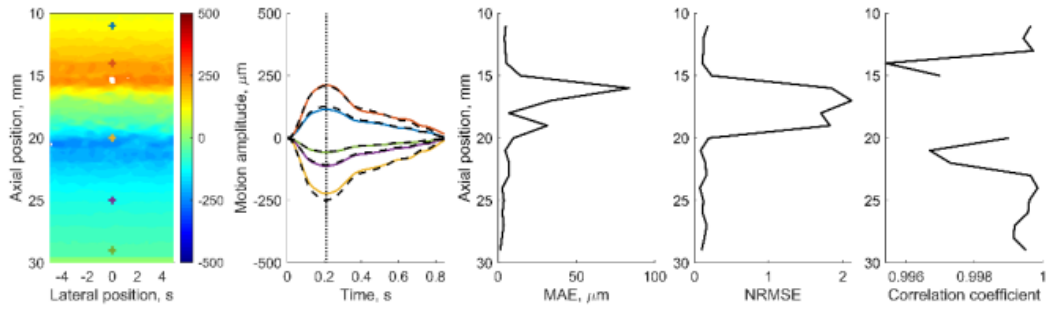
27 years old female, theoretical radial motion peak-to-peak amplitude is 1 mm



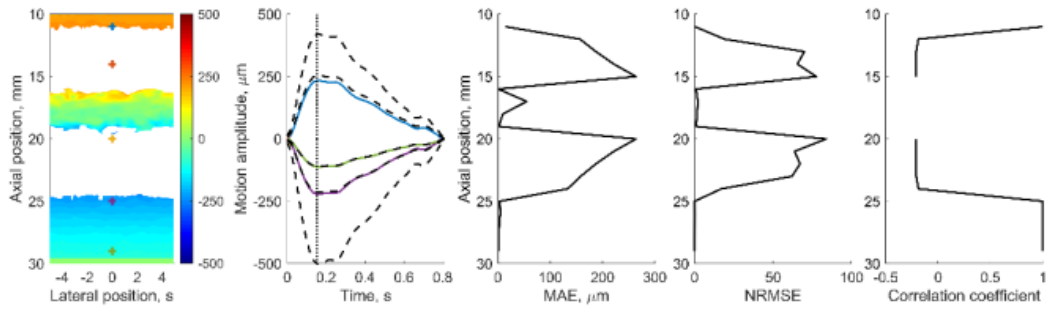
27 years old female, theoretical radial motion peak-to-peak amplitude is 0.75 mm



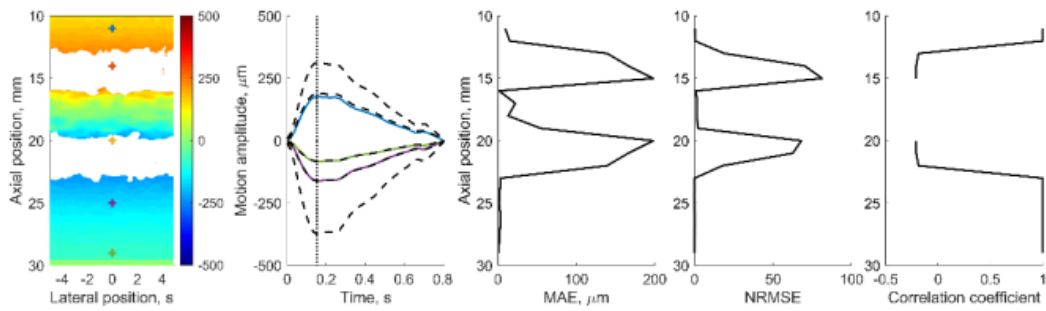
27 years old female, theoretical radial motion peak-to-peak amplitude is 0.5 mm



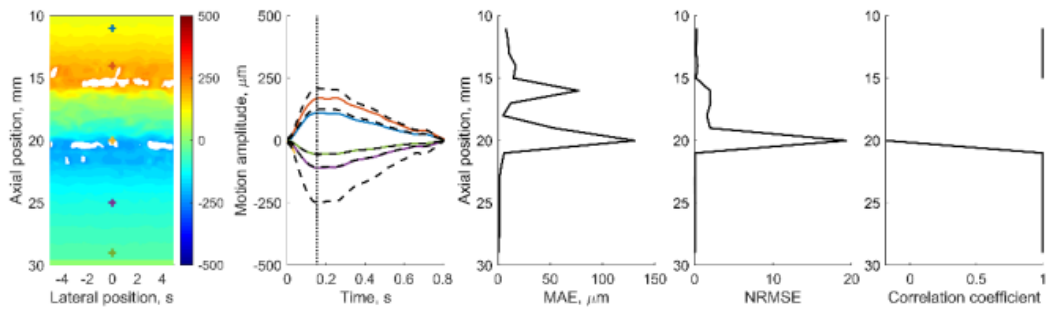
23 years old male, theoretical radial motion peak-to-peak amplitude is 1 mm



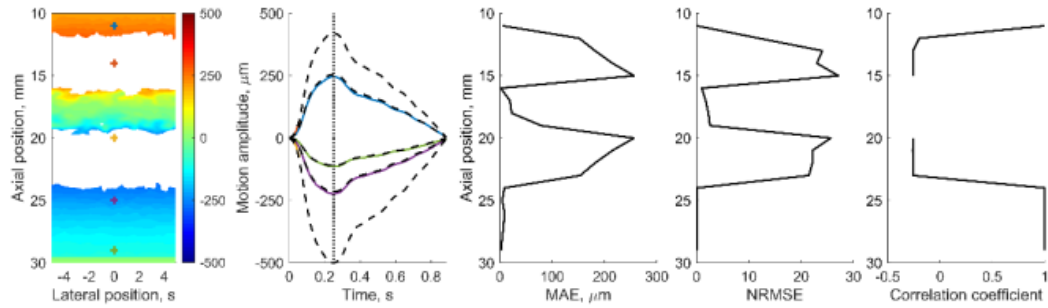
23 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



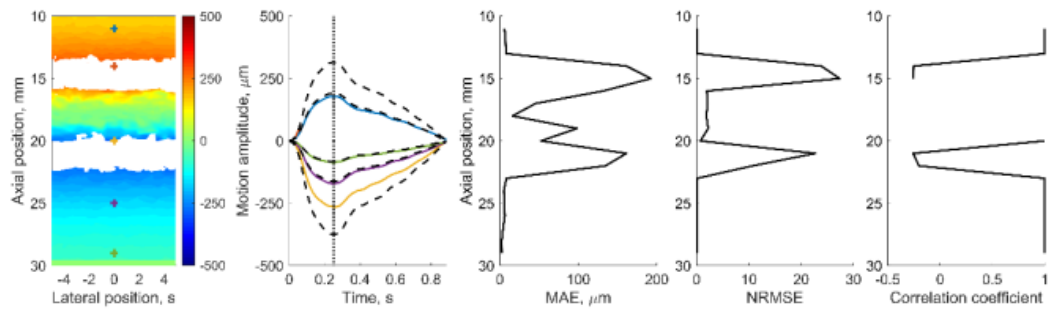
23 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm



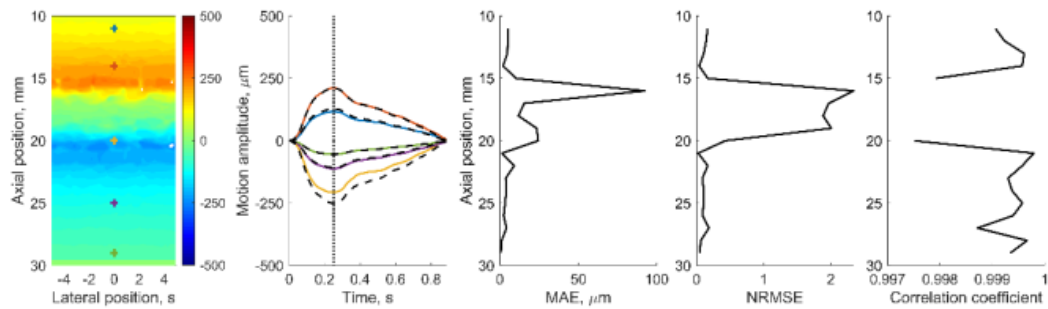
24 years old female, theoretical radial motion peak-to-peak amplitude is 1 mm



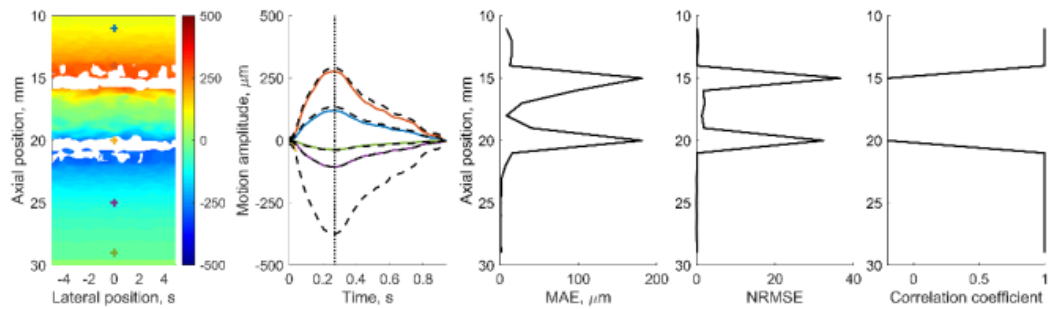
24 years old female, theoretical radial motion peak-to-peak amplitude is 0.75 mm



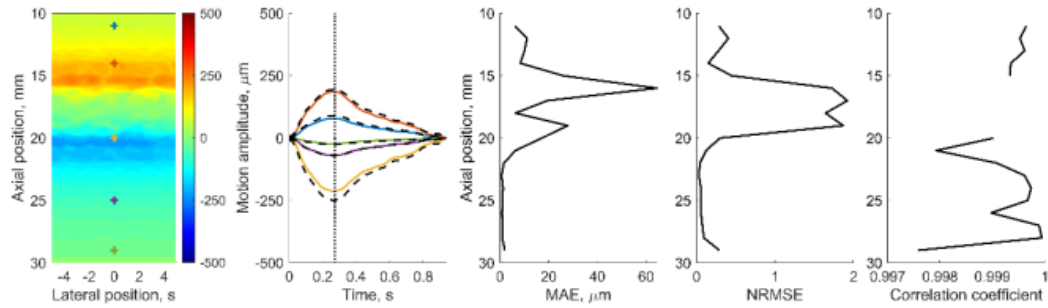
24 years old female, theoretical radial motion peak-to-peak amplitude is 0.5 mm



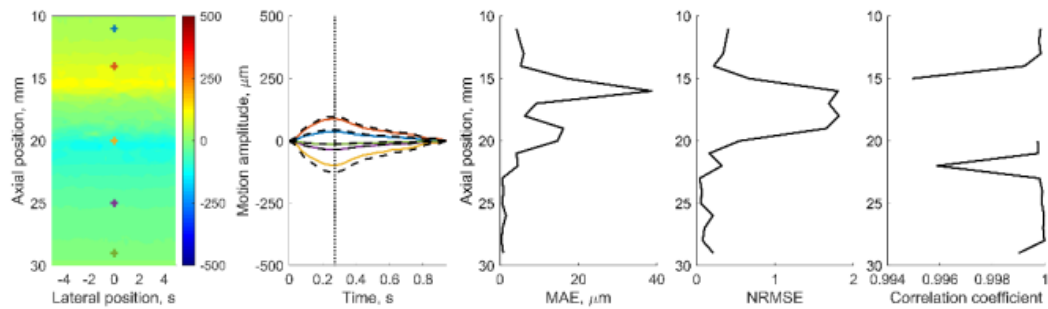
56 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



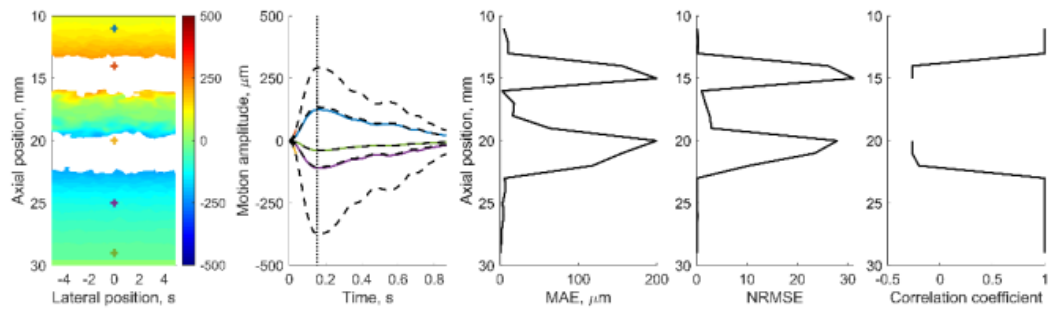
56 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm



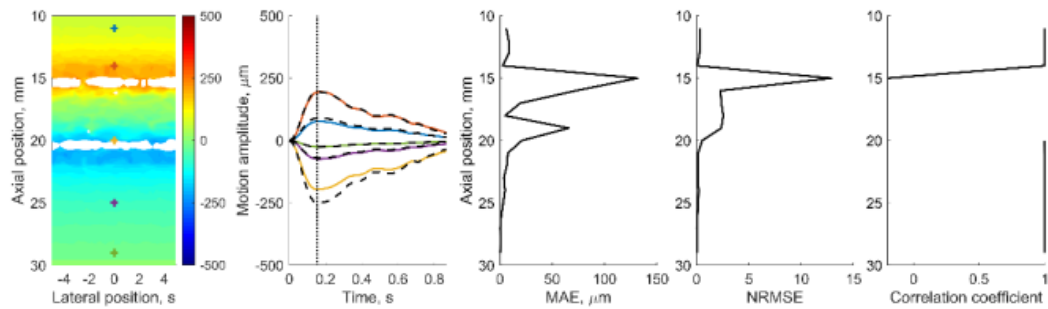
56 years old male, theoretical radial motion peak-to-peak amplitude is 0.25 mm



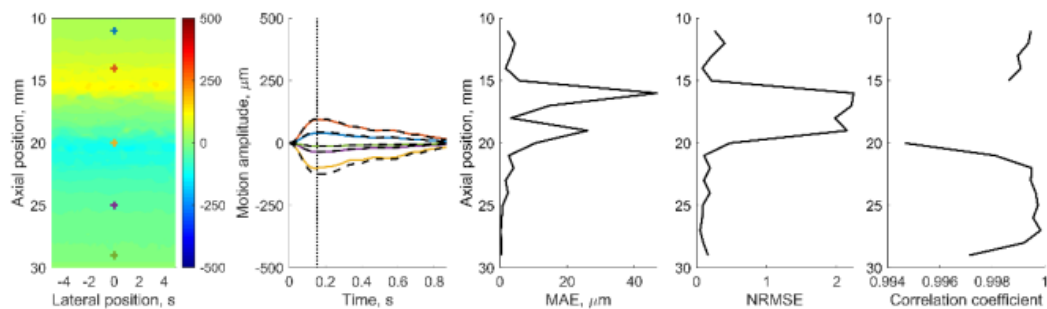
61 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



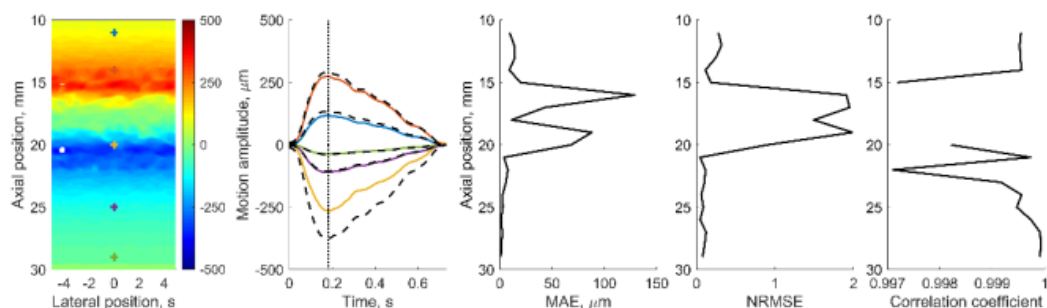
61 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm



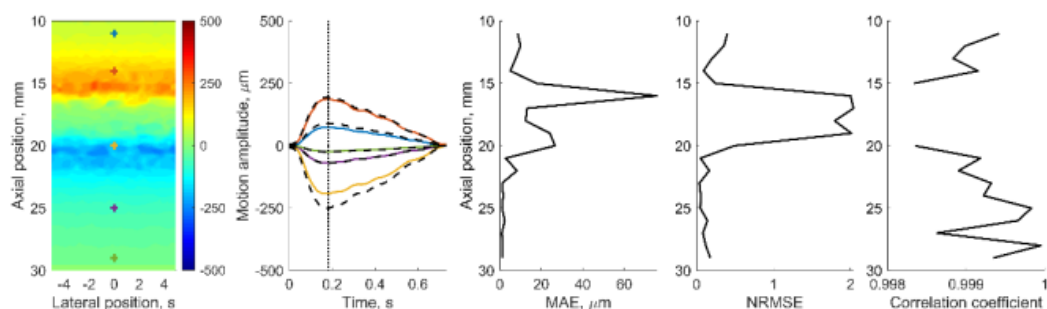
61 years old male, theoretical radial motion peak-to-peak amplitude is 0.25 mm



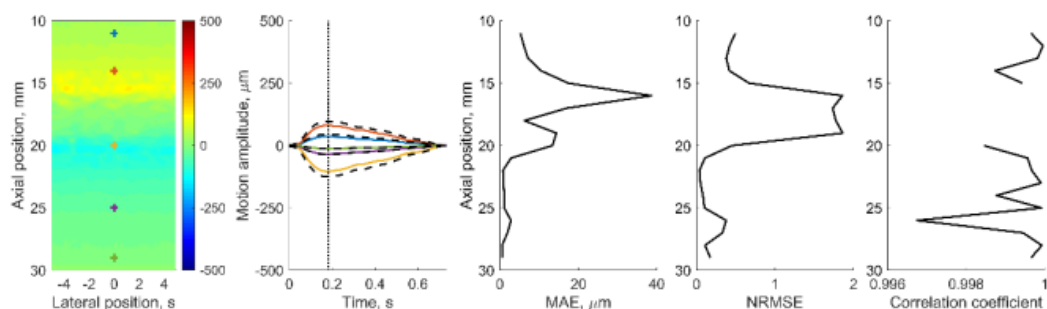
47 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



47 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm

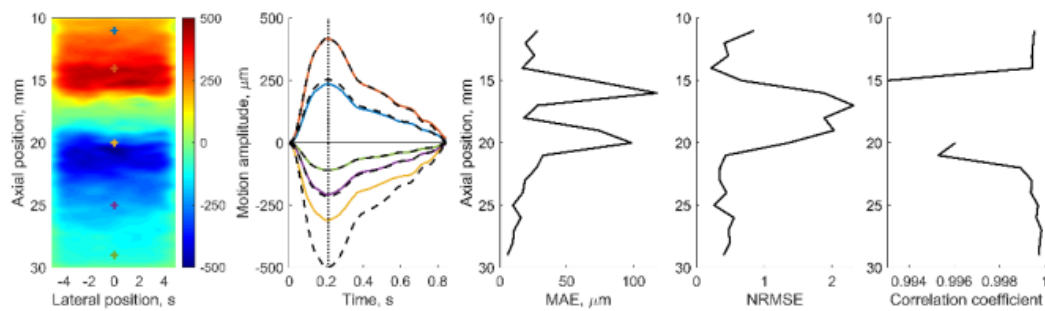


47 years old male, theoretical radial motion peak-to-peak amplitude is 0.25 mm

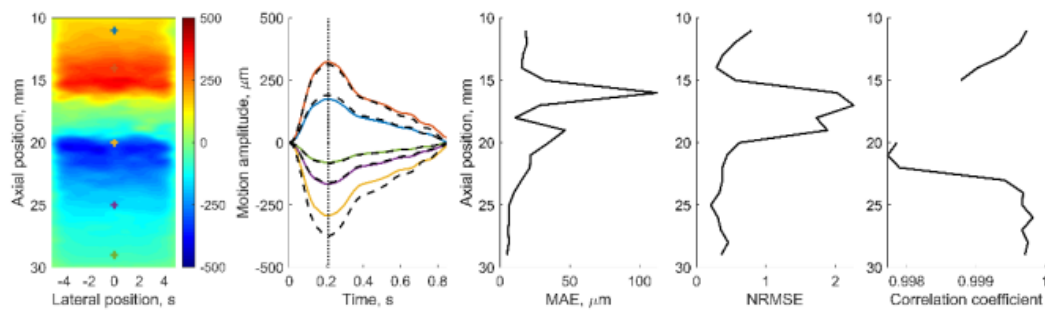


Radial motion estimated by OpenOpticalFlow and evaluation of mean absolute error (MAE), normalized root-mean-square error (NRMSE), and Pearson correlation coefficient between estimated and theoretical radial motion. Radial motion map in scanning plane with preselected five points from where the estimated motion is taken and depicted together with theoretical radial motion. Here, the vertical dashed line corresponds to the time the moment of maximal theoretical displacement. At this time moment, a radial motion map is depicted. Finally, MAE, NRMSE, and Pearson correlation coefficient are evaluated in the midline of the motion map at the different axial positions, i.e. starting from 11 mm every 1mm to 29 mm. Inter-frame radial displacements are accumulated relative to the first frame resulting in radial motion.

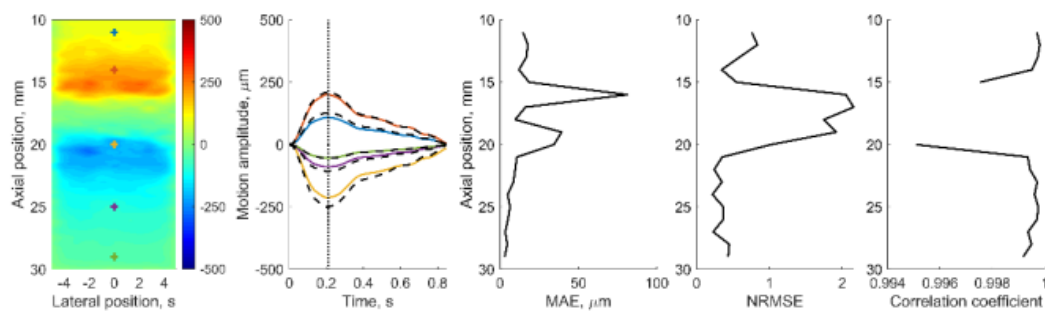
27 years old female, theoretical radial motion peak-to-peak amplitude is 1 mm



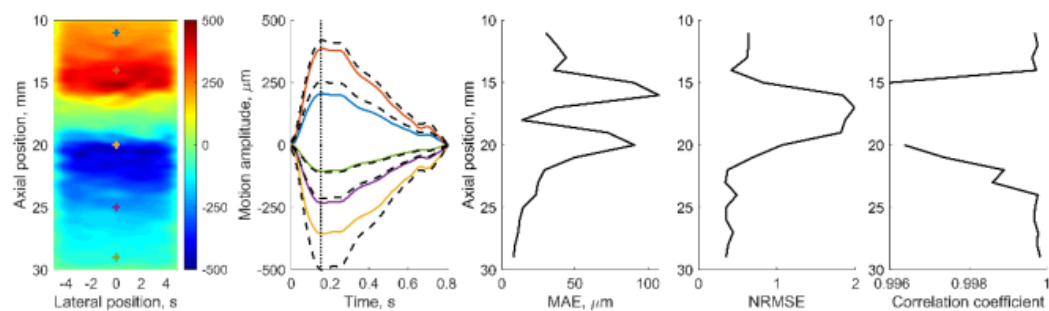
27 years old female, theoretical radial motion peak-to-peak amplitude is 0.75 mm



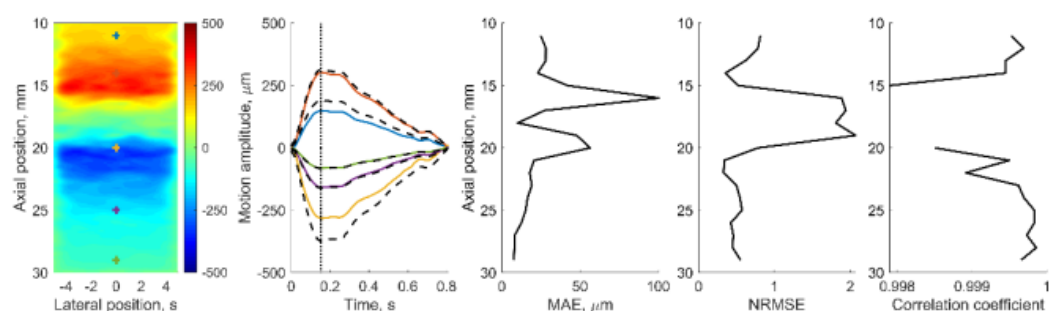
27 years old female, theoretical radial motion peak-to-peak amplitude is 0.5 mm



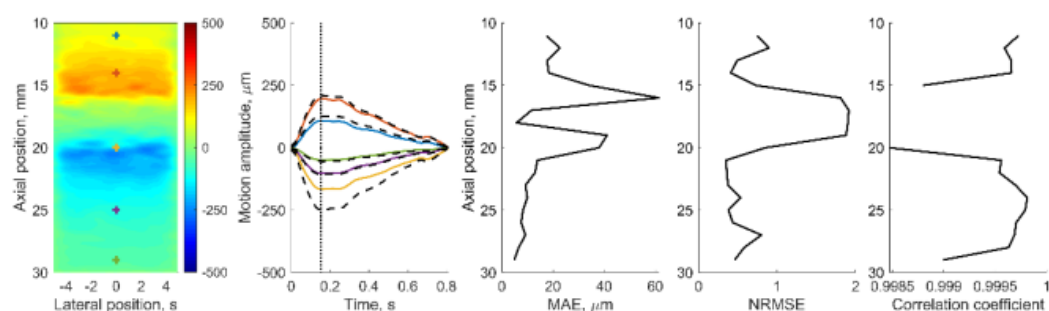
23 years old male, theoretical radial motion peak-to-peak amplitude is 1 mm



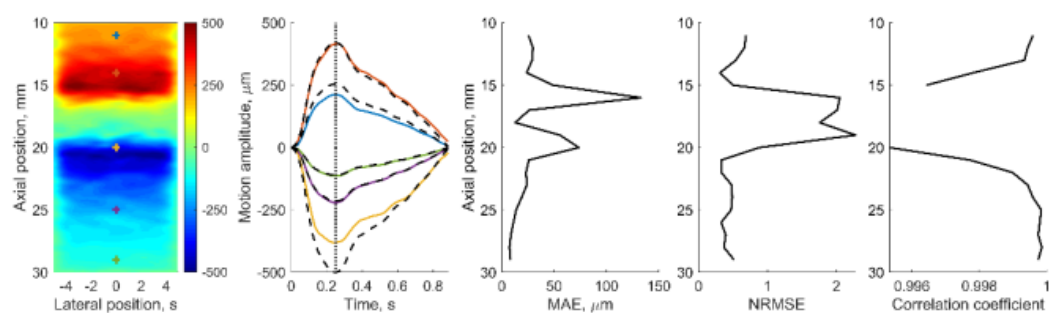
23 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



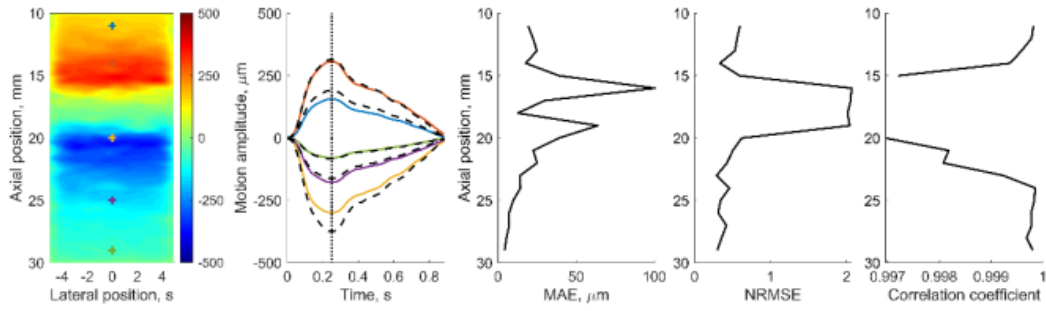
23 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm



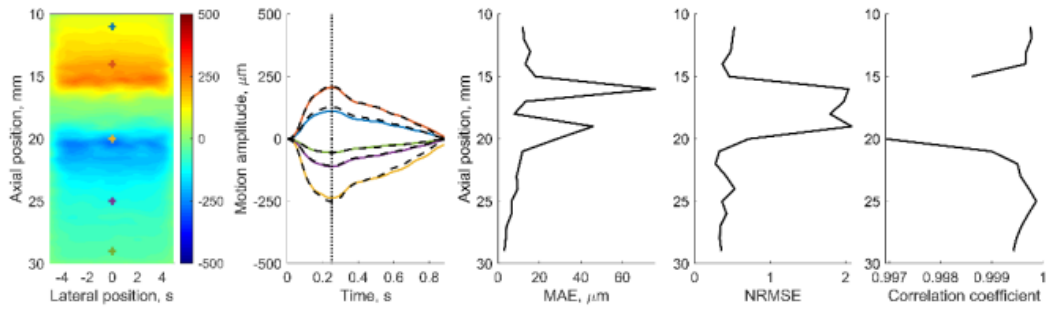
24 years old female, theoretical radial motion peak-to-peak amplitude is 1 mm



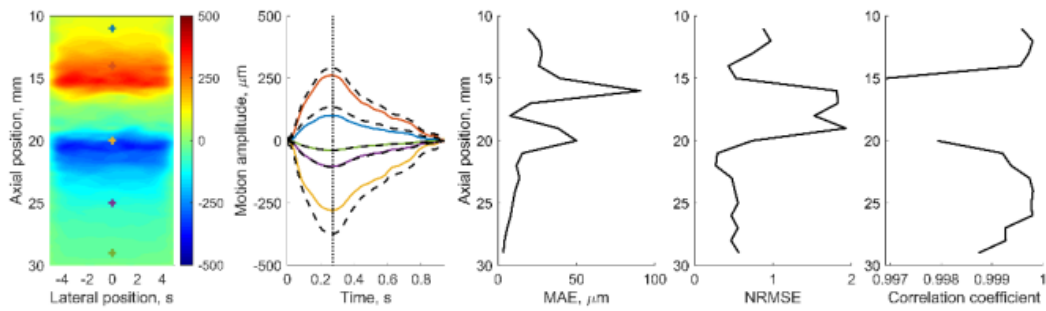
24 years old female, theoretical radial motion peak-to-peak amplitude is 0.75 mm



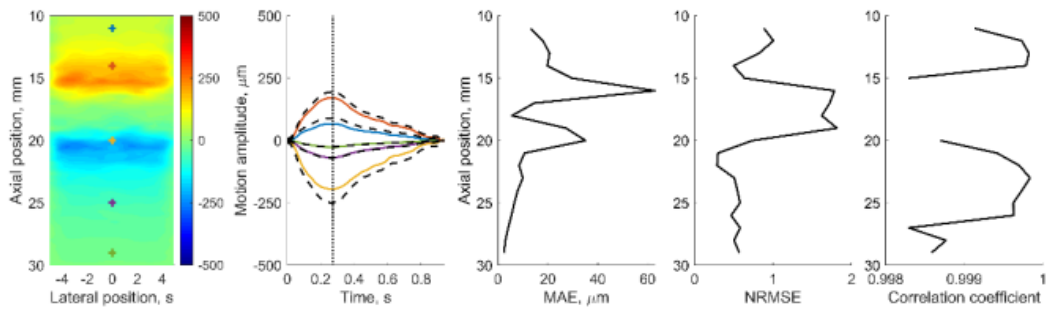
24 years old female, theoretical radial motion peak-to-peak amplitude is 0.5 mm



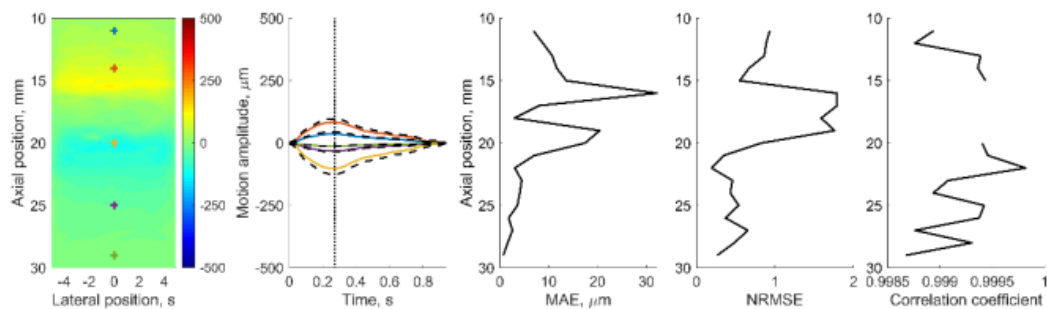
56 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



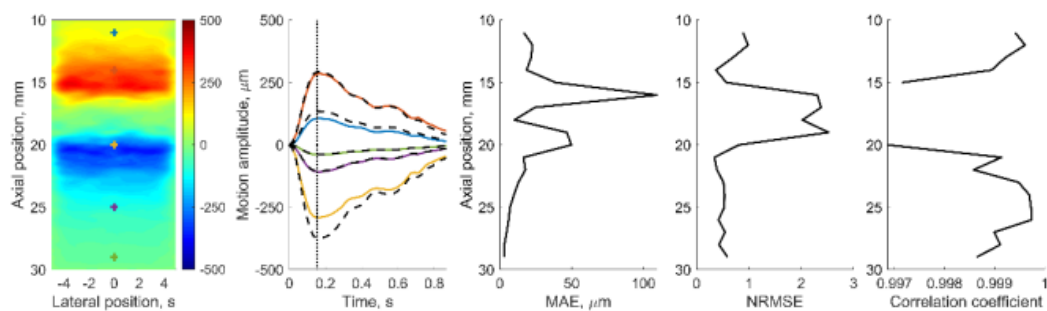
56 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm



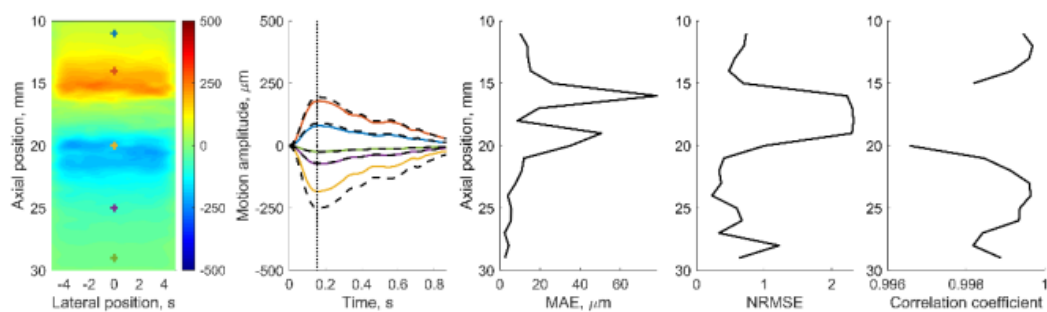
56 years old male, theoretical radial motion peak-to-peak amplitude is 0.25 mm



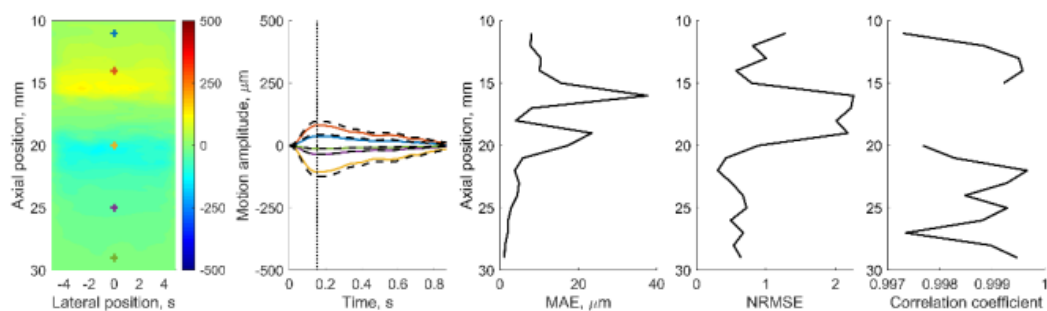
61 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



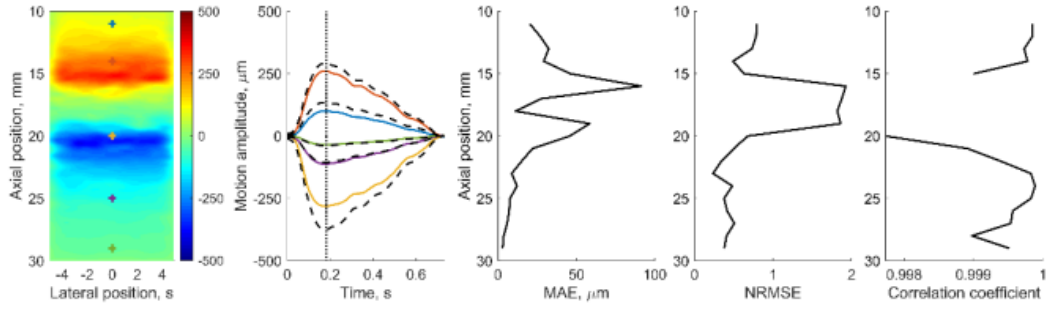
61 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm



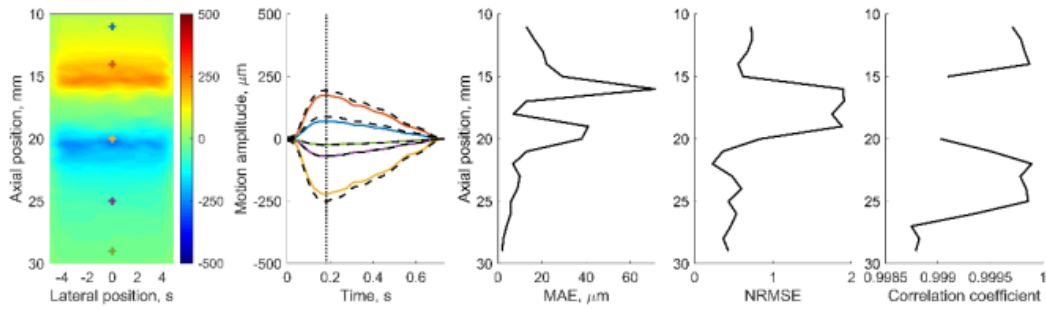
61 years old male, theoretical radial motion peak-to-peak amplitude is 0.25 mm



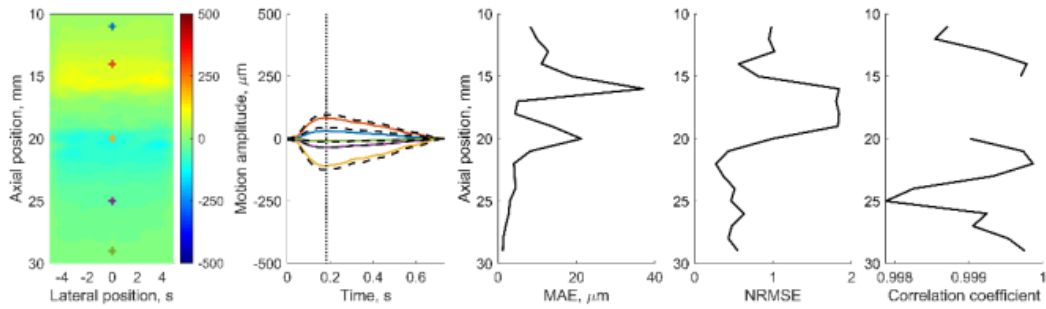
47 years old male, theoretical radial motion peak-to-peak amplitude is 0.75 mm



47 years old male, theoretical radial motion peak-to-peak amplitude is 0.5 mm

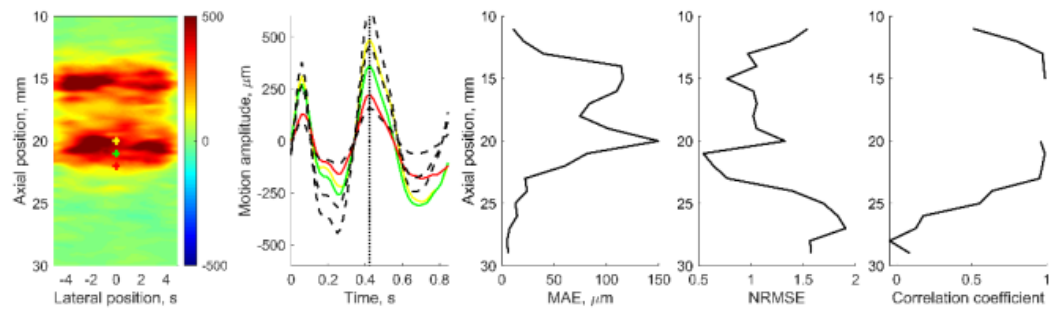


47 years old male, theoretical radial motion peak-to-peak amplitude is 0.25 mm

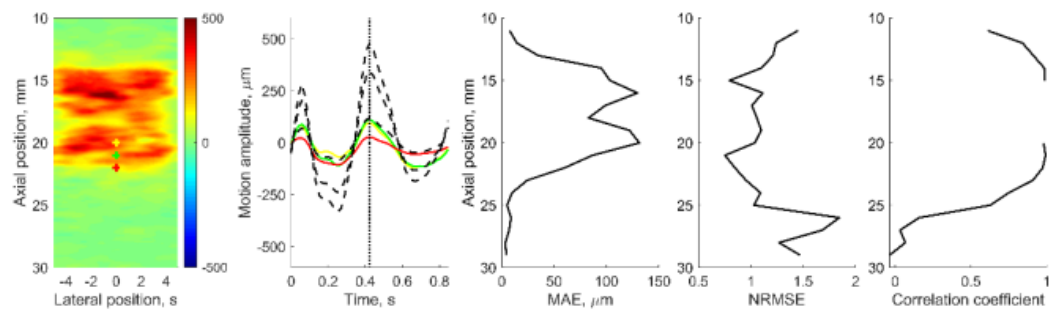


Longitudinal motion estimated by OpenOpticalFlow and evaluation of mean absolute error (MAE), normalized root-mean-square error (NRMSE), and Pearson correlation coefficient between estimated and theoretical longitudinal motion. Longitudinal motion map in scanning plane with preselected three points from where the estimated motion is taken and depicted together with theoretical longitudinal motion. Here, the vertical dashed line corresponds to the time the moment of maximal positive theoretical displacement. At this time moment, a longitudinal motion map is depicted. Finally, MAE, NRMSE, and Pearson correlation coefficient are evaluated in the midline of the motion map at the different axial positions, i.e. starting from 11 mm every 1mm to 29 mm. Inter-frame longitudinal displacements are accumulated relative to the first frame resulting in longitudinal motion.

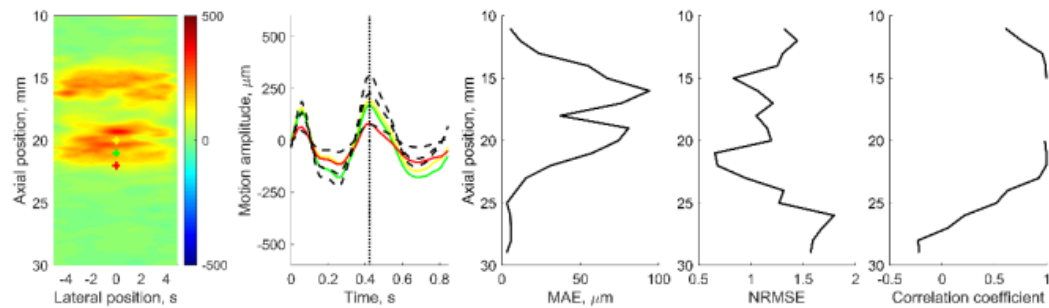
27 years old female, theoretical longitudinal motion peak-to-peak amplitude is 1 mm



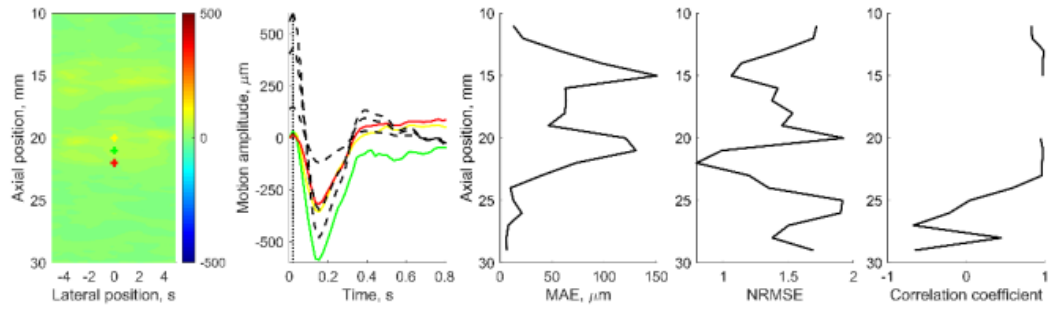
27 years old female, theoretical longitudinal motion peak-to-peak amplitude is 0.75 mm



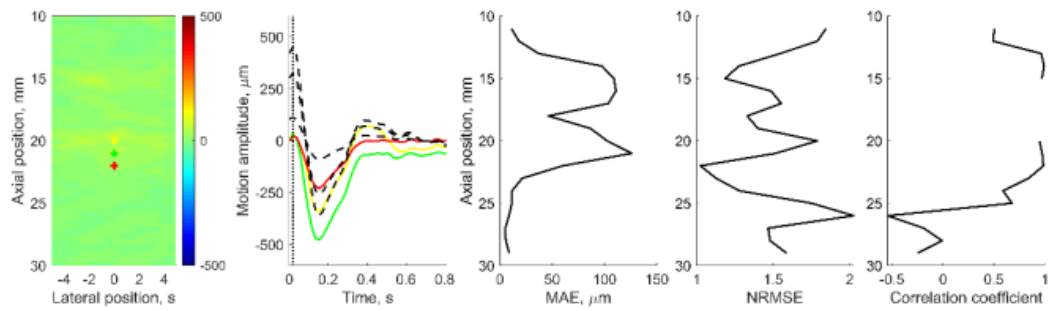
27 years old female, theoretical longitudinal motion peak-to-peak amplitude is 0.5 mm



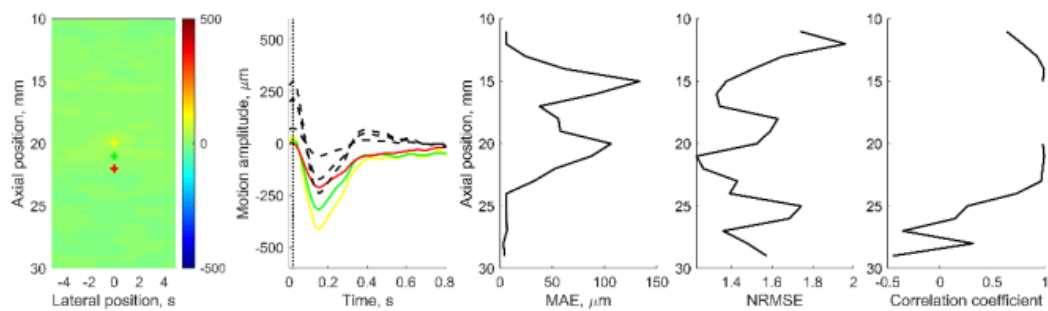
23 years old male, theoretical longitudinal motion peak-to-peak amplitude is 1 mm



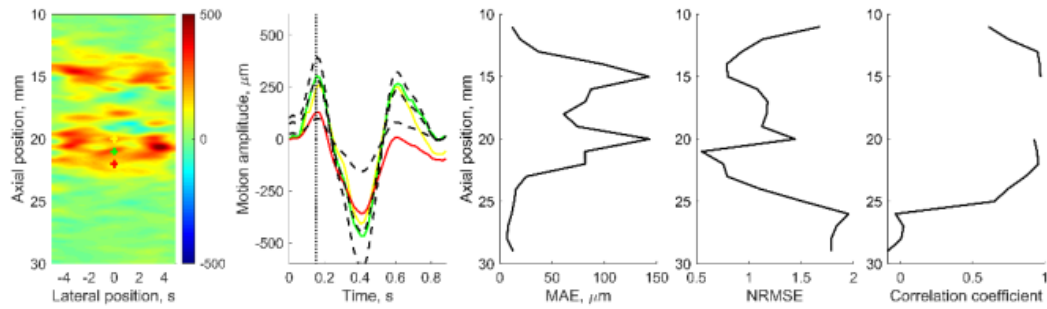
23 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.75 mm



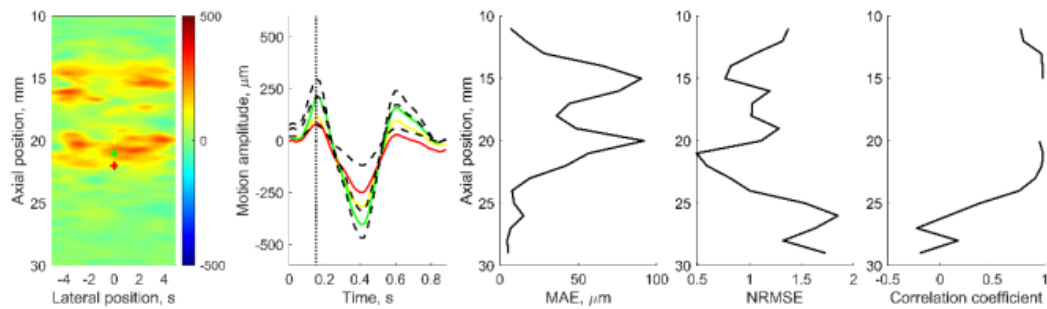
23 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.5 mm



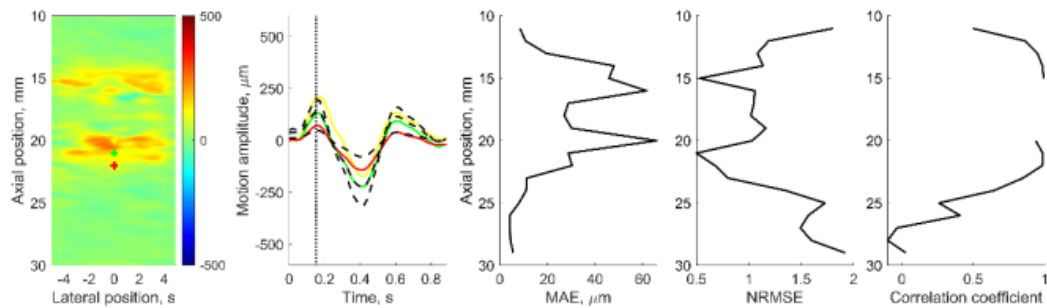
24 years old female, theoretical longitudinal motion peak-to-peak amplitude is 1 mm



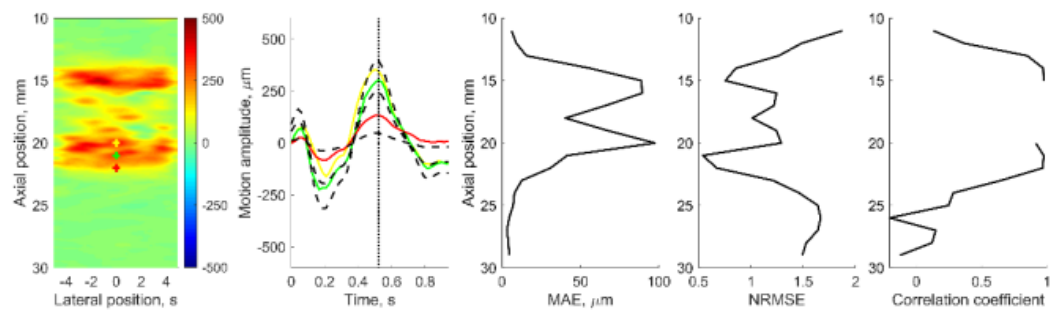
24 years old female, theoretical longitudinal motion peak-to-peak amplitude is 0.75 mm



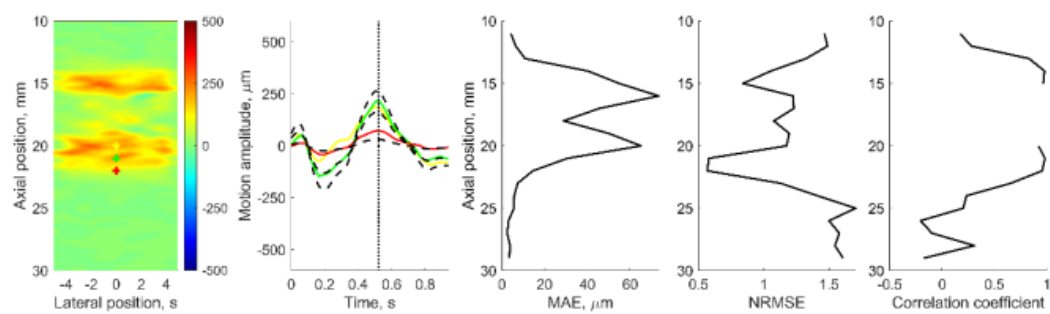
24 years old female, theoretical longitudinal motion peak-to-peak amplitude is 0.5 mm



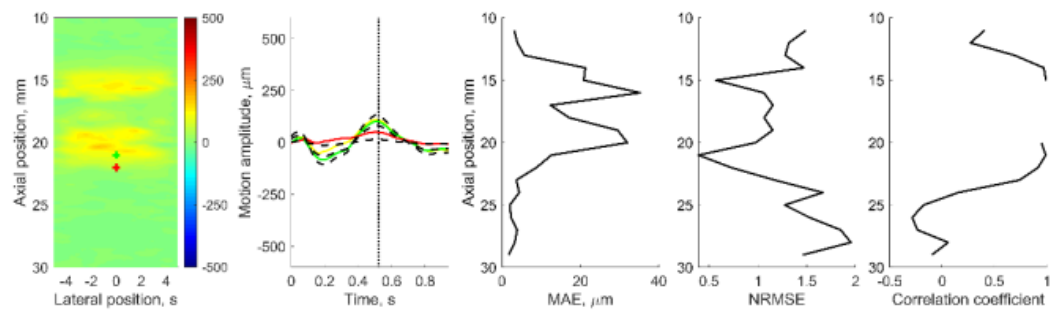
56 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.75 mm



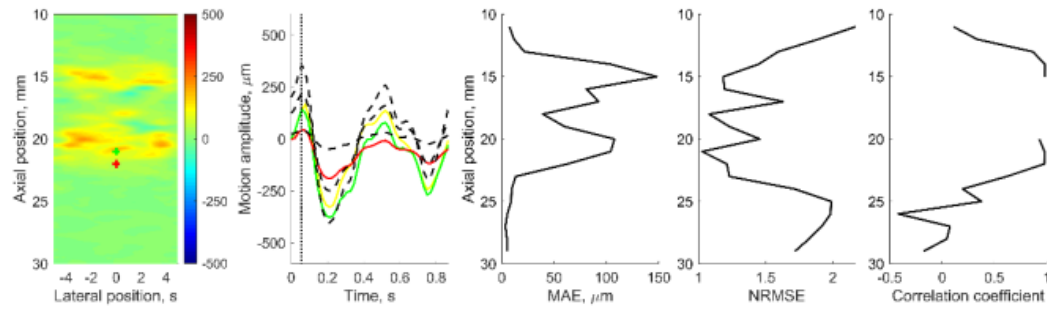
56 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.5 mm



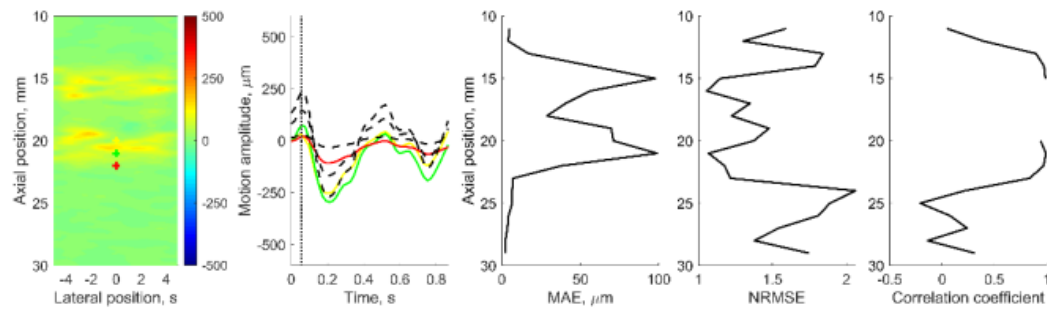
56 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.25 mm



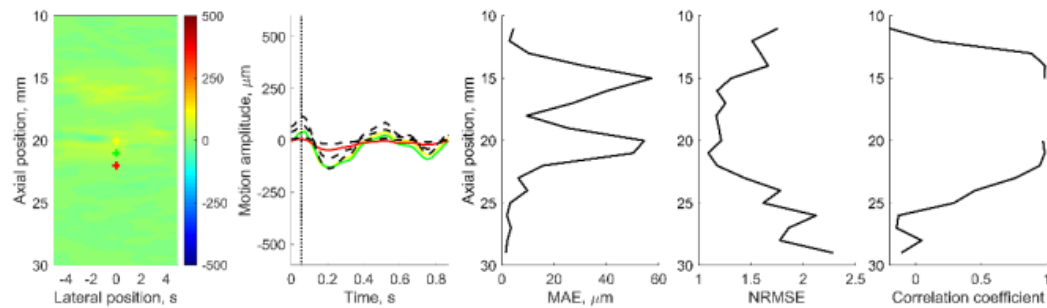
61 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.75 mm



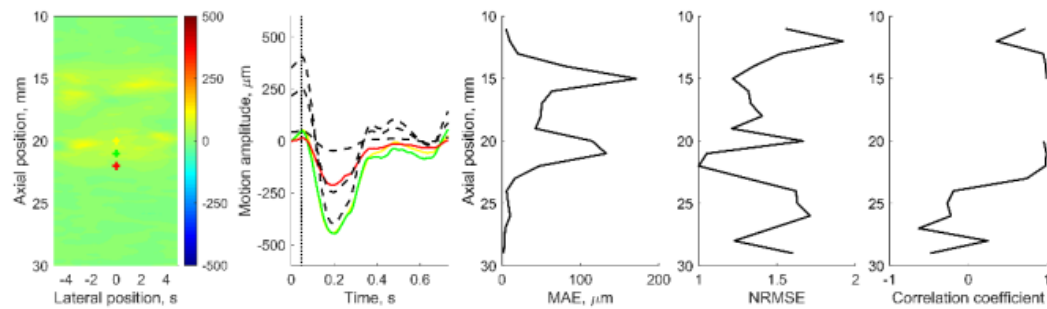
61 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.5 mm



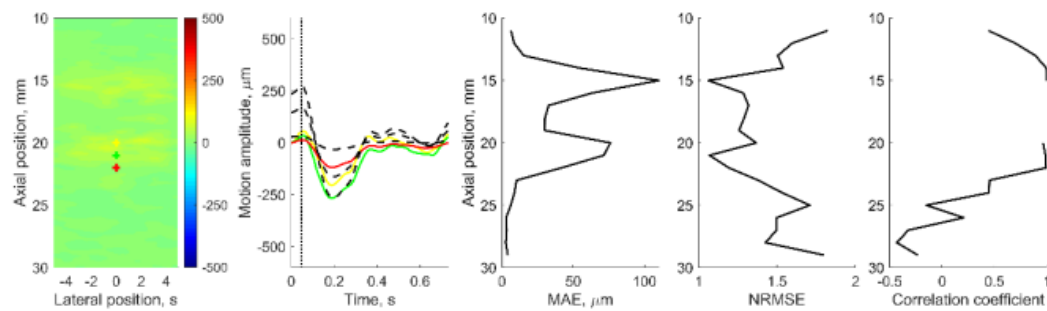
61 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.25 mm



47 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.75 mm



47 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.5 mm



47 years old male, theoretical longitudinal motion peak-to-peak amplitude is 0.25 mm

